

## CS 350 Theory of Computation

### Assignment 4 (8 marks)

#### Question 1 (1 marks)

Let  $\mathcal{B}$  be the set of all infinite sequences over  $\{0, 1\}$ . Show that  $\mathcal{B}$  is uncountable, using a proof by diagonalization.

#### Question 2 (1 marks)

Let  $T = \{(i, j, k) \mid i, j, k \in \mathcal{N}\}$ . Show that  $T$  is countable.

#### Question 3 (2 marks)

Let  $INFINITE_{PDA} = \{ \langle M \rangle \mid M \text{ is a PDA and } L(M) \text{ is an infinite language} \}$ . Show that  $INFINITE_{PDA}$  is decidable.

#### Question 4 (2 marks)

Show that  $EQ_{CFG}$  is undecidable.

#### Question 5 (1 marks)

Show that  $EQ_{CFG}$  is co-Turing-recognizable.

#### Question 6 (1 marks)

Problem 5.3 (page 195—first edition; page 211—second edition).

**Date Due:** before the end of class on **Friday, March 24, 2006**. Late assignment will lose 2 marks for each overdue day.