

CSCI 132:

Basic Data Structures and Algorithms

Sorting (Bubble Sort)

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Fall 2023

Announcements

Lab 11 due **Thursday** @ 11:59 PM

Program 4 Due **FRIDAY** @ 11:59 PM

Friday will be a work day/help session for
Program 4 (no lecture)

Sorting

We will spend the next several lectures discussing how to **sort** a set of values (typically an Array of ints)

Sorting a dataset is a very frequently done task, and working with a sorted dataset is much easier than working with an unsorted dataset

Instead of saying `Array.Sort()`, we will write **four** different sorting algorithms

Sorting

We will spend the next several lectures discussing how to **sort** a set of values (typically an Array of ints)

Sorting a dataset is a very frequently done task, and working with a sorted dataset is much easier than working with an unsorted dataset

Instead of saying `Array.Sort()`, we will write **four** different sorting algorithms

First, let's write a method that will generate an N-sized array filled with random integers (1-100)

Sorting

```
public int[] getRandomArray(int n) {  
    int[] array = new int[n];  
    Random rand = new Random();  
    for(int i = 0; i < array.length; i++) {  
        array[i] = rand.nextInt(101);  
    }  
    return array;  
}
```

Bubble Sort

Iterate through an array and compare **pairs** in the array. When comparing two numbers, if one is bigger than the other, **swap**. Keep iterating until array is sorted

7	2	5	3	9	1	6
---	---	---	---	---	---	---

Bubble Sort

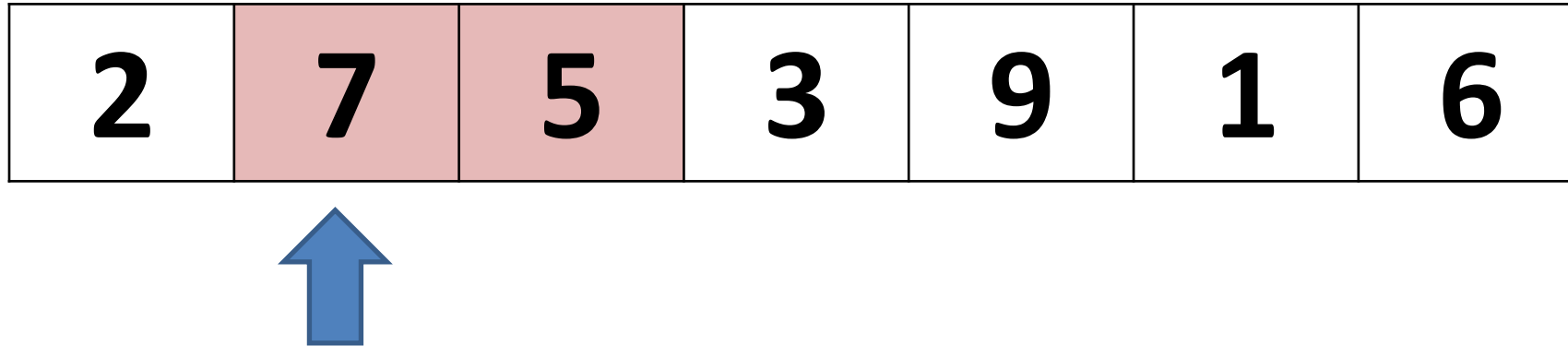
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Is 7 greater than 2? → SWAP

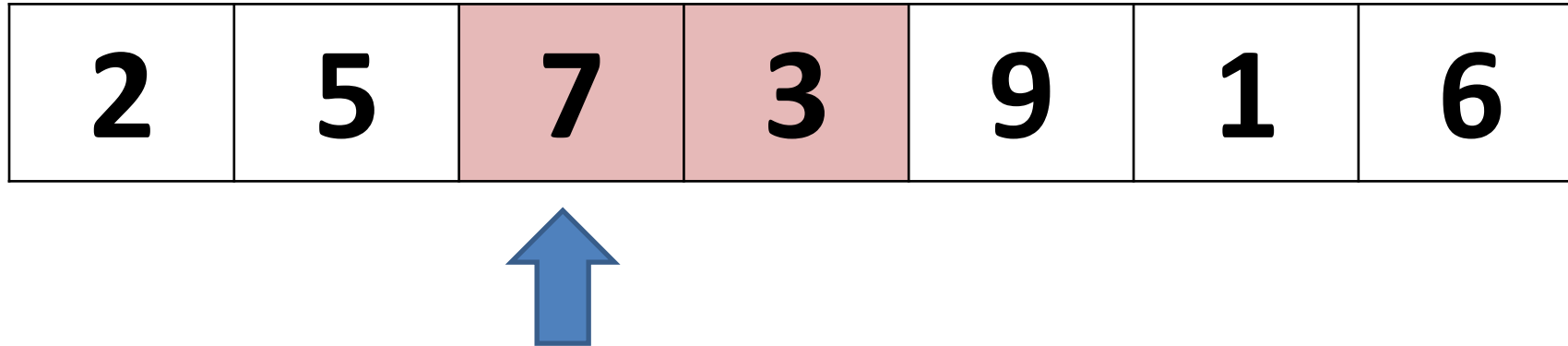
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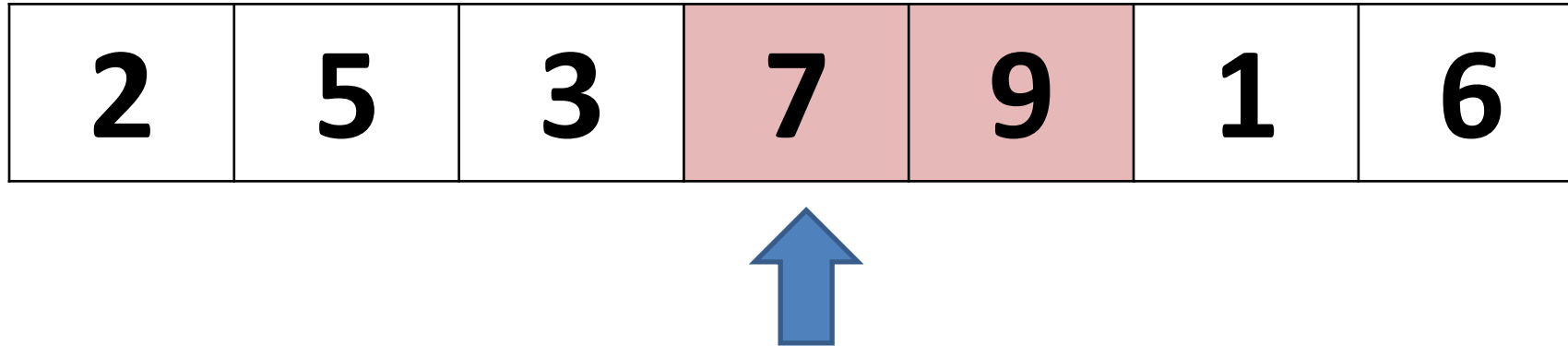
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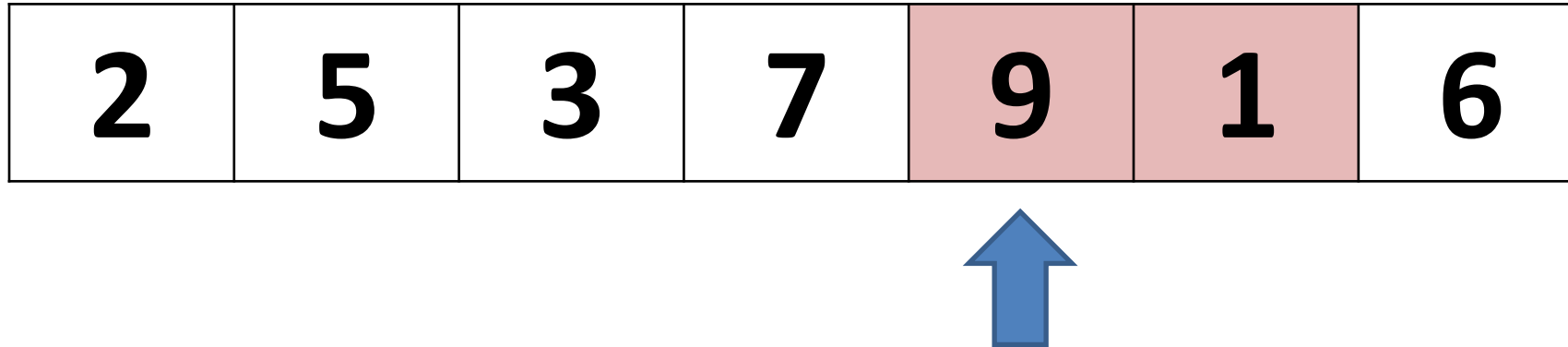
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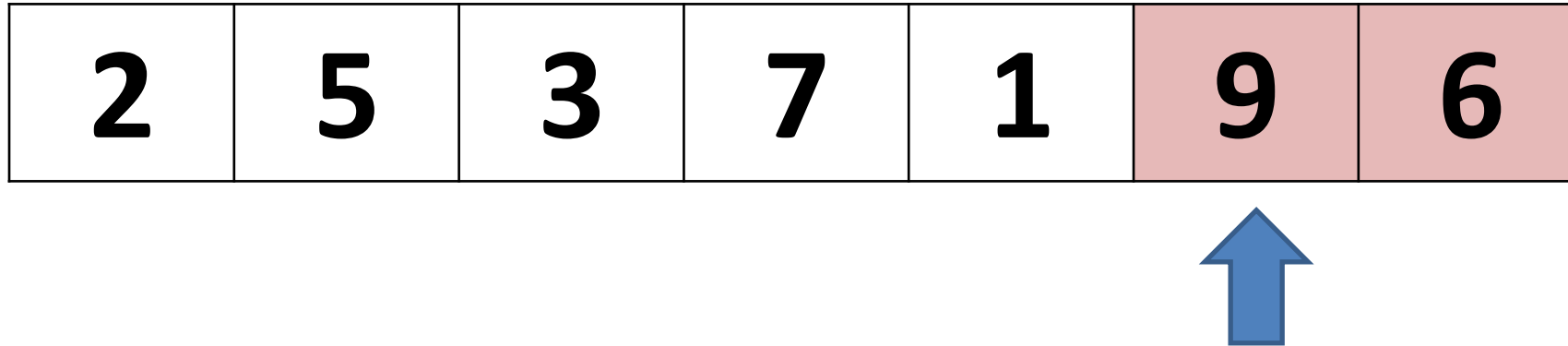
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Bubble Sort

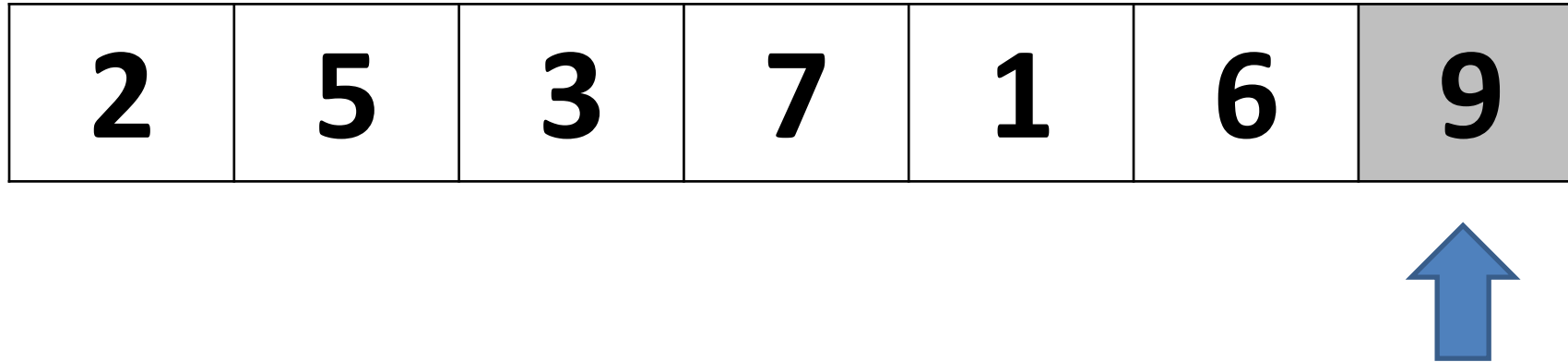
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2	5	3	7	1	6	9
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Bubble Sort

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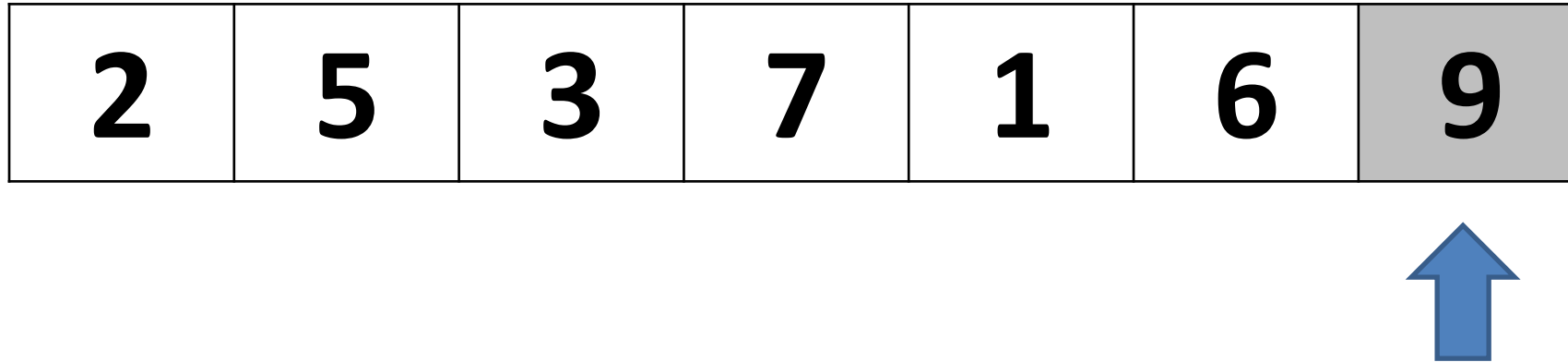


At this point, 9 (the biggest number) is at the correct spot in the array.

So, we no longer need to check that index!

Bubble Sort

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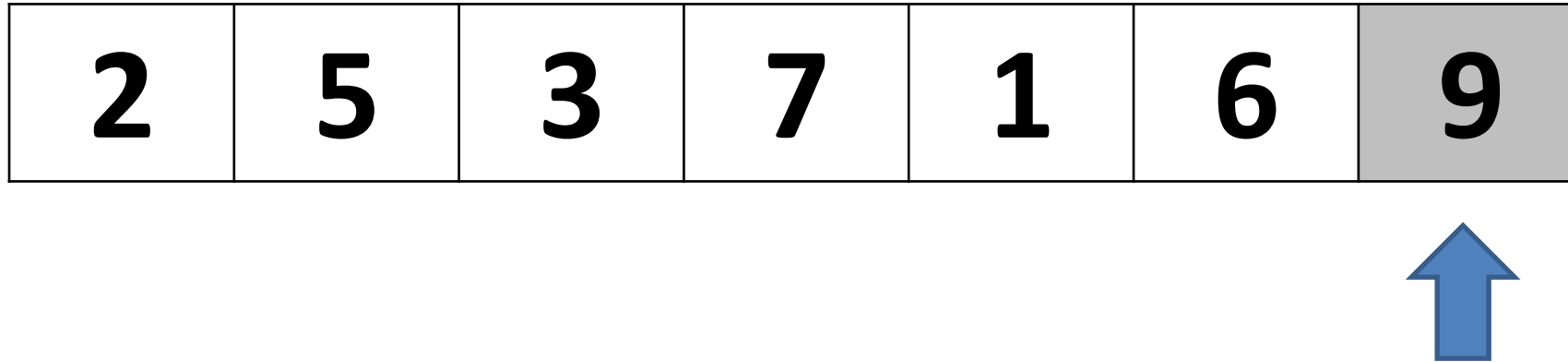
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Bubble Sort → “The biggest bubbles rise to the top naturally”

Bubble Sort

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At this point, 9 (the biggest number) is at the correct spot in the array.

So, we no longer need to check that index!

Now, we start over again, but now we check one less spot!

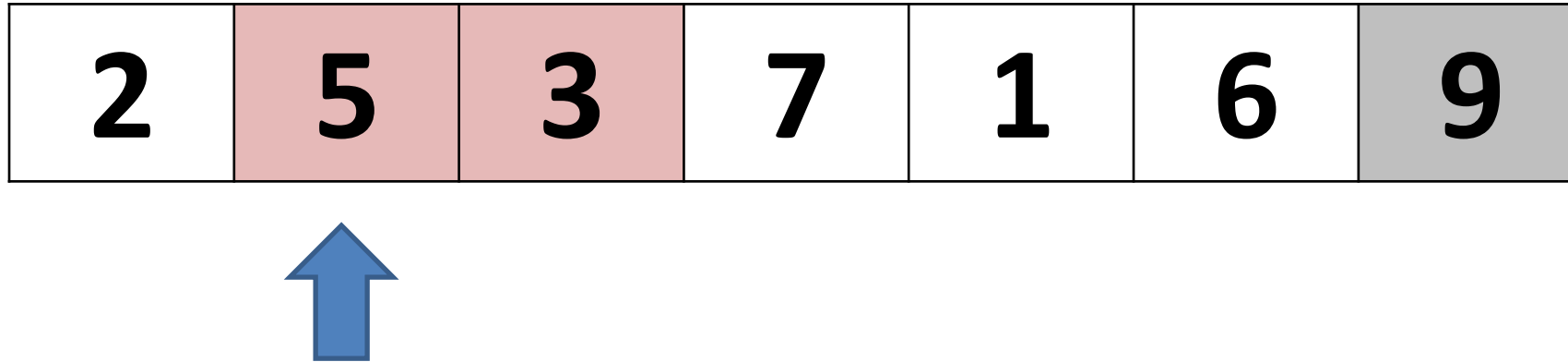
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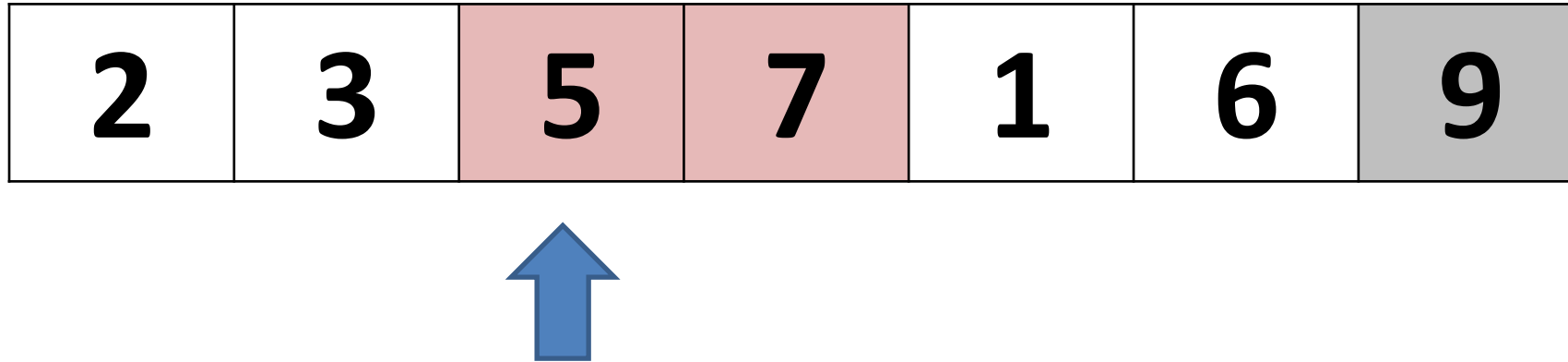
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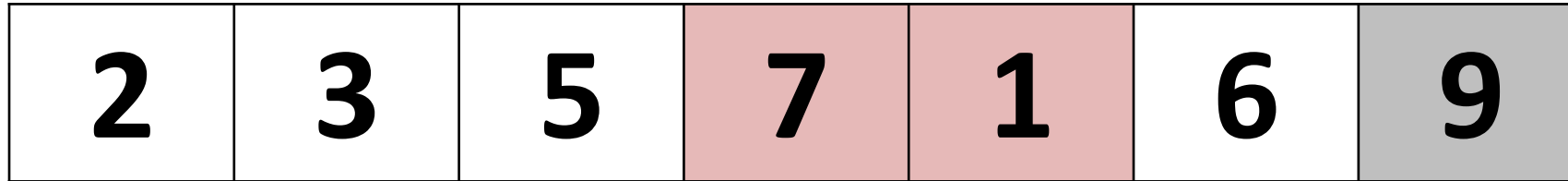
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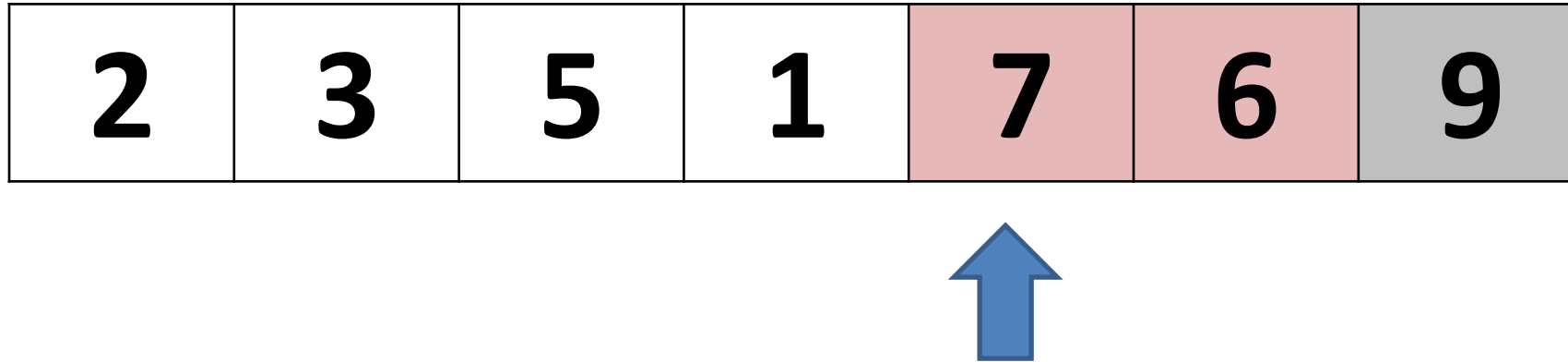
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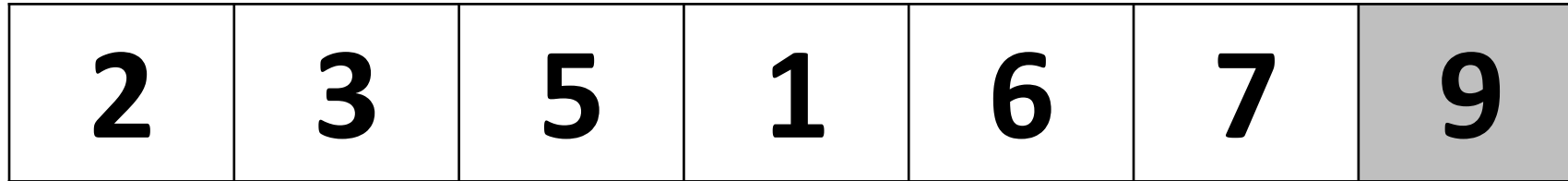
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Bubble Sort

Iterate through an array and compare **pairs** in the array. When comparing two numbers, if one is bigger than the other, **swap**. Keep iterating until array is sorted



7 is now in the correct spot of the array

Bubble Sort

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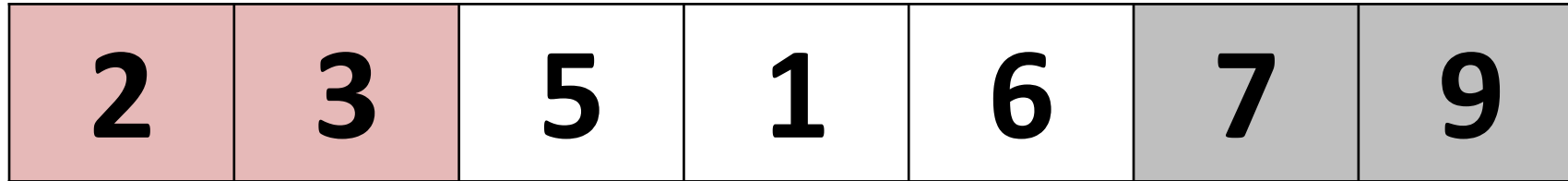
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---	---	---	---	---	---	---



Repeat again!

Bubble Sort

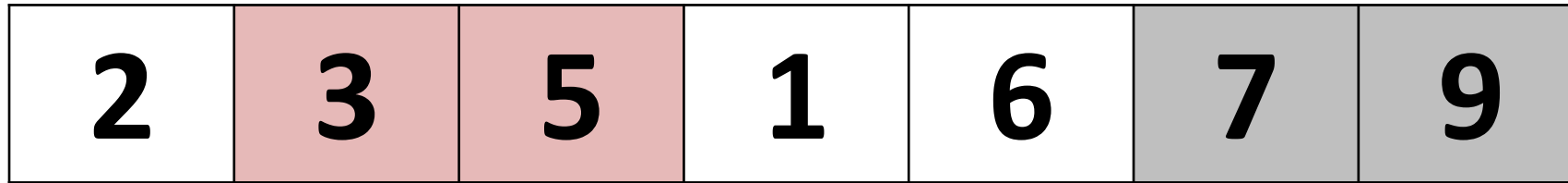
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Bubble Sort

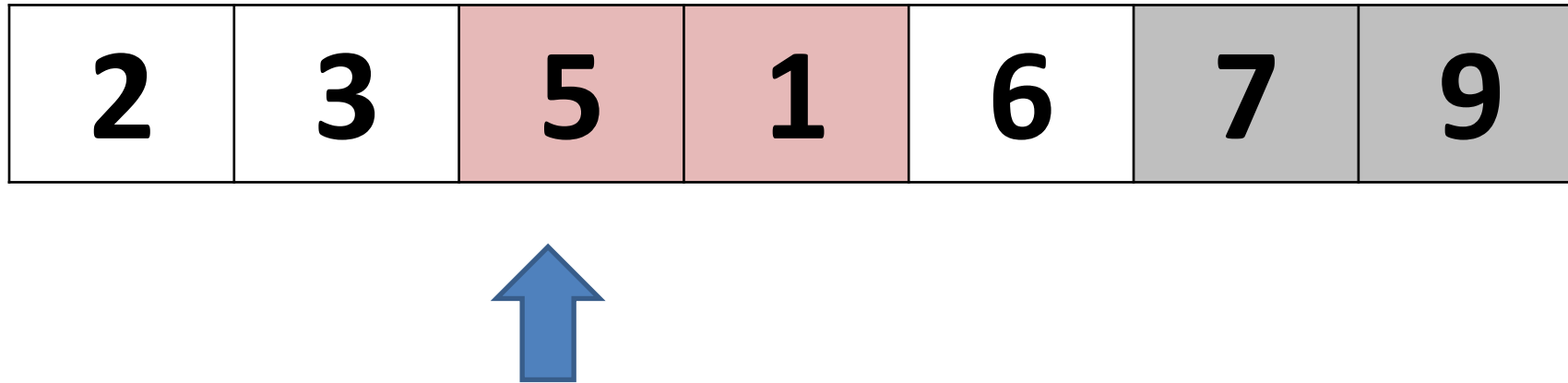
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Repeat again!

Bubble Sort

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Repeat again!

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Repeat again!

Bubble Sort

Iterate through an array and compare **pairs** in the array. When comparing two numbers, if one is bigger than the other, **swap**. Keep iterating until array is sorted

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(fast forwarding....)

Bubble Sort

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All done!

Bubble Sort

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1	2	3	5	6	7	9
---	---	---	---	---	---	---

All done!

Bubble Sort

```
public void bubbleSort(int[] array) {  
    int n = array.length;  
    for(int i = 0; i < n - 1; i++) {  
        for(int j = 0; j < n - i - 1; j++) {  
            if( array[j] > array[j + 1]) {  
                //swap  
                int temp = array[j];  
                array[j] = array[j+1];  
                array[j + 1] = temp;  
            }  
        }  
    }  
}
```


Bubble Sort

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public void bubbleSort(int[] array) {  
    int n = array.length;  
    for(int i = 0; i < n - 1; i++) {  
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                //swap  
                int temp = array[j];  
                array[j] = array[j+1];  
                array[j + 1] = temp;  
            }  
        }  
    }  
}
```

Running time?

Bubble Sort

```
public void bubbleSort(int[] array) {  
    int n = array.length; O(1)  
    for(int i = 0; i < n - 1; i++) { O(n)  
        for(int j = 0; j < n - i - 1; j++) { O(n)  
            if( array[j] > array[j + 1]) { O(1)  
                //swap  
                int temp = array[j]; O(1)  
                array[j] = array[j+1]; O(1)  
                array[j + 1] = temp; O(1)  
            }  
        }  
    }  
}
```

Running time?

Bubble Sort

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public void bubbleSort(int[] array) {  
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                //swap  
                int temp = array[j]; O(1)  
                array[j] = array[j+1]; O(1)  
                array[j + 1] = temp; O(1)  
            }  
        }  
    }  
}
```

Running time? **$O(n^2)$**

$n = | \text{array} |$

For loop in a for loop = $n * n$

Bubble Sort

Bubble Sort Gif

<https://upload.wikimedia.org/wikipedia/commons/c/c8/Bubble-sort-example-300px.gif>

Bubble Sort (Recursion)

Base Case:

If we have one array element left to sort, return

Recursive case:

Do one loop of bubble sort, call the method again and pass the array except for the last element (last element is already in place!)

Bubble Sort (Recursion)

```
public void bubbleSortRecursion(int[] array, int n) {  
    if (n == 1) {  
        return;  
    }  
    for(int i = 0; i < n - 1; i++) {  
        if(array[i] > array[i+1]) {  
            int temp = array[i];  
            array[i] = array[i+1];  
            array[i+1] = temp;  
        }  
    }  
    bubbleSortRecursion(array, n-1);  
}
```

n = size of unsorted section of array

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

7	2	5	3	9	1	6
---	---	---	---	---	---	---



start

Goal: Find the minimum element

`minimum_so_far = 7`

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

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start

Goal: Find the minimum element

`minimum_so_far = 2`

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

7	2	5	3	9	1	6
---	---	---	---	---	---	---



start

Goal: Find the minimum element

`minimum_so_far = 2`

Selection Sort

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Goal: Find the minimum element

`minimum_so_far = 2`

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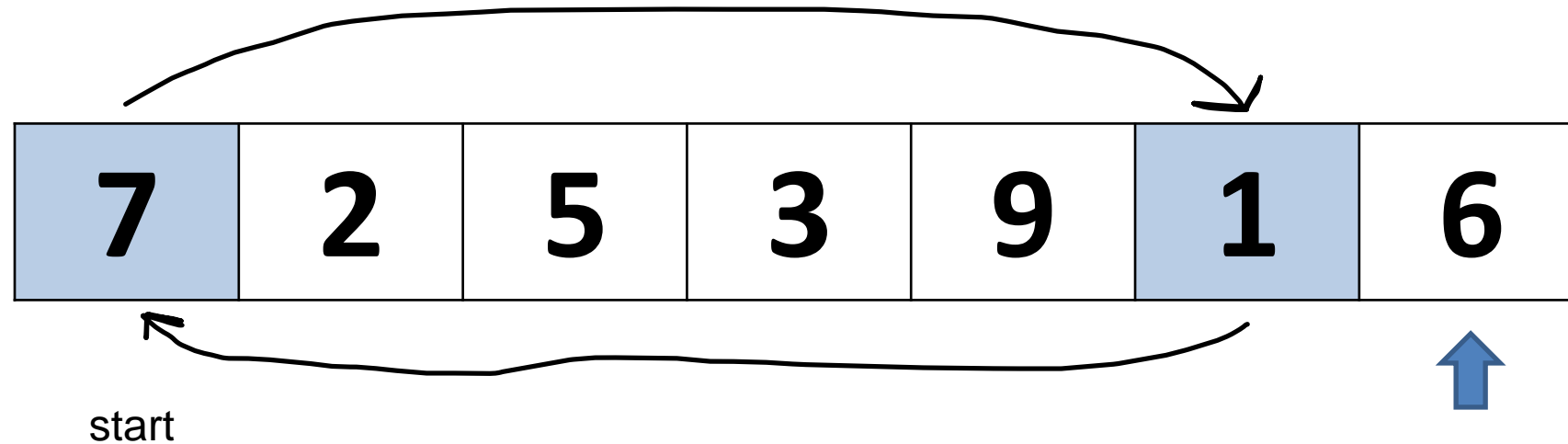
start

Goal: Find the minimum element

`minimum_so_far = 1`

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



Goal: Find the minimum element

`minimum_so_far = 1`

Now that we've found the minimum value, swap it with the spot that we started at

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

1	2	5	3	9	7	6
---	---	---	---	---	---	---



start

Goal: Find the minimum element

`minimum_so_far = 2`

1 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

1	2	5	3	9	7	6
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start

Goal: Find the minimum element

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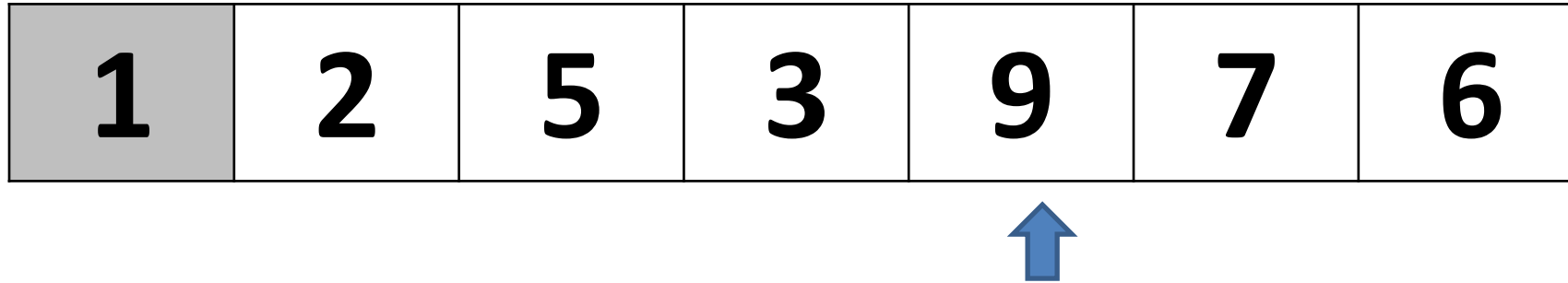
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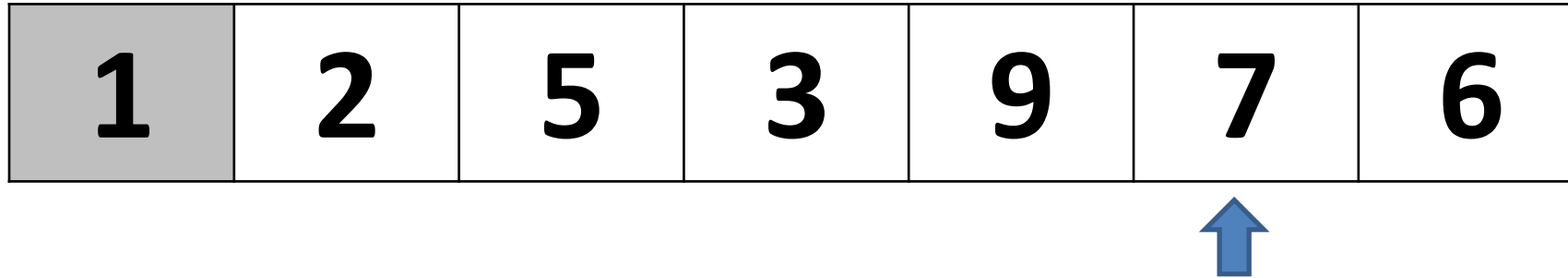
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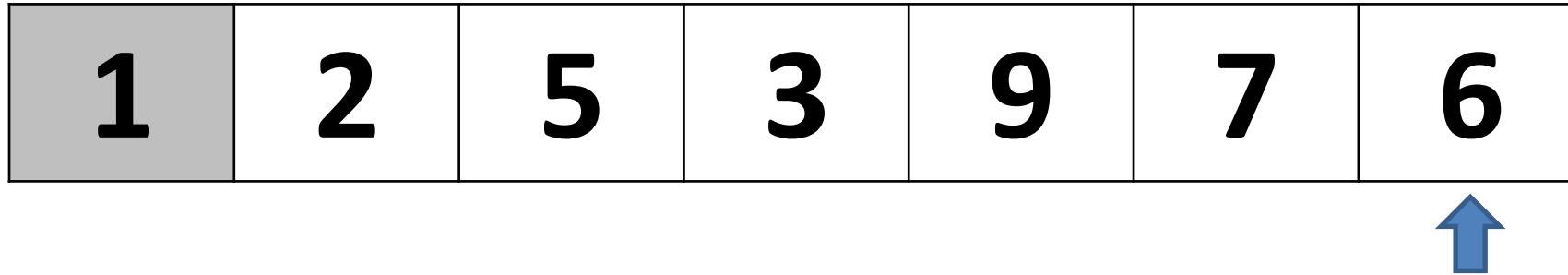
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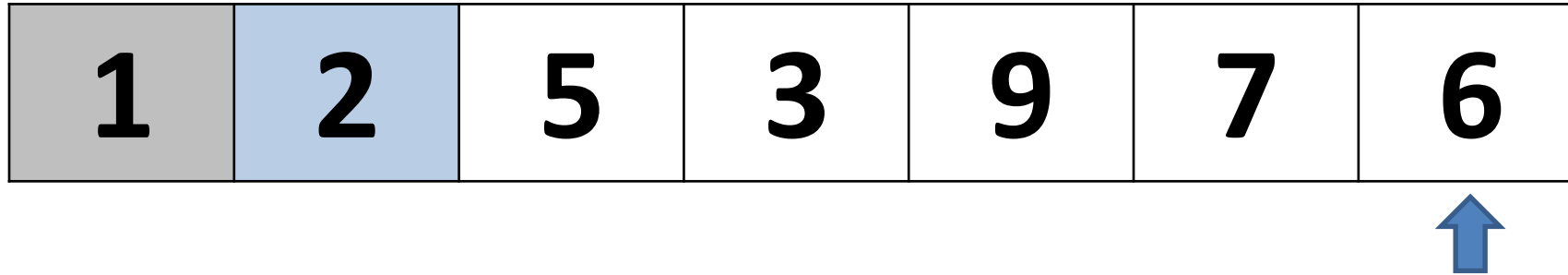
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`minimum_so_far = 2`

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Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



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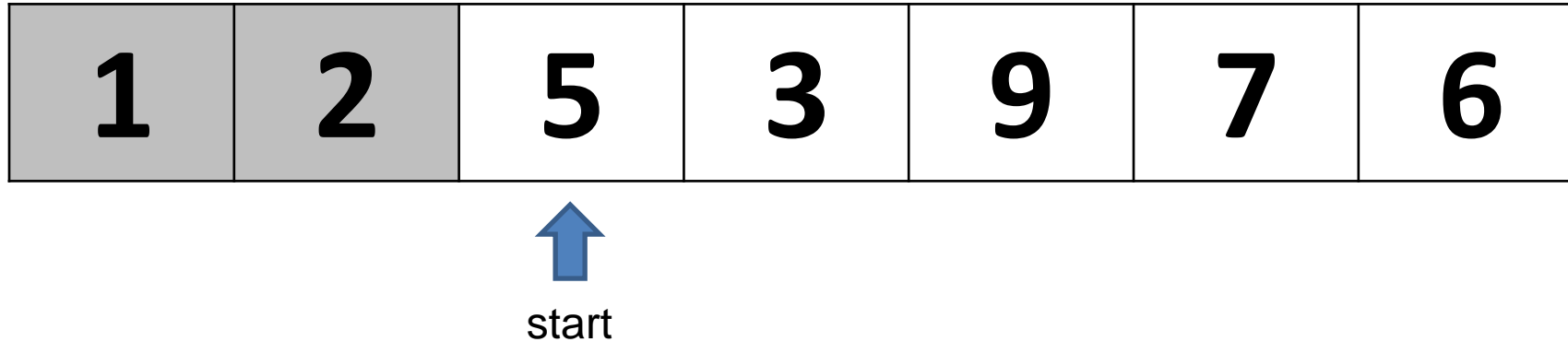
Goal: Find the minimum element

`minimum_so_far = 2`

1 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



Goal: Find the minimum element

`minimum_so_far = 5`

2 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

1	2	5	3	9	7	6
---	---	---	---	---	---	---



start

Goal: Find the minimum element

`minimum_so_far = 5`

2 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

1	2	5	3	9	7	6
---	---	---	---	---	---	---



start

Goal: Find the minimum element

`minimum_so_far = 3`

2 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

1	2	5	3	9	7	6
---	---	---	---	---	---	---



start

Goal: Find the minimum element

`minimum_so_far = 3`

2 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot

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start

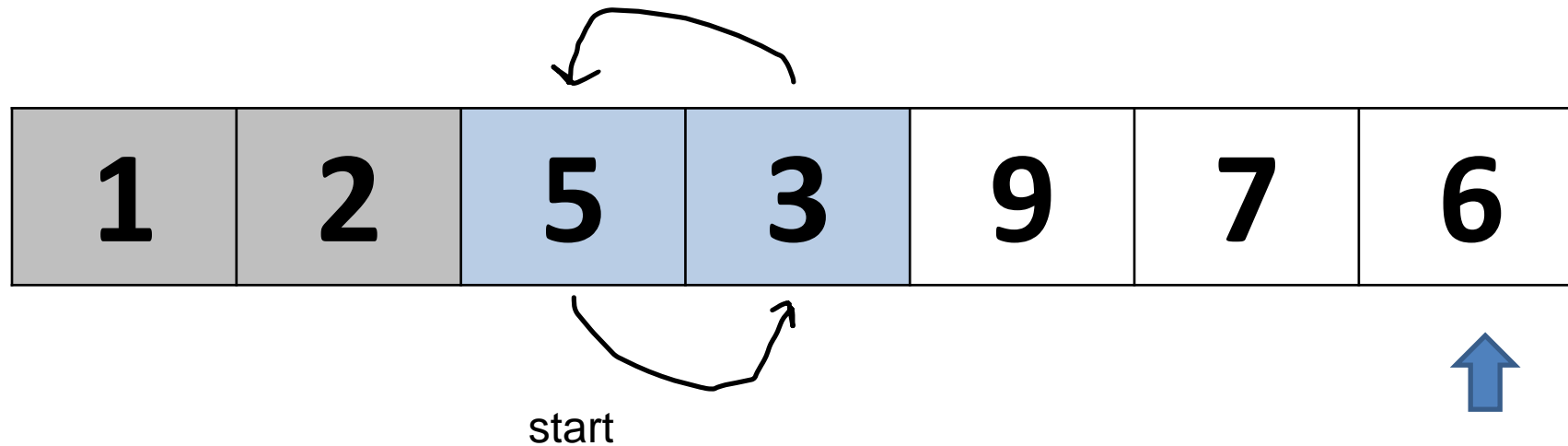
Goal: Find the minimum element

`minimum_so_far = 3`

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Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



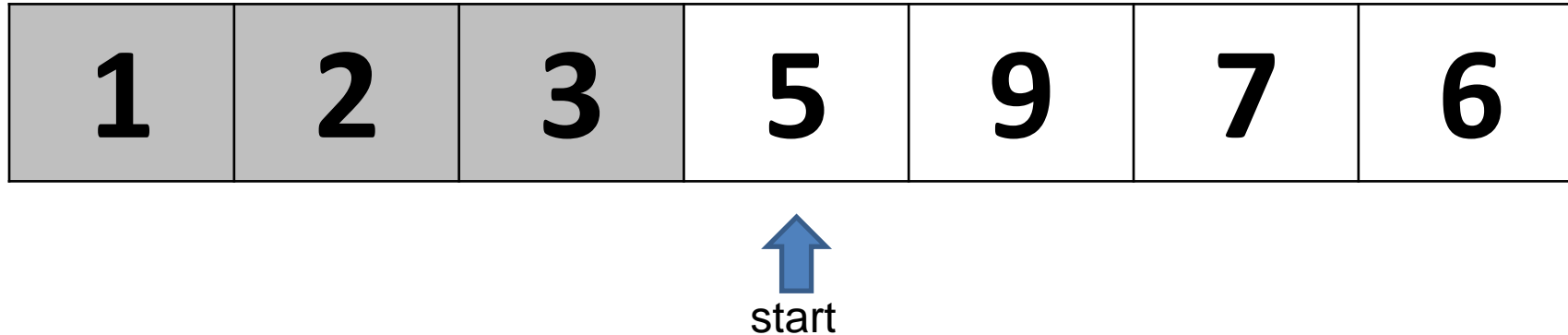
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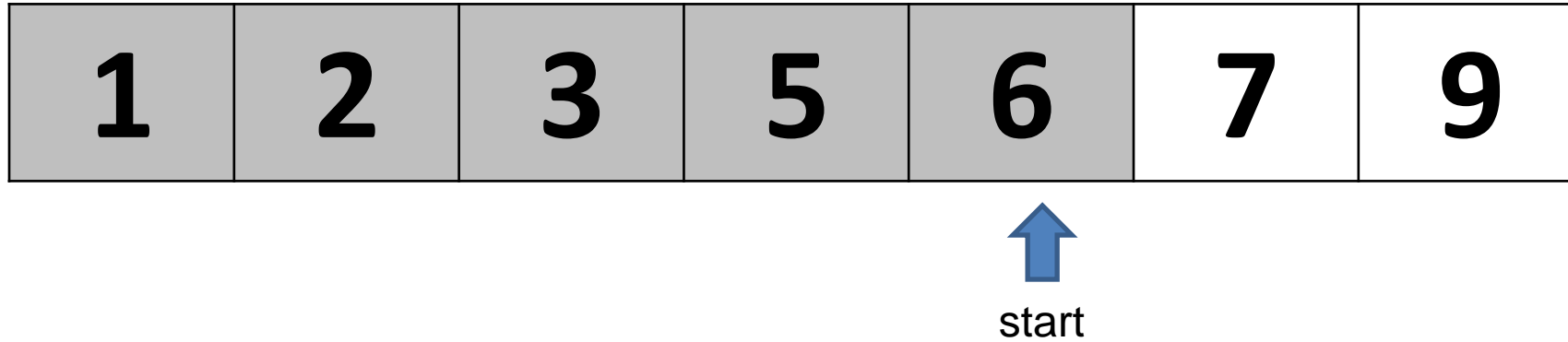
Goal: Find the minimum element

`minimum_so_far = 3`

2 is at the correct spot in the array now, so now we find the next lowest number

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



↑
start

Selection Sort

Iterate through the array N times, and during each iteration, **find the minimum element** and place it in the correct spot



start

Selection Sort

Selection Sort Gif

<https://upload.wikimedia.org/wikipedia/commons/9/94/Selection-Sort-Animation.gif>