

A Turing Machine is a 7-tuple,
 $(Q, \Sigma, \Gamma, \delta, q_0, q_{\text{accept}}, q_{\text{reject}})$

1. Q is the set of states.
2. Σ — input alphabet not containing " $\sqcup$ ".
3. Γ — tape alphabet, " $\sqcup$ " $\in \Gamma$ and $\Sigma \subseteq \Gamma$.
4. $\delta: Q \times \Gamma \rightarrow Q \times \Gamma \times \{L, R\}$ is the transition function
5. $q_0 \in Q$ is the start state
6. $q_{\text{accept}} \in Q$ is the accept state
7. $q_{\text{reject}} \in Q$ is the reject state, where
 $q_{\text{accept}} \neq q_{\text{reject}}$.

- A language is Turing-recognizable if some Turing machine recognizes it.
- 3 outcomes for a TM:
accept, reject, loop.
- Looping is difficult to be distinguished from taking a long time to compute.
- A TM decides over a language A if it either accepts or rejects A .
- A language is Turing-decidable or decidable if some TM decides it.