

$$2.4(c) \quad S \rightarrow XSX \mid X$$

$$X \rightarrow \text{~~XXXX~~ } 0 \mid 1$$

$$(A) \quad S \rightarrow S$$

$$2.6(b) \quad S \rightarrow bw \mid awbaw \mid \epsilon \quad N$$

$$w \rightarrow aw \mid bw \mid \epsilon$$

$$\{a, b\}^*$$

$$N \rightarrow aNb \mid A \mid B$$

$$a^i b^j \quad i \neq j$$

$$A \rightarrow aA \mid a$$

$$a^k \quad k \geq 1$$

$$B \rightarrow bB \mid b$$

$$b^k \quad k \geq 1$$

2.14

add S_0

$$S_0 \rightarrow A$$

$$A \rightarrow BAB \mid B \mid \epsilon$$

$$B \rightarrow 00 \mid \epsilon$$

eliminate $B \rightarrow \epsilon$

$$S_0 \rightarrow A$$

$$A \rightarrow BAB \mid B \mid \epsilon \mid AB \mid BA \mid \cancel{A}$$

$$B \rightarrow 00$$

can eliminate
since $A \rightarrow A$
does nothing

2.14

eliminate $A \rightarrow \epsilon$
new

$$S_0 \rightarrow A | \epsilon$$

$$A \rightarrow BAB | B | AB | BA | BB | \epsilon\epsilon$$

$$B \rightarrow \epsilon\epsilon$$

new

remove $A \rightarrow B$

$$S_0 \rightarrow A | \epsilon$$

$$A \rightarrow \epsilon\epsilon B | AB | BA | BB | \epsilon\epsilon$$

$$B \rightarrow \epsilon\epsilon$$

remove $S_0 \rightarrow A$

$$S_0 \rightarrow \epsilon | BAB | AB | BA | BB | \epsilon\epsilon$$

$$A \rightarrow BAB | AB | BA | BB | \epsilon\epsilon$$

$$B \rightarrow \epsilon\epsilon$$

convert remaining rules

$$S_0 \rightarrow \epsilon | BC | AB | BA | BB | \epsilon\epsilon$$

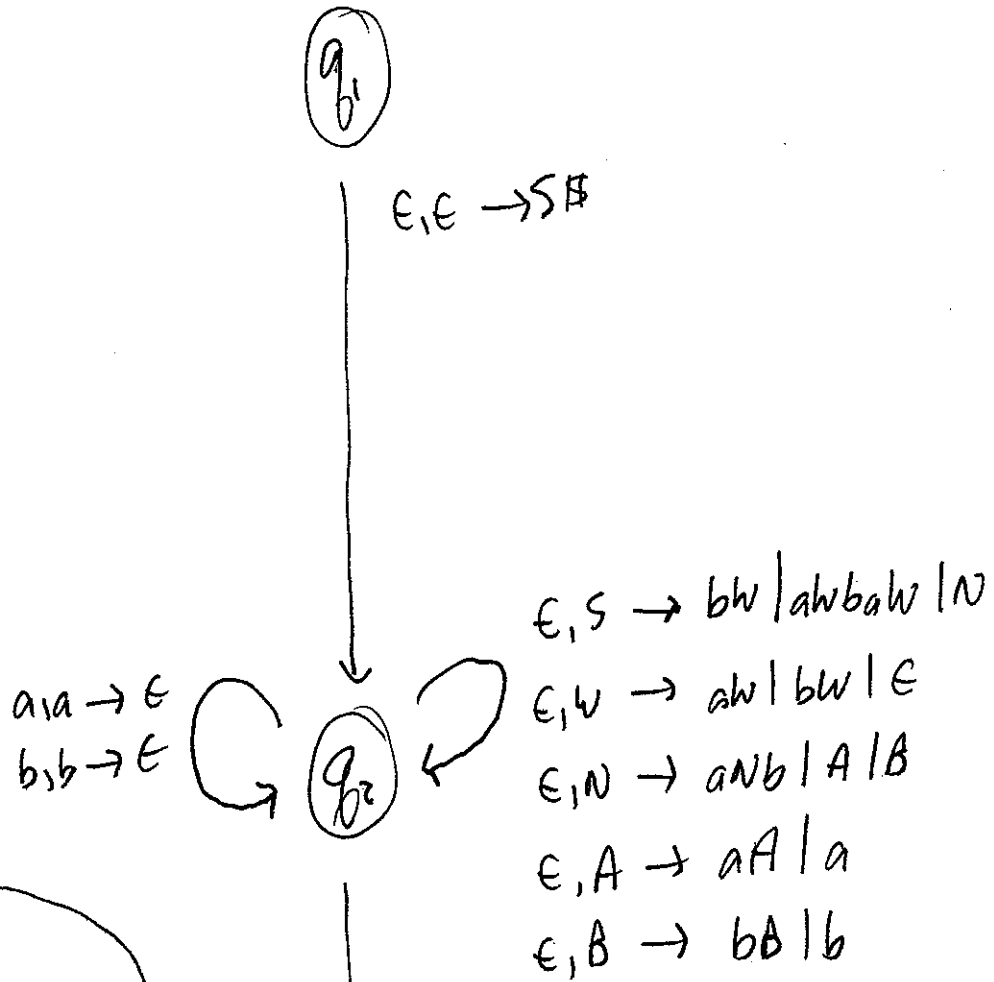
$$A \rightarrow BC | AB | BA | BB | \epsilon\epsilon$$

$$B \rightarrow \epsilon\epsilon$$

$$C \rightarrow AB$$

$$\epsilon \rightarrow \epsilon$$

#4



add states for
multiple state productions
as follows:

- bw : q_4
- awbaw : q_5, q_6, q_7, q_8
- aw : q_9
- aNb : q_{10}, q_{11}
- aA : q_{12}
- bB : q_{13}
- S# : q_{14}

see #6 for example

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$$Q = \{q_1, \dots, q_{14}\}$$

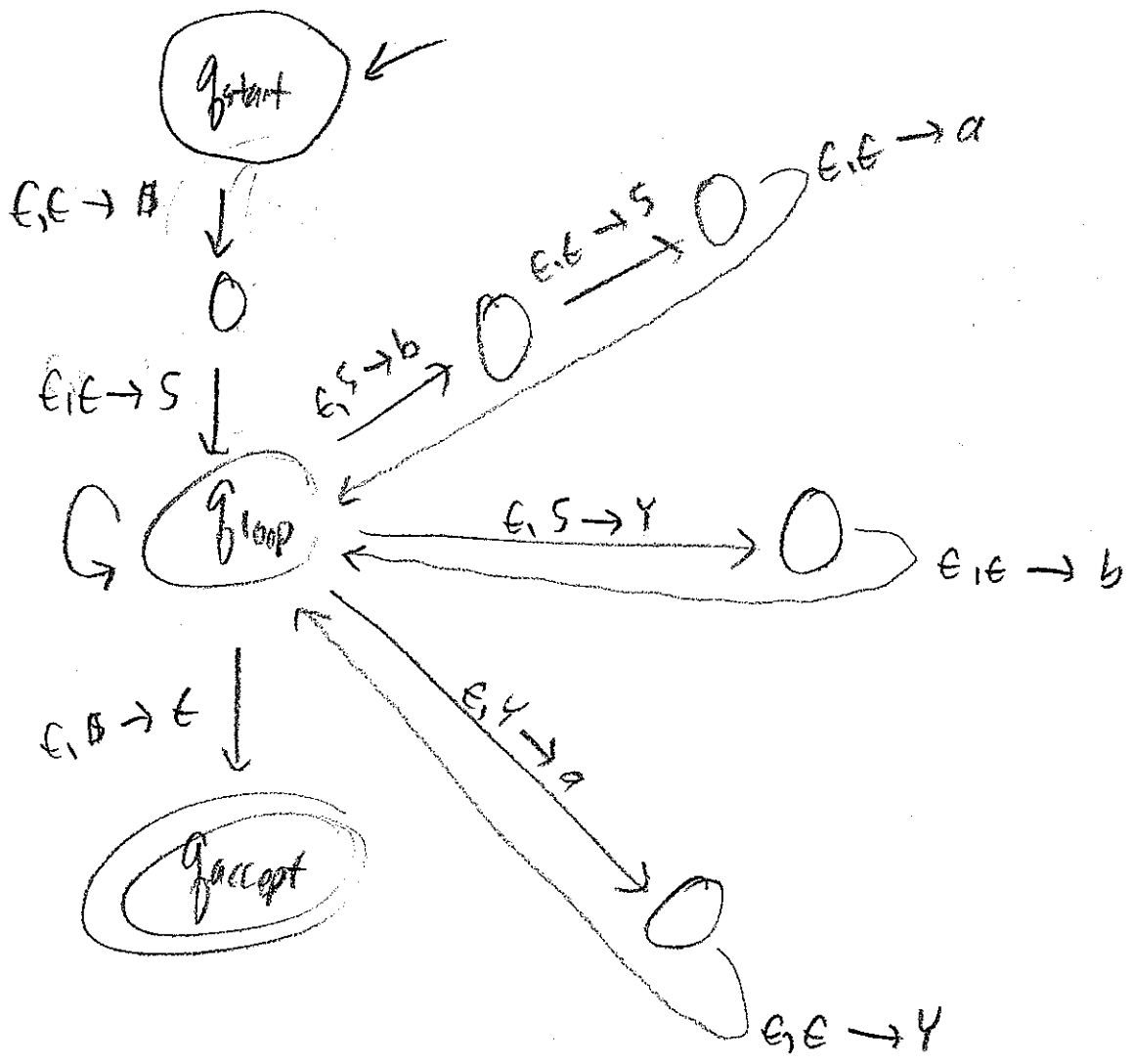
$$\Sigma = \{a, b\}$$

$$\Gamma = \{a, b, \#, S, W, N, A, B\}$$

$$q_0 = q_1$$

$$R = \{q_3\}$$

#6



$\epsilon, y \rightarrow \epsilon$
 $a, a \rightarrow \epsilon$
 $b, b \rightarrow \epsilon$