

Example 3:

$L = \{w \mid w \text{ has an equal number of a's, b's, and c's}\}$

ex: $abacccb \in L$

Step 1: $S = a^p b^p c^p$ $|S| = 3p > p$ \checkmark
 $S \in L$

Step 2: Case 1: V or y contain 1 or more a's
 V and y cannot contain c's since that would
require $|Vxy| > p$

Case 2: V or y contain 1 or more c's
 V and y cannot contain a's since that
would require $|Vxy| > p$

Case 3: V and y contain just b

note: V and y cannot contain all three letters
as that would require $|Vxy| > p$

Step 3: Case 1: UV^2xy^2z ~~has~~ contains more
a's than c's so $UV^2xy^2z \notin L$

Case 2: UV^2xy^2z contains p c's and
more than p number of a's so $UV^2xy^2z \notin L$

Case 3: UV^2xy^2z contains p number of
a's and c's but the number of b's
is larger than p so $UV^2xy^2z \notin L$