

CSCI 132:

Basic Data Structures and Algorithms

Queues (Array implementation)

Reese Pearsall & Iliana Castillon
Fall 2024

Announcements

Lab 8 due **tomorrow** at 11:59pm

No lecture on Friday → Program 3 workday

Program 3 due next Friday (Nov. 1st)

my brain on a sunday at 3am



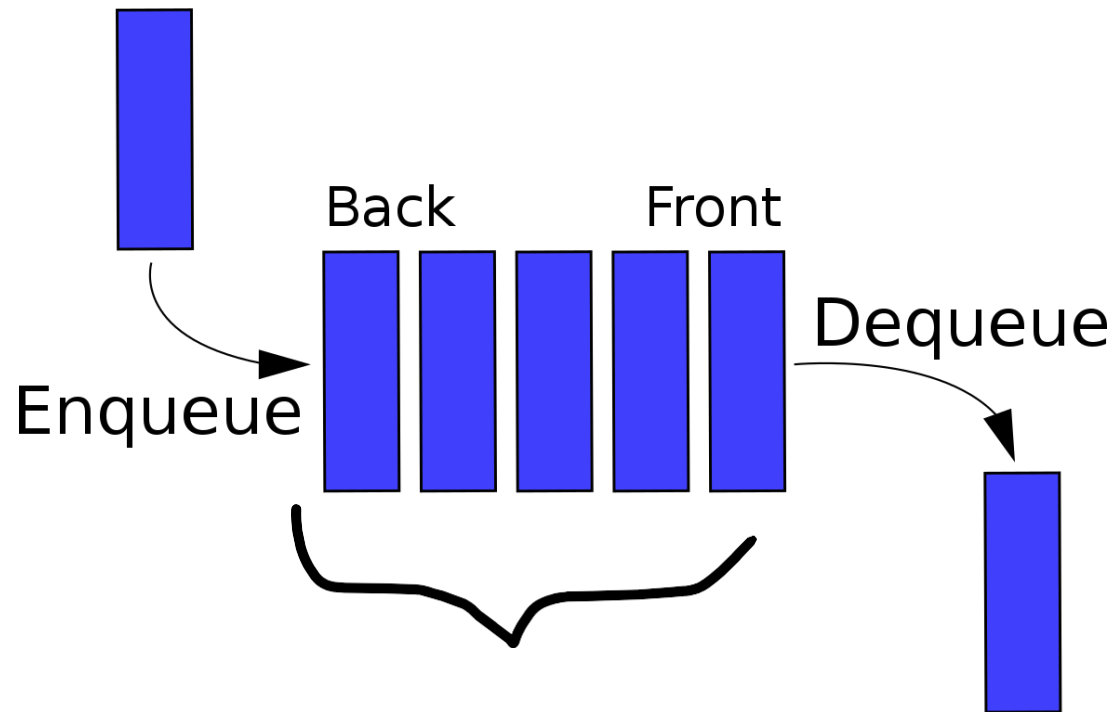
I just reduced this
call from $O(n^2)$ to $O(1)$

my brain on
a wednesday 2pm



help me, what
is an interface

A Queue is a data structure that holds data, but operates in a **First-in First-out (FIFO)** fashion

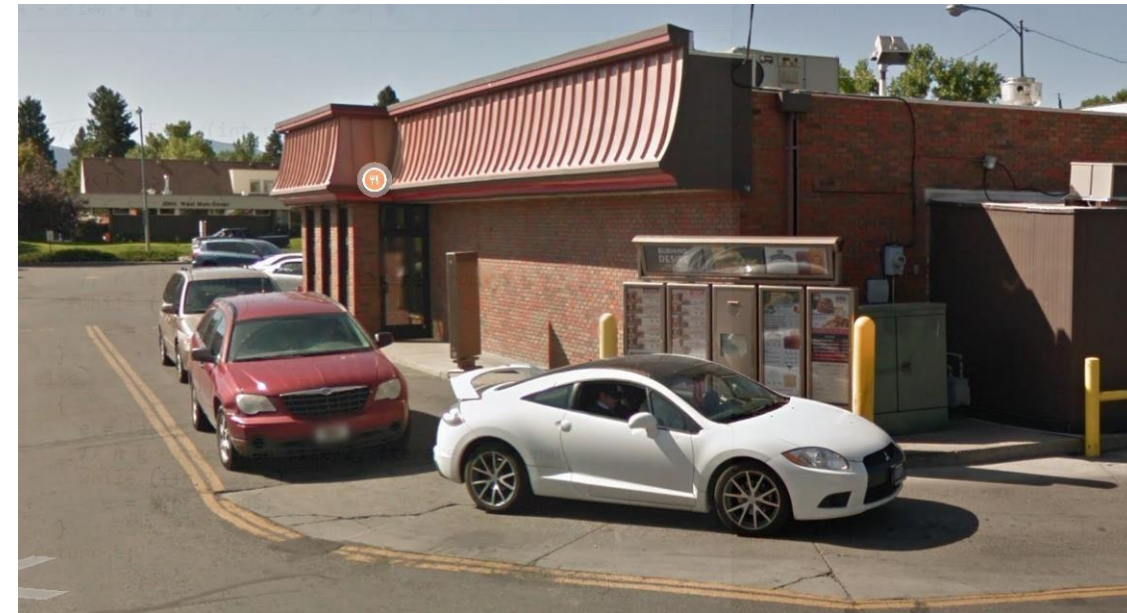


Once again, we need a data structure to hold the data of the queue

- Linked List
- Array

Elements get added to the **Back** of the Queue.

Elements get removed from the **Front** of the queue



A Queue is a data structure that holds data, but operates in a First-in First-out (FIFO) fashion

The Queue ADT has the following methods:

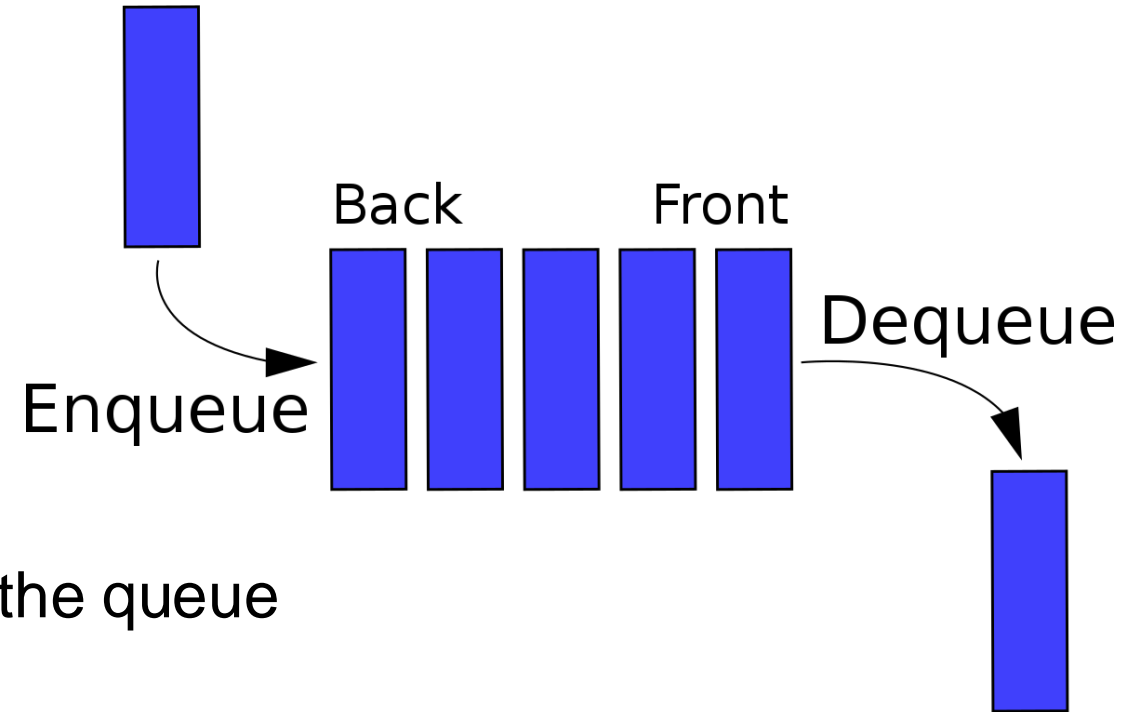
Enqueue- Add new element to the queue

Dequeue- Remove element from the queue

**** Always remove the front-most element**

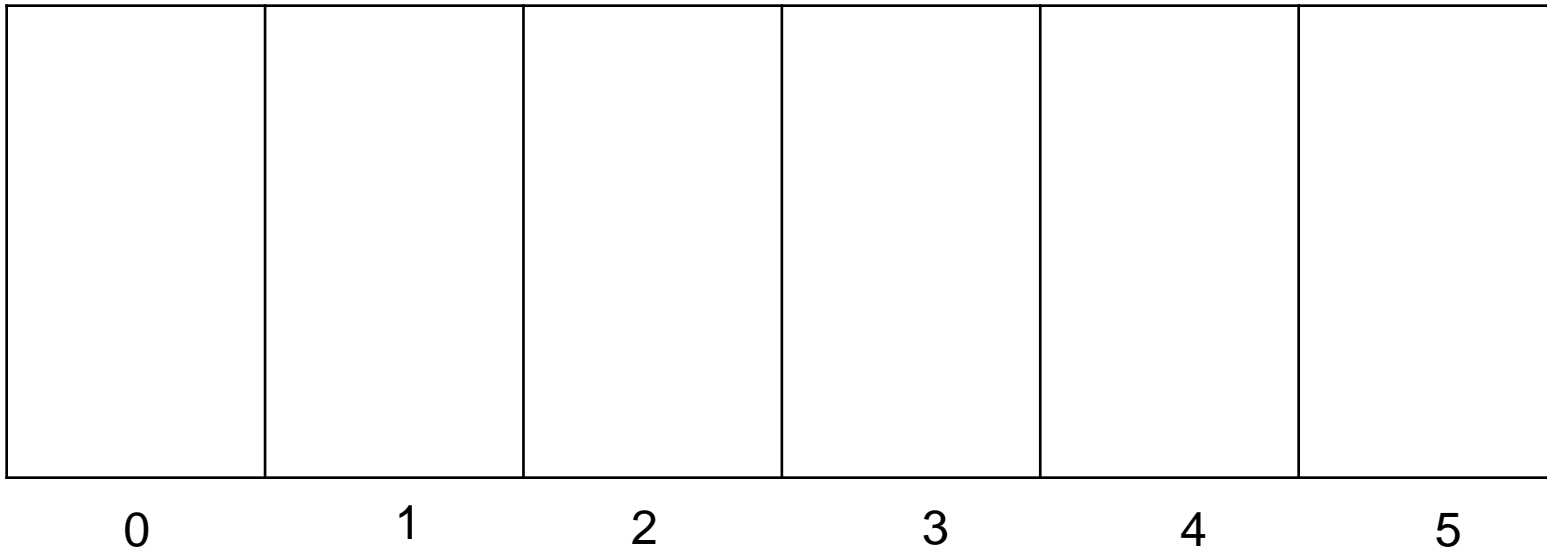
Peek()- Return the element that is at the front of the queue

IsEmpty()- Returns true if queue is empty, returns false if queue is not empty



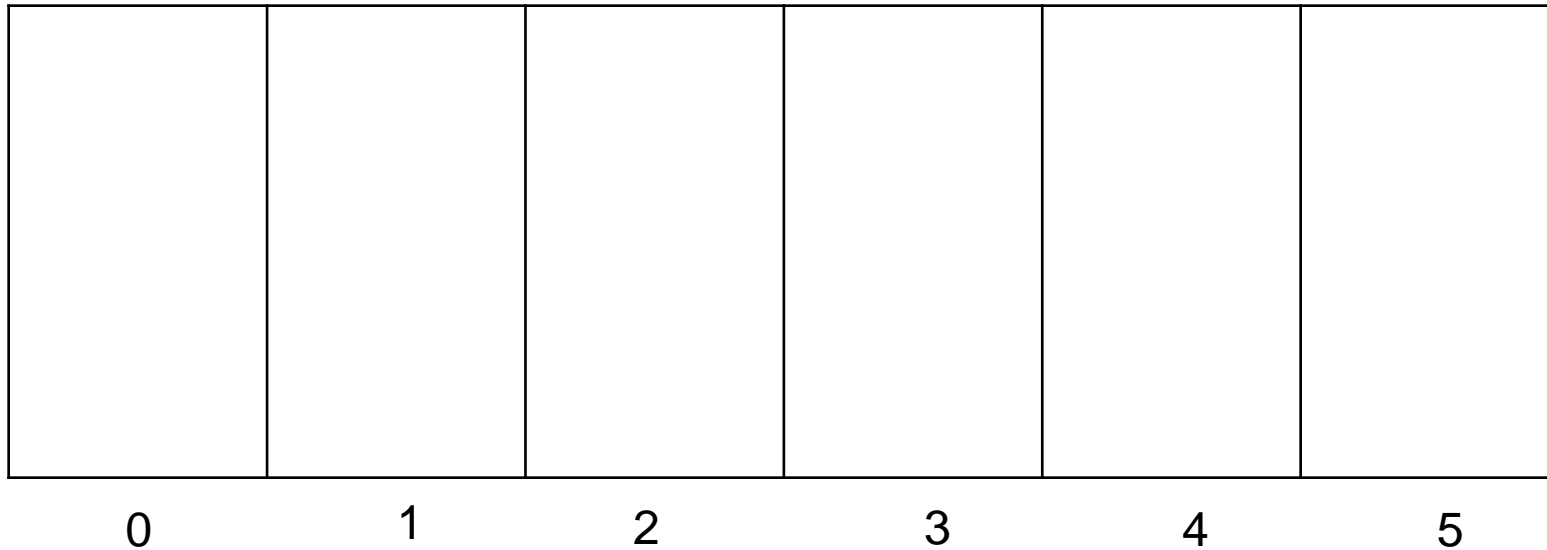
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Suppose that we have a queue that can hold 6 elements



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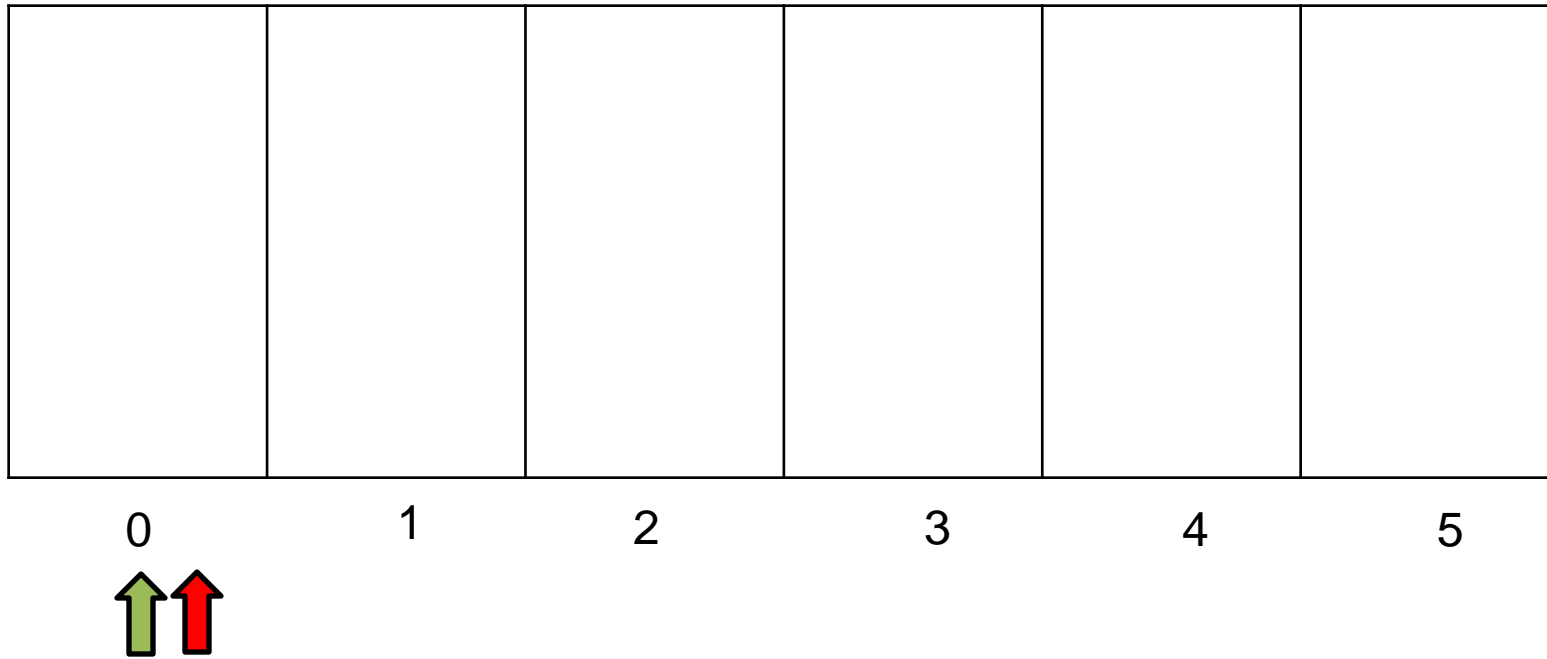


We need to keep track of a few things:

1. The index of the **front** of the queue
2. The index of the rear of the queue
3. The size of the queue
4. The capacity of the queue

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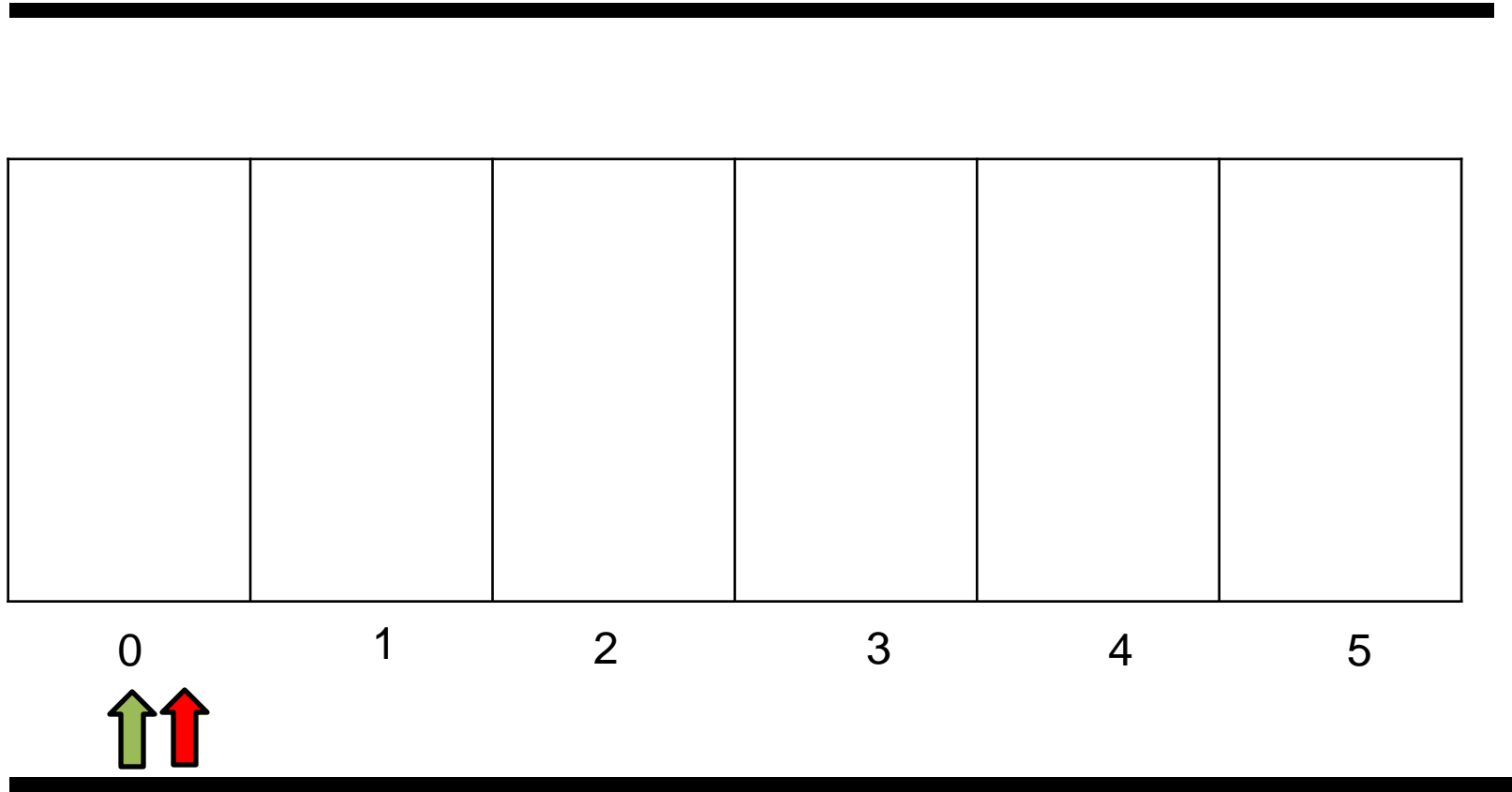
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1. The index of the **front** of the queue
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capacity = 6 front = 0
size = 0 rear = 0

Today, we will be implementing a Queue with an Array.

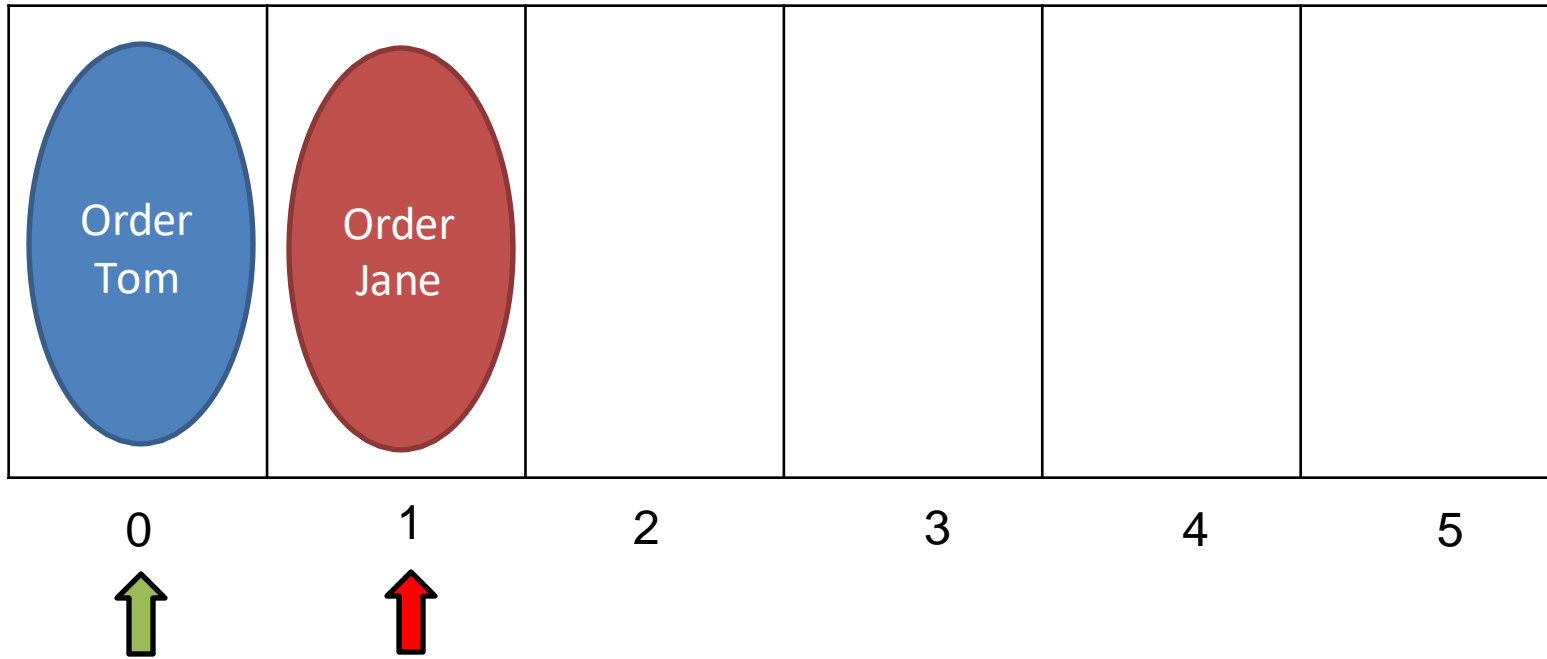
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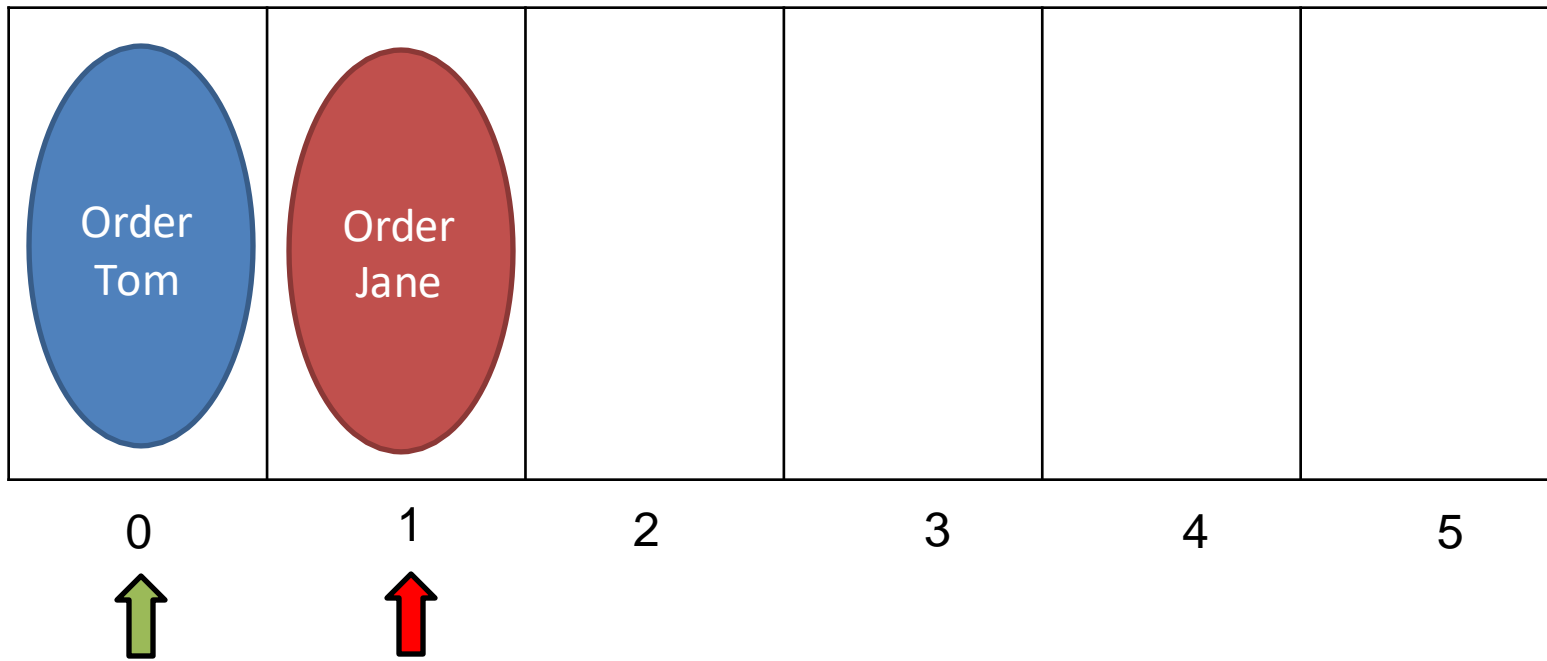
Suppose that we have a queue that can hold 6 elements



capacity = 6 front = 0
size = 2 rear = 1

Today, we will be implementing a Queue with an Array.

Suppose that we have a queue that can hold 6 elements

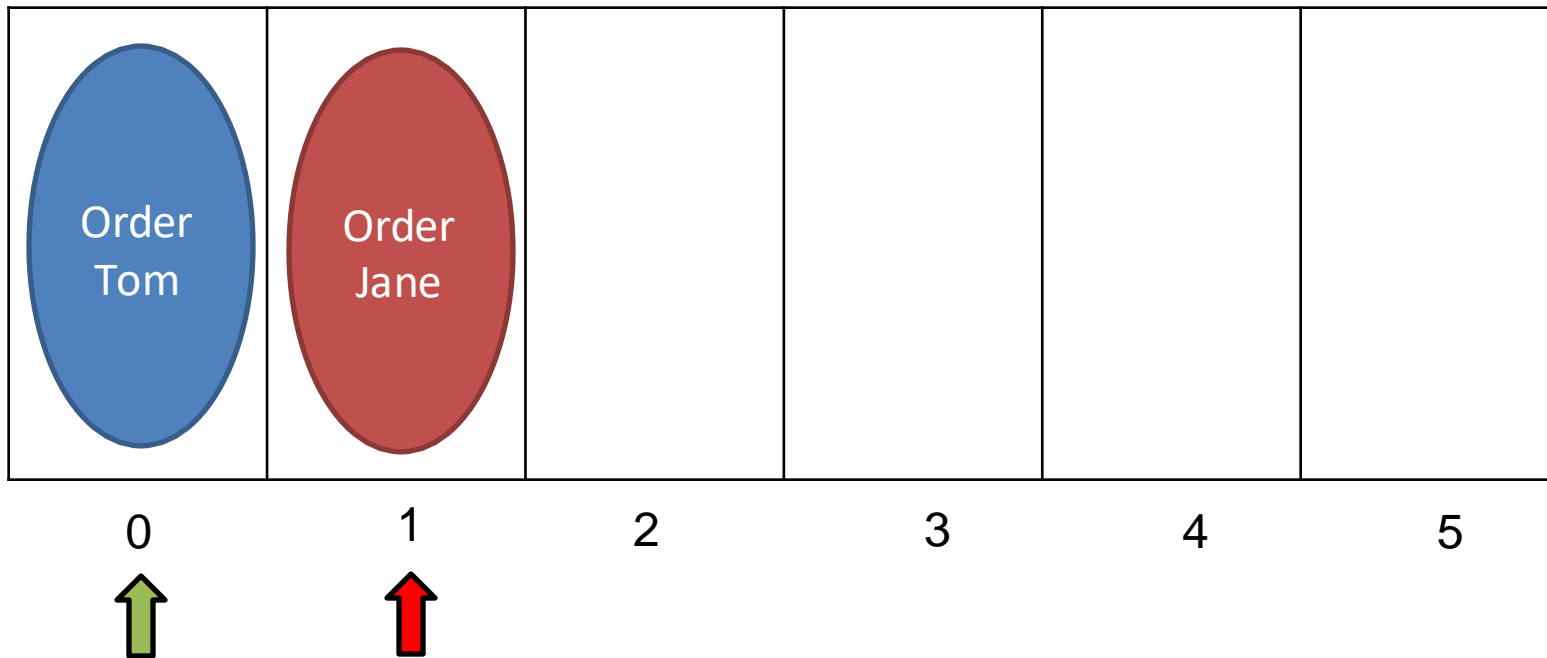


Enqueue?

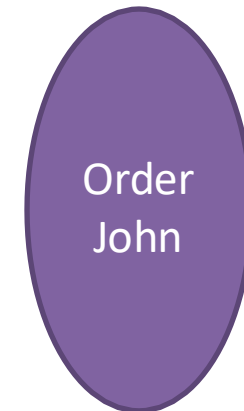
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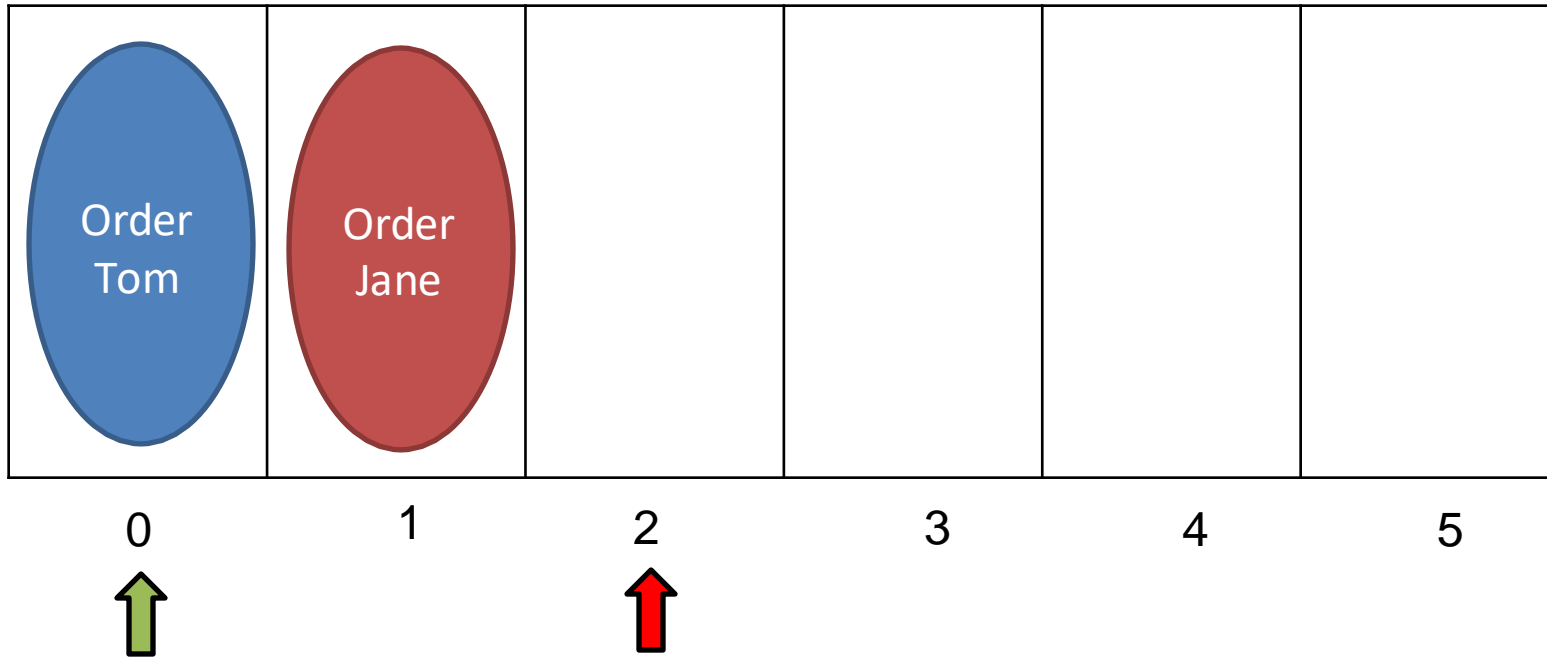
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    if (size == capacity) {  
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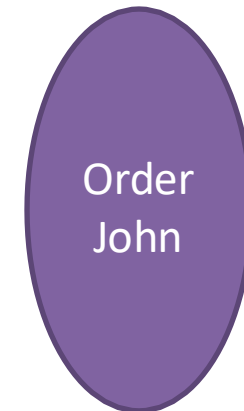
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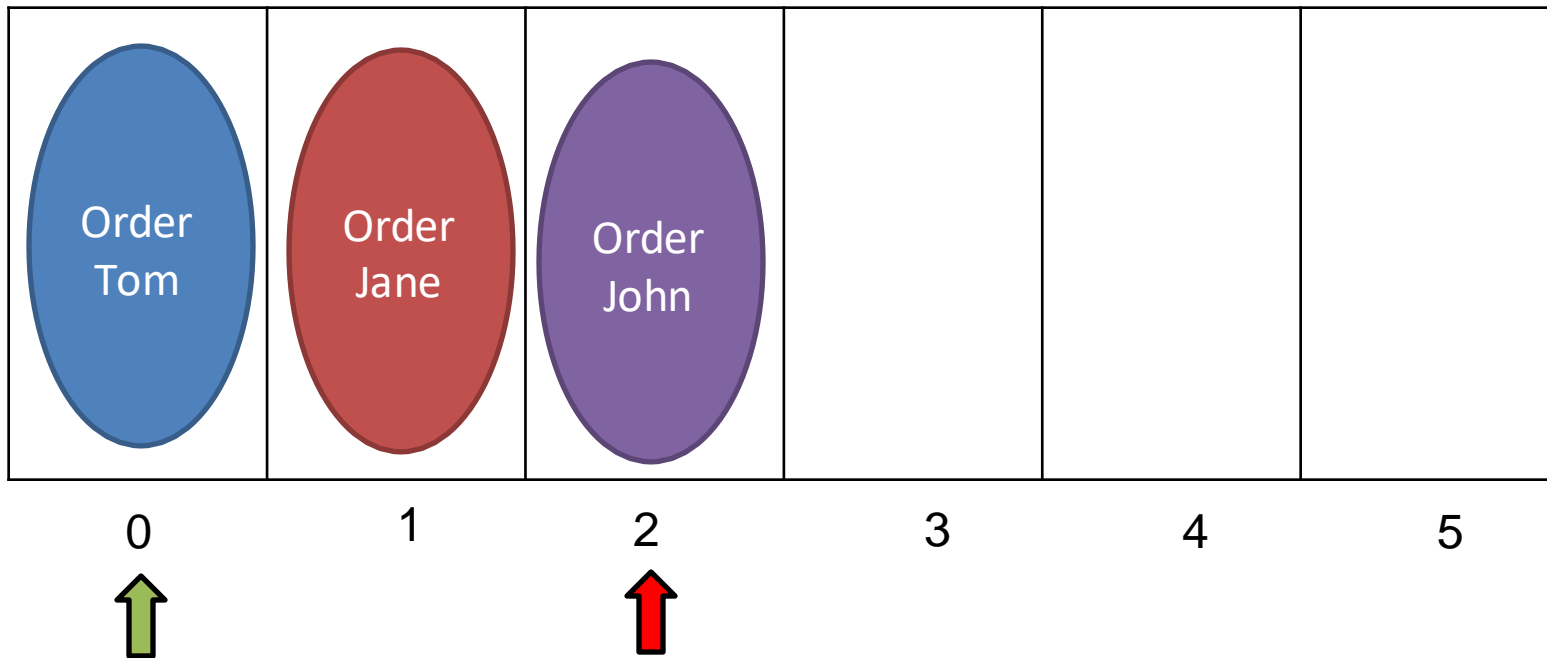
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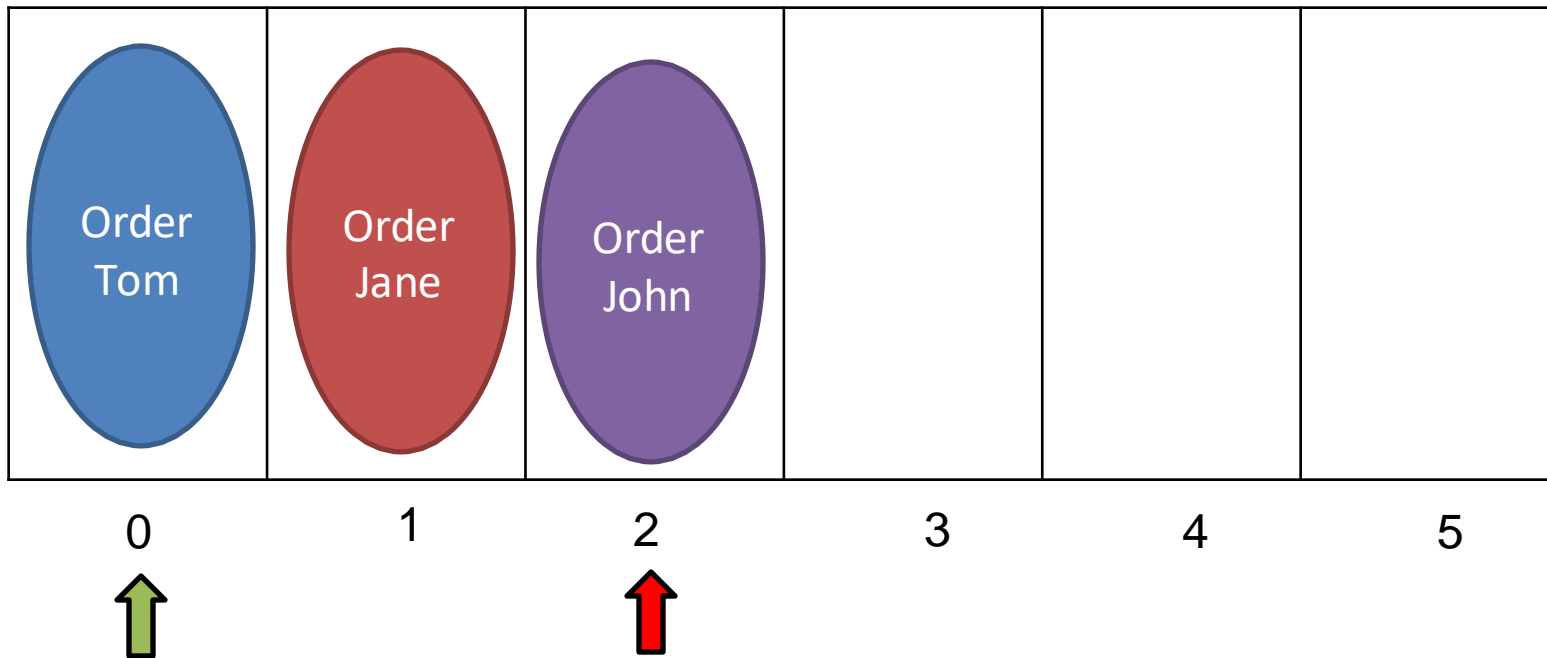


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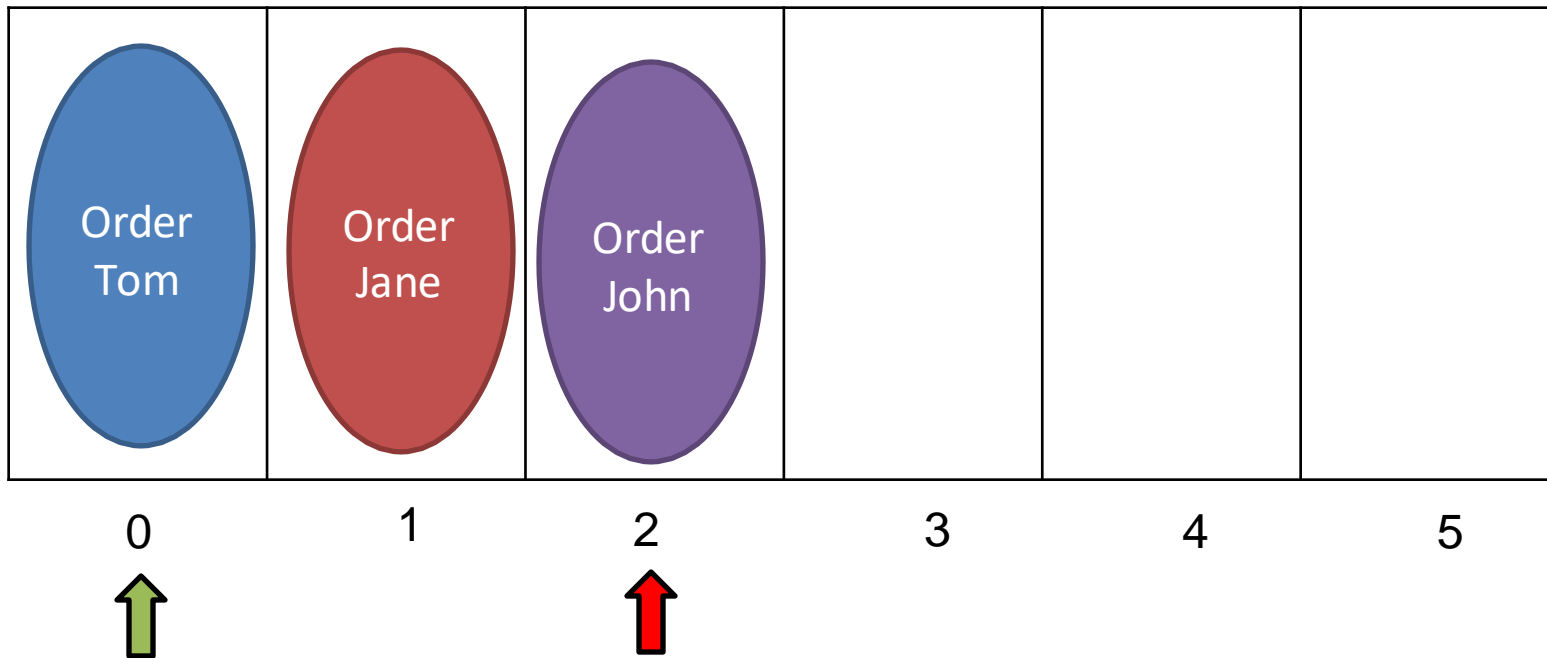


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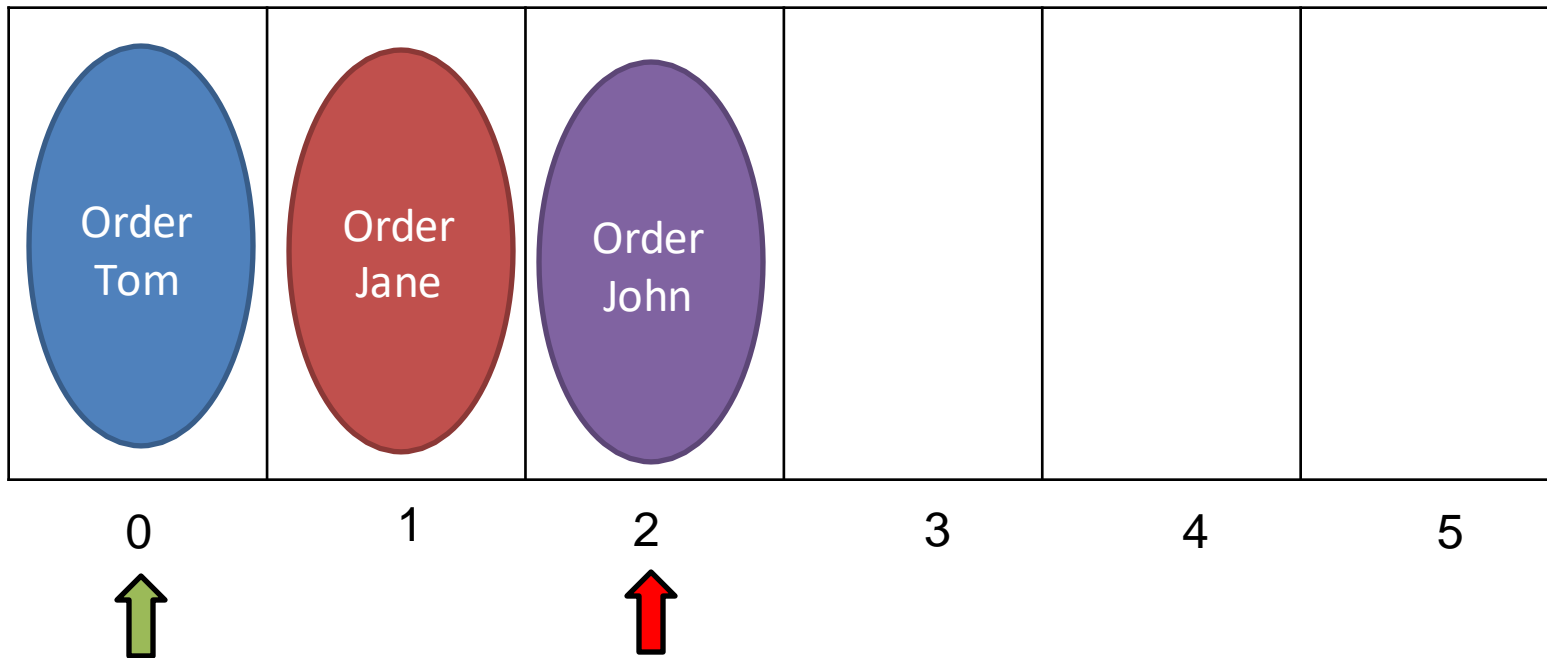


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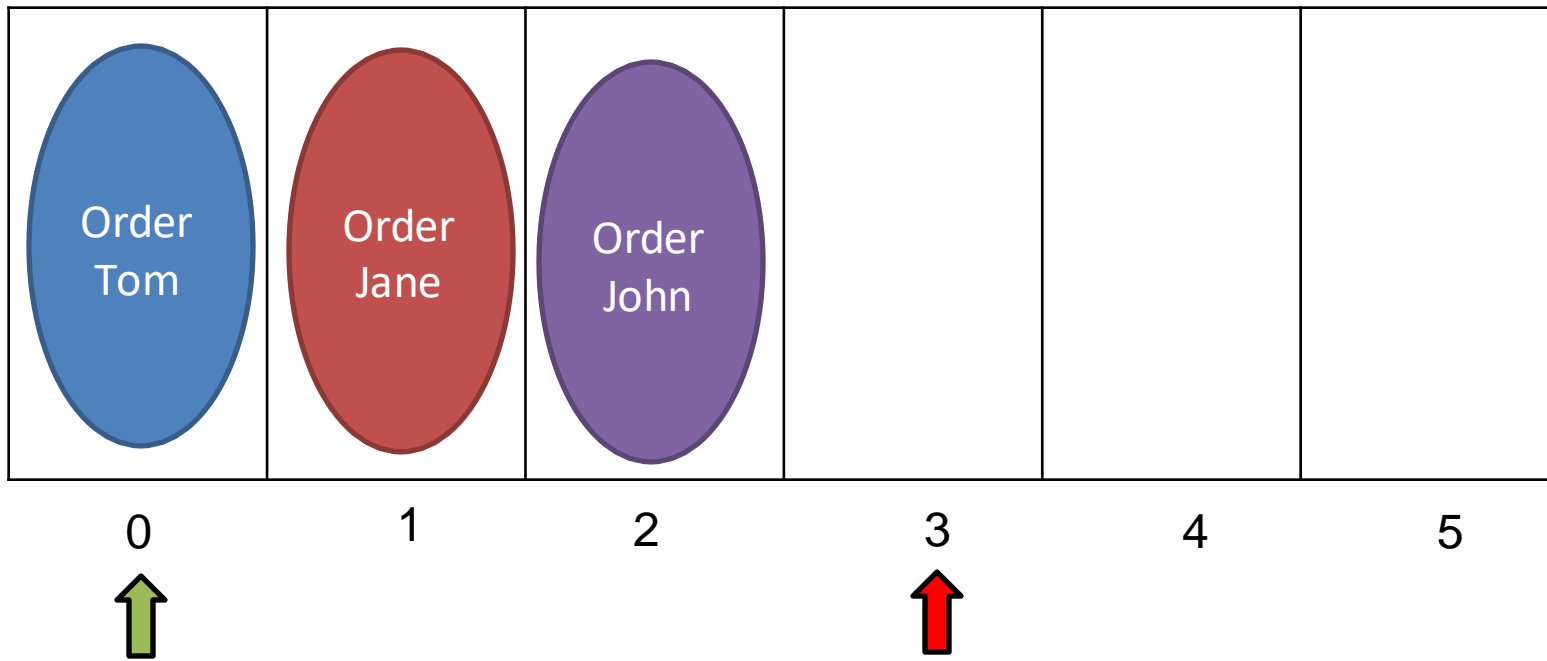
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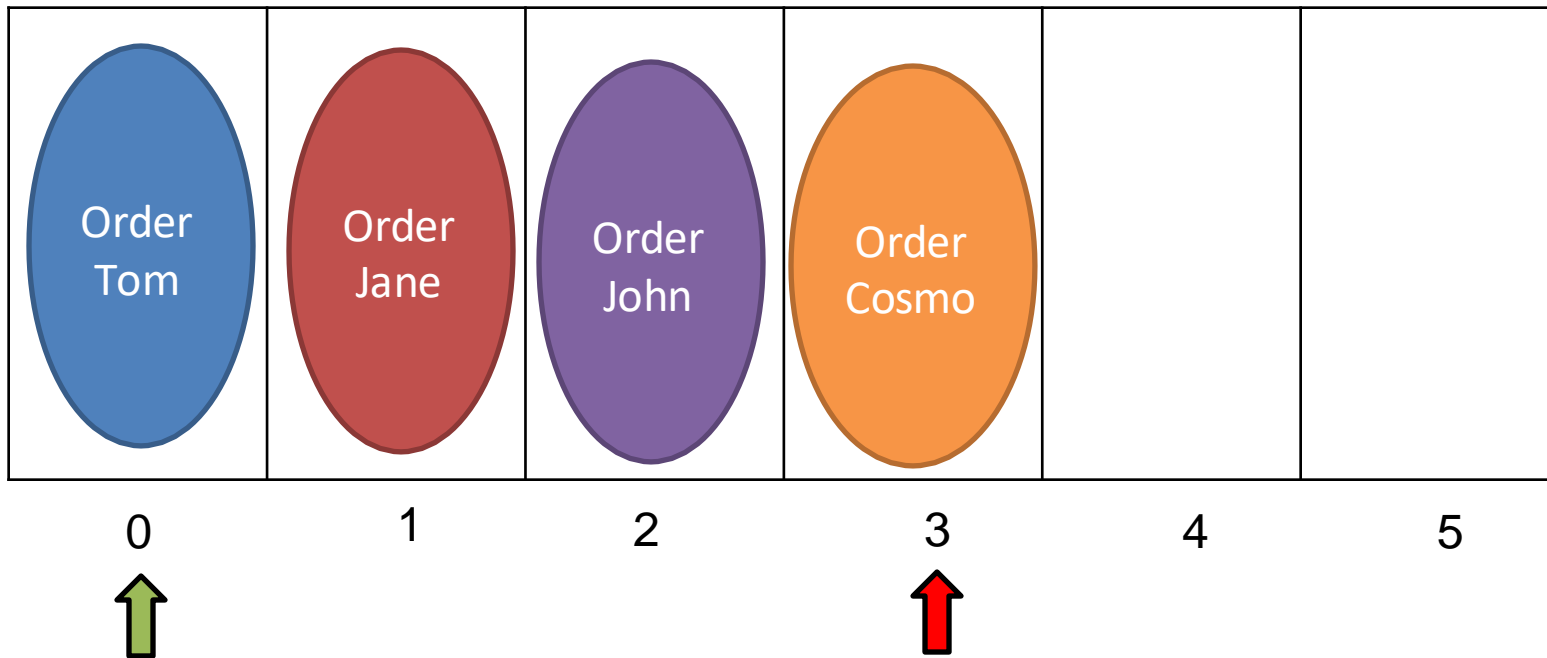
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capacity = 6 front = 0
size = 3 rear = 3

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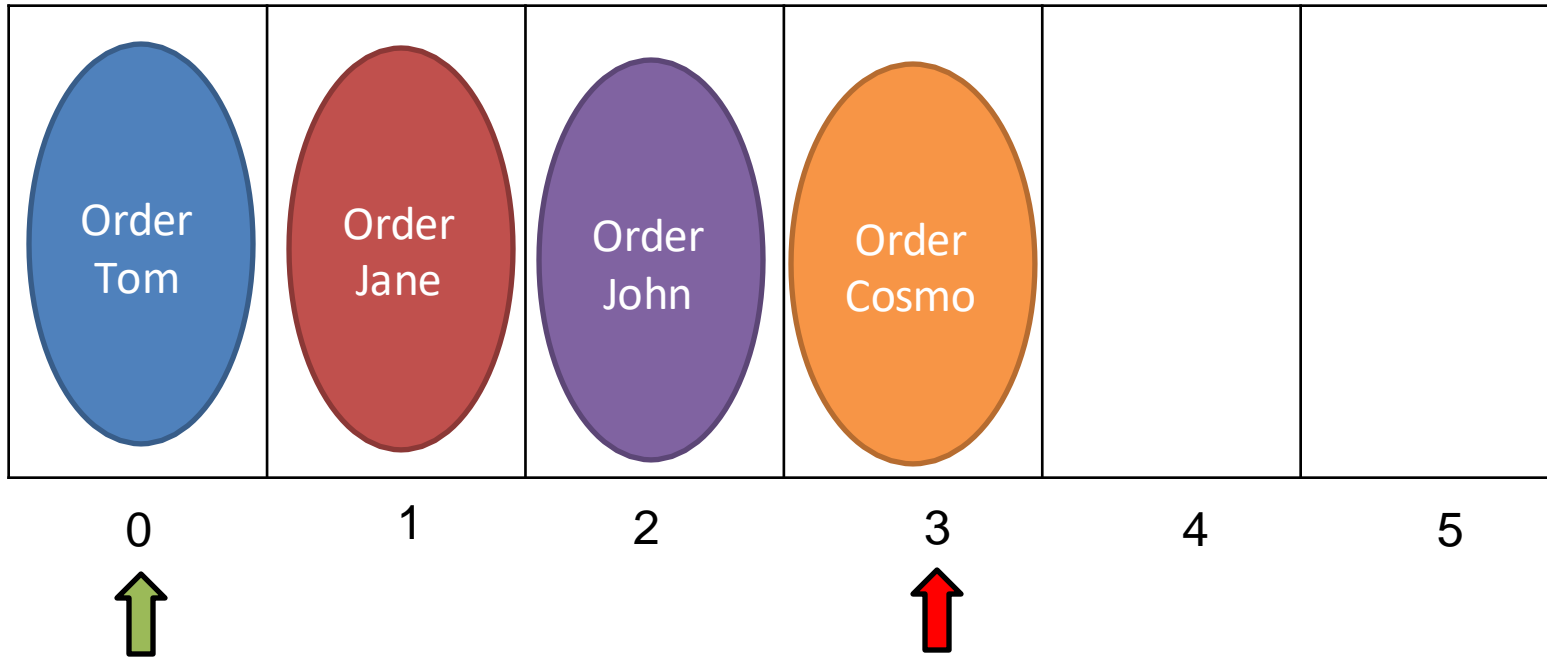


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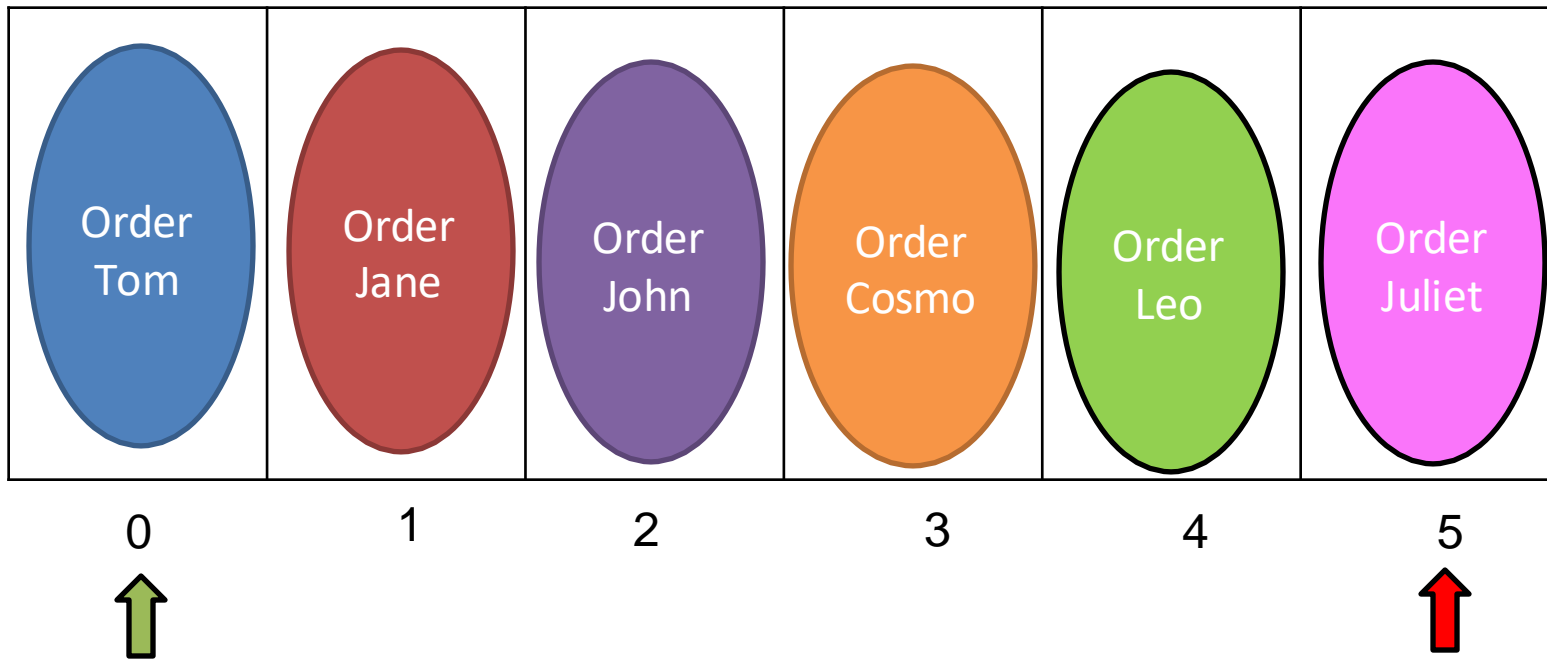


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capacity = 6 front = 0
size = 4 rear = 3

Today, we will be implementing a Queue with an Array.

Suppose that we have a queue that can hold 6 elements

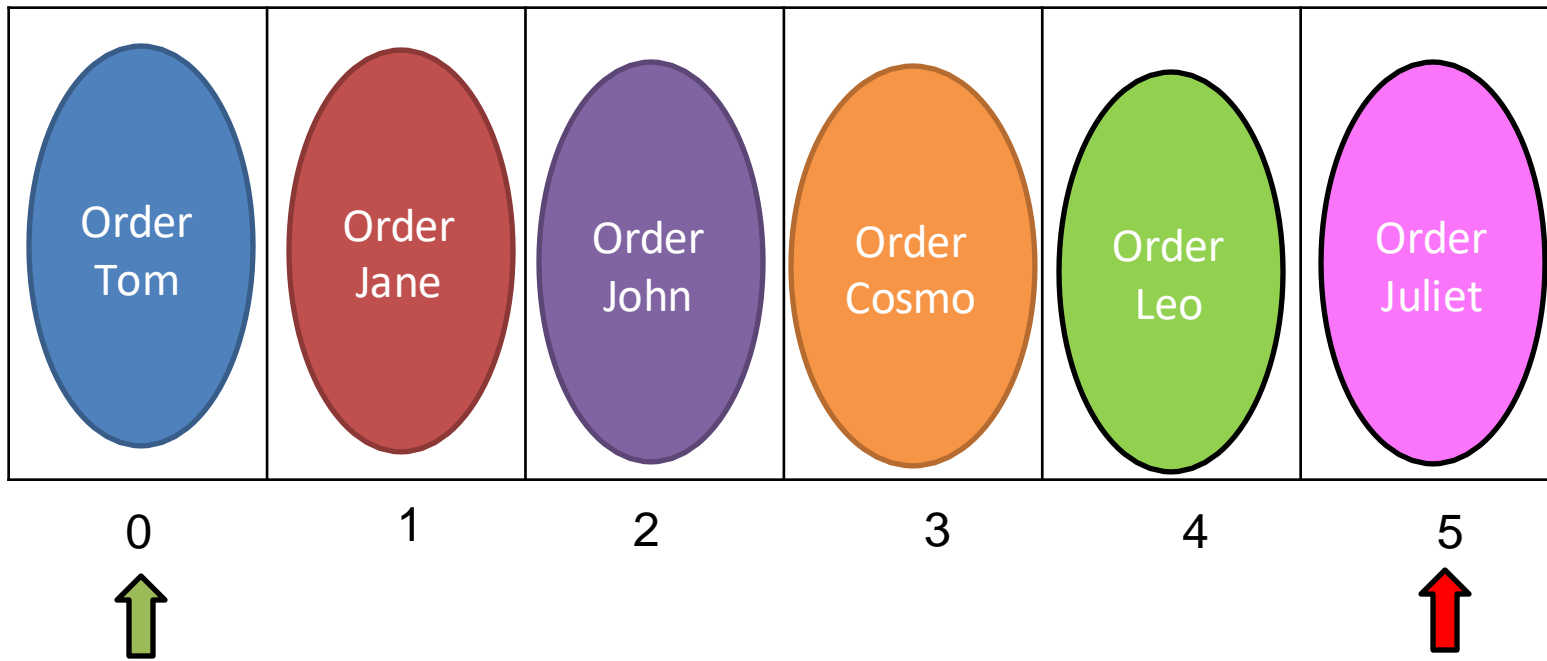


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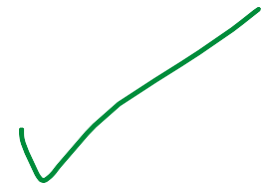
capacity = 6 front = 0
size = 6 rear = 5

Today, we will be implementing a Queue with an Array.

Suppose that we have a queue that can hold 6 elements



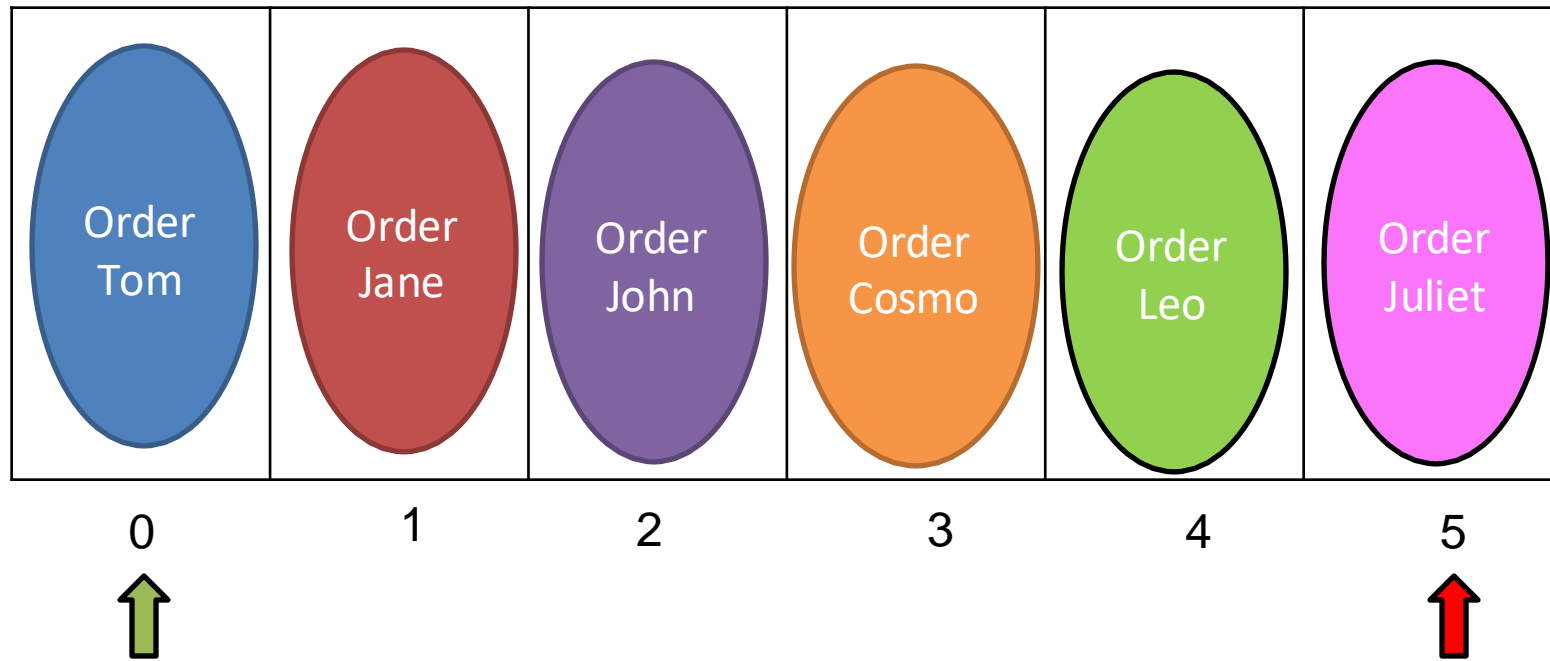
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    if (size == capacity) {  
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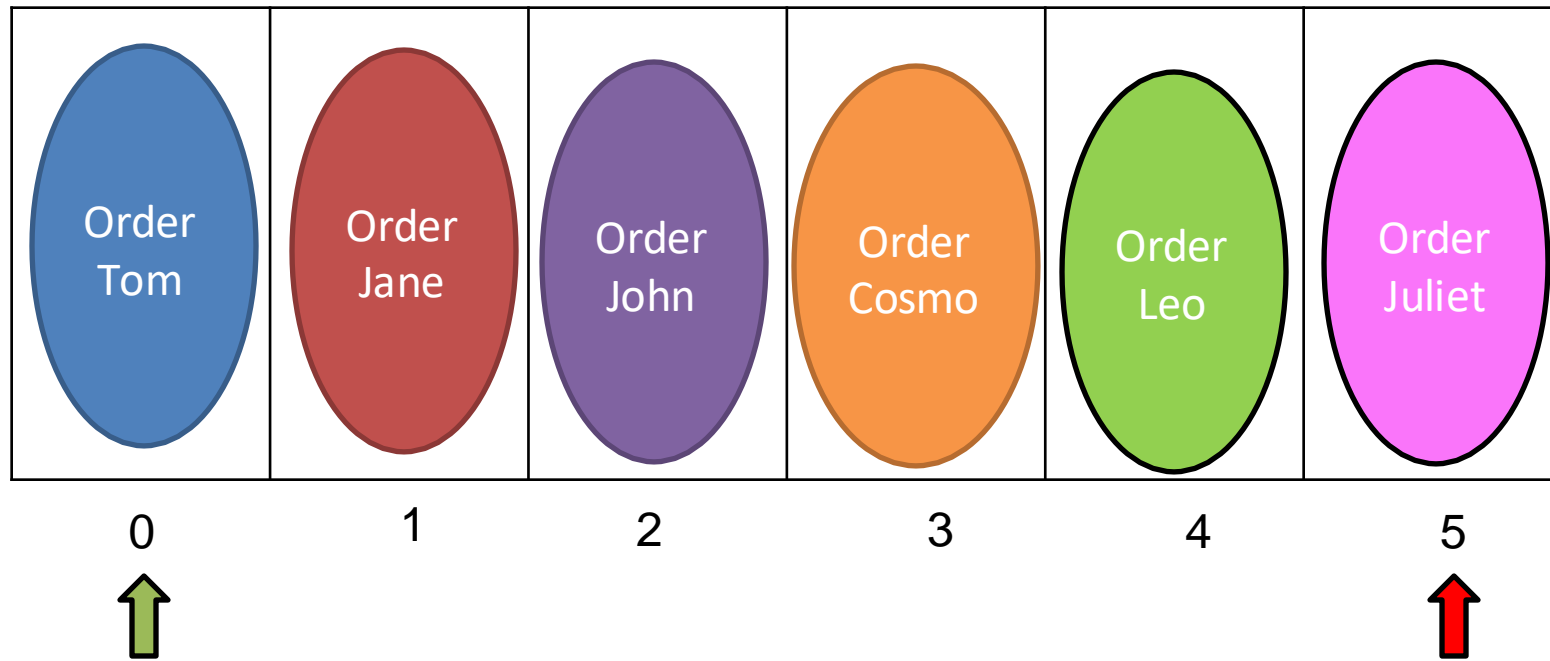


Dequeue?

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size = 6 rear = 5

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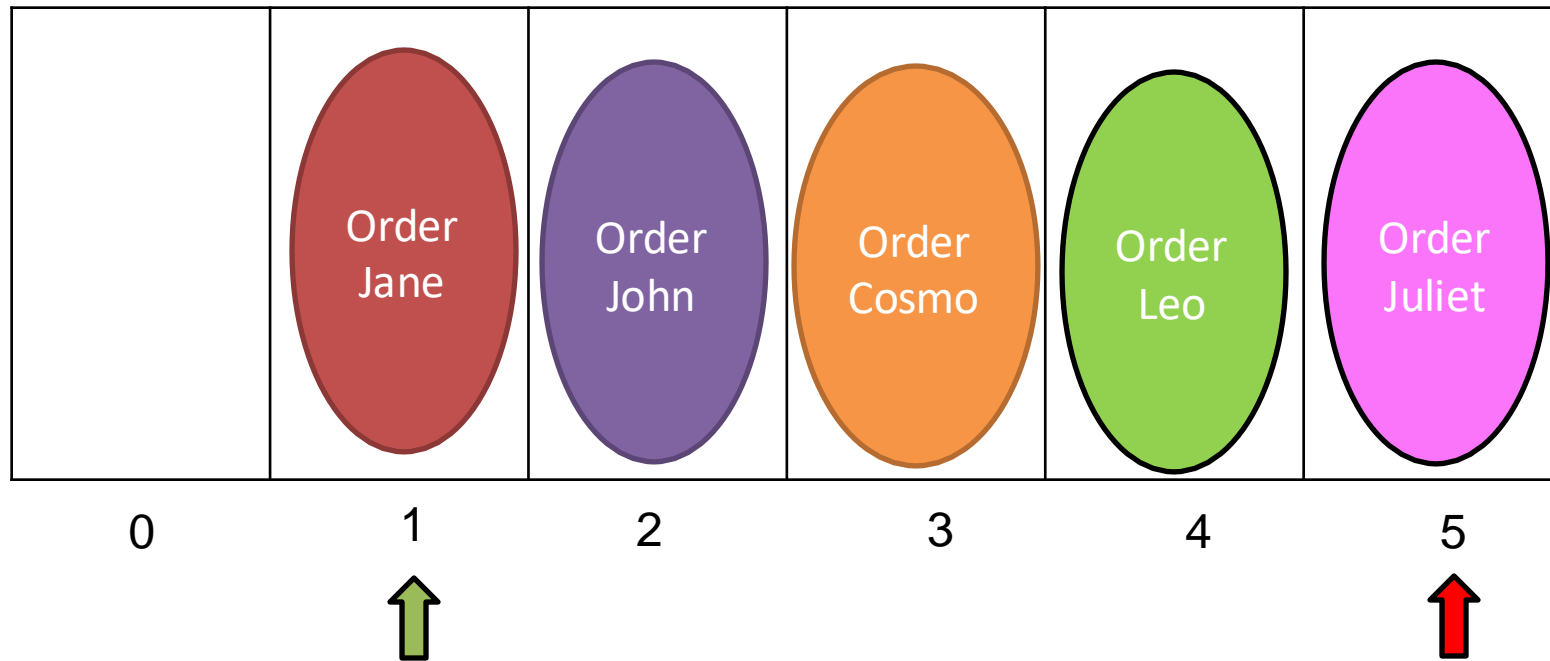


Remove the front element,
move front pointer forward
one spot

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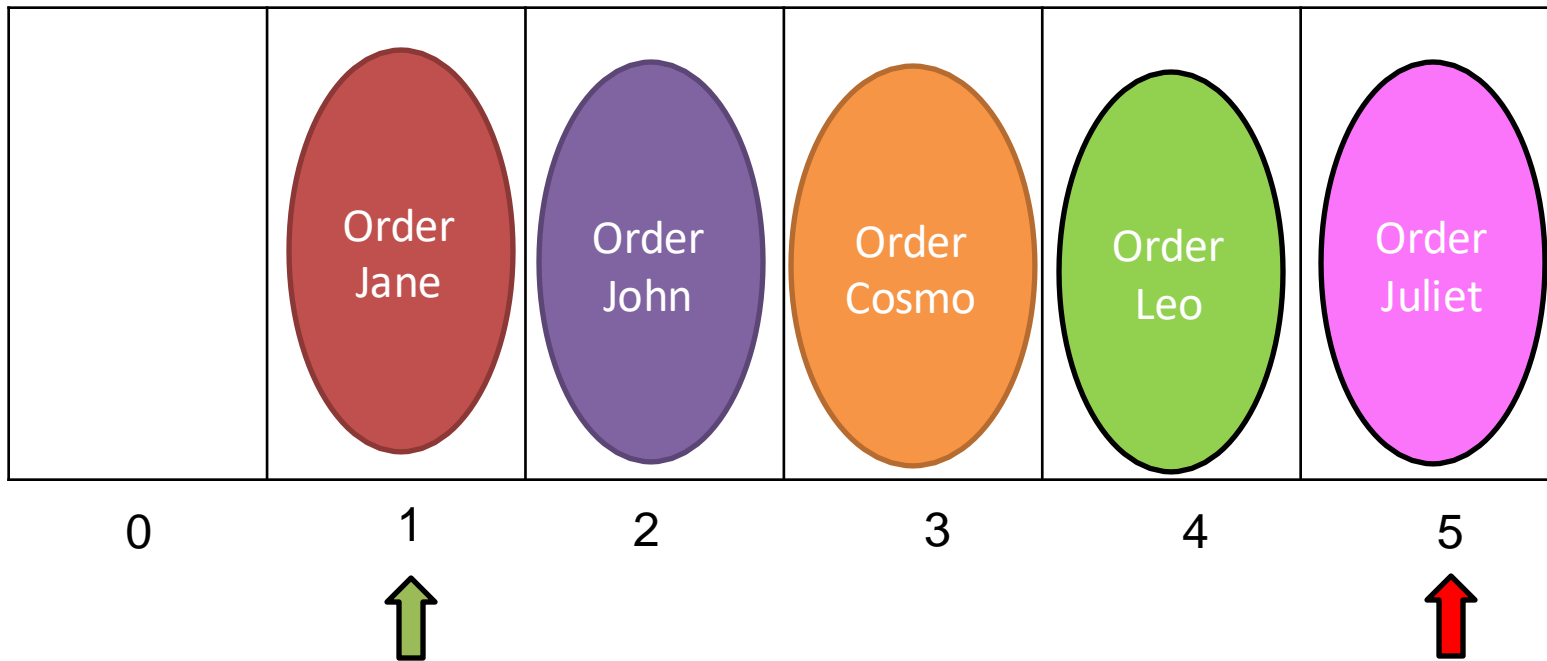


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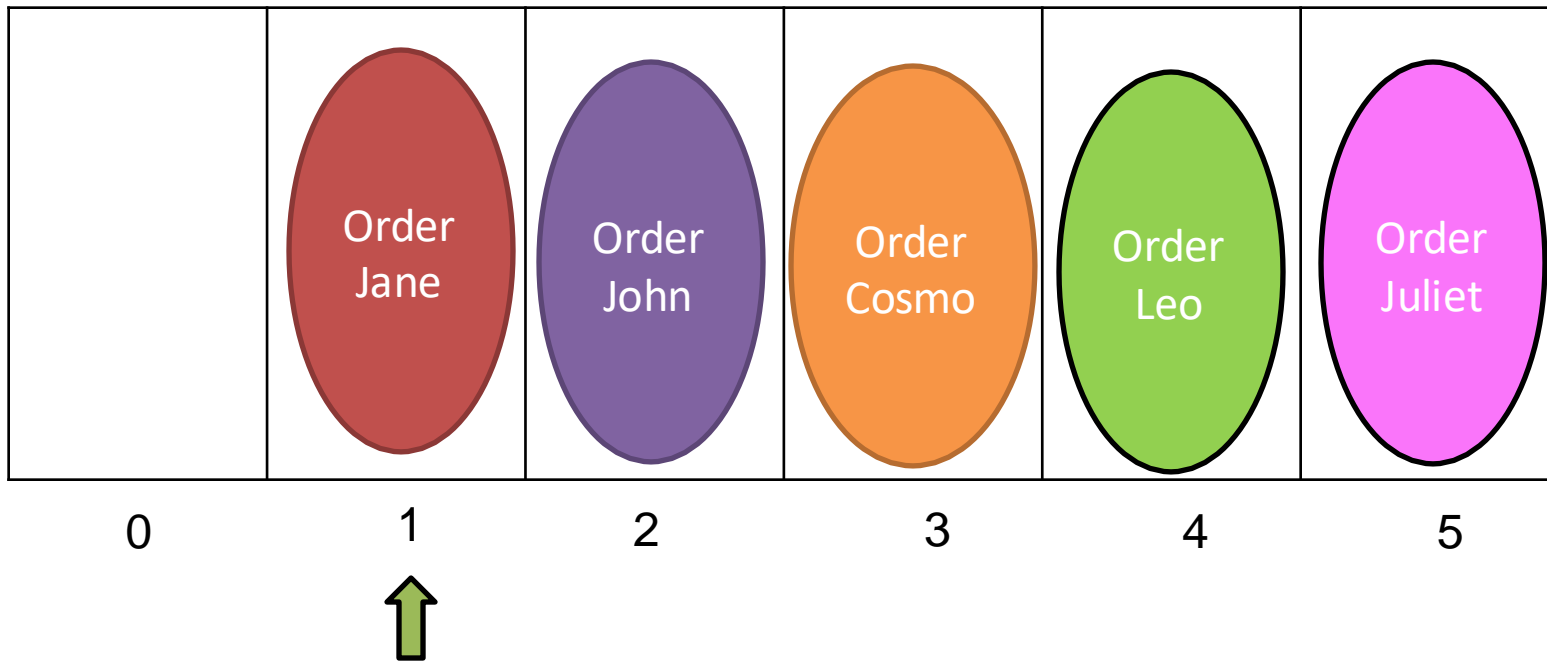
Enqueue again?

```
public void enqueue(Order newOrder) {  
  
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capacity = 6 front = 0
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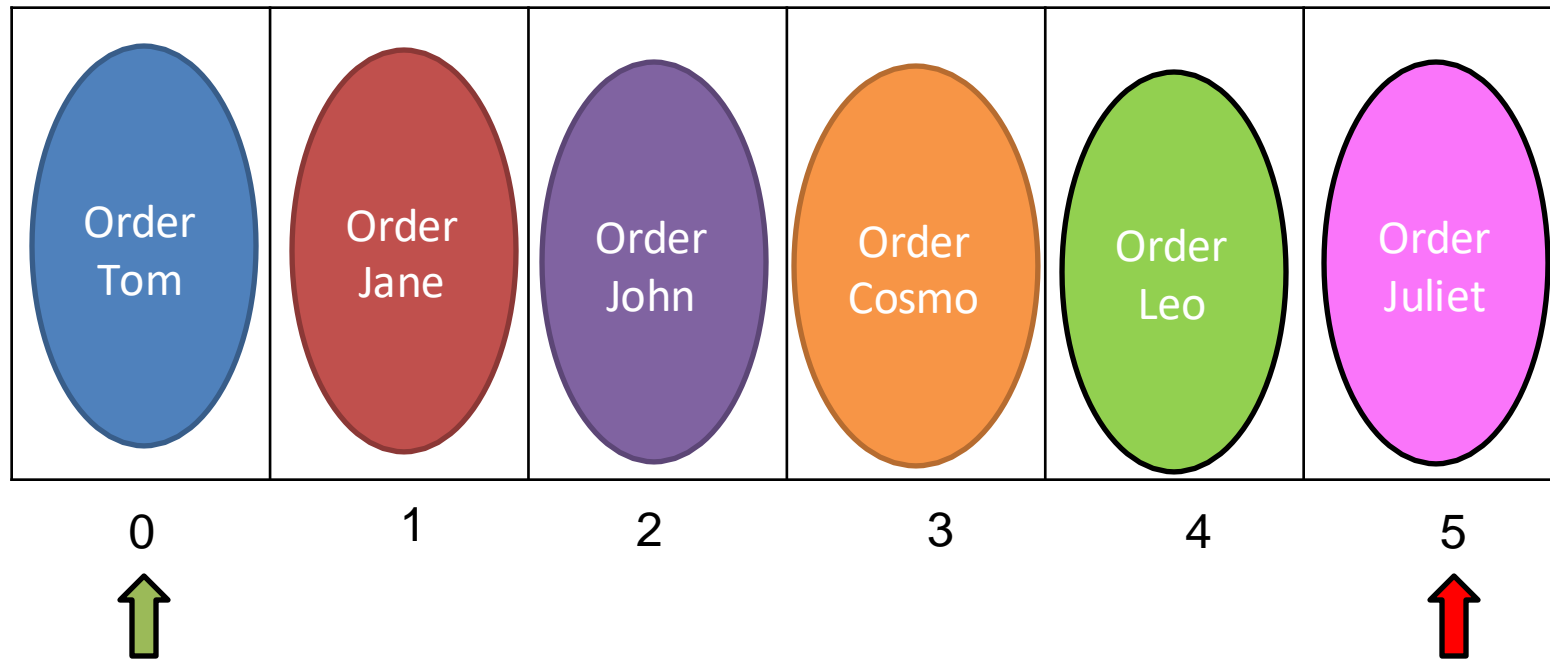
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Array index out of bounds error!

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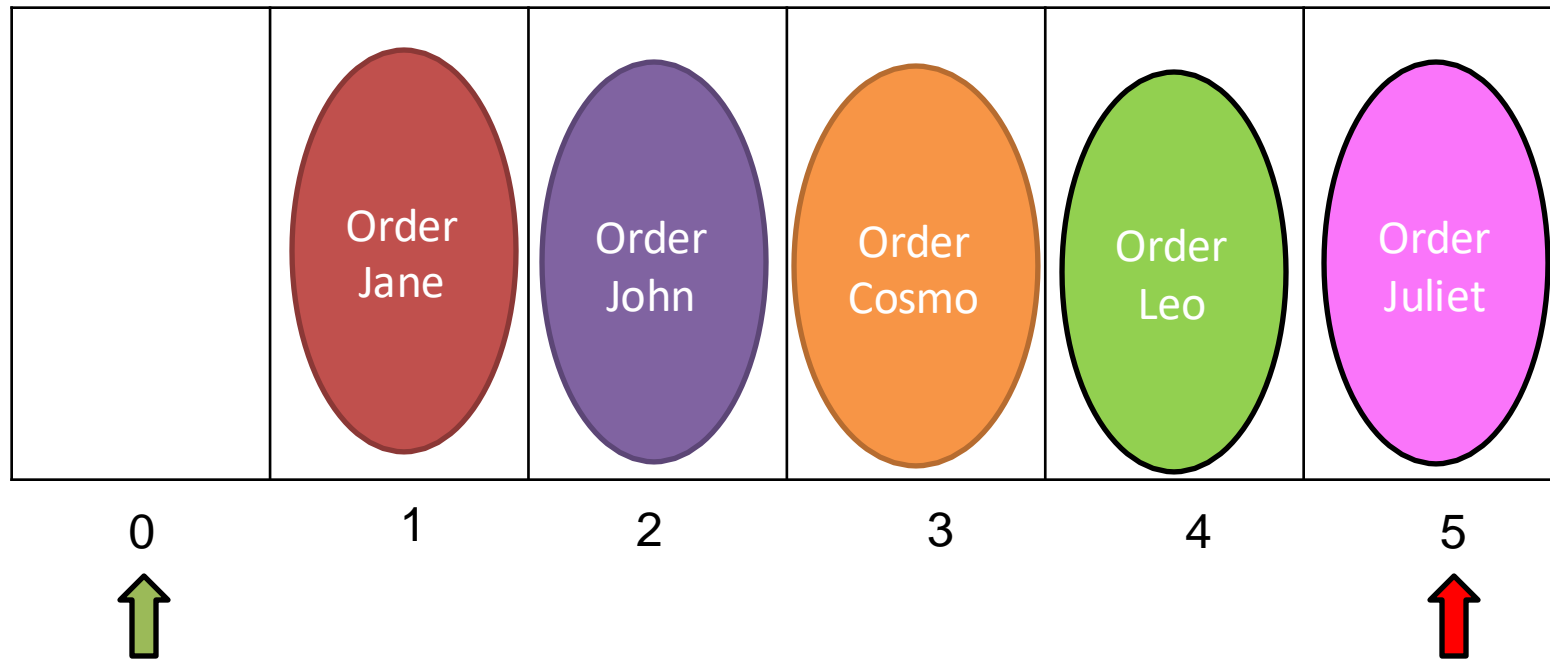
Dequeue?

1. Remove the front element
2. Make some room in the back

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size = 6 rear = 5

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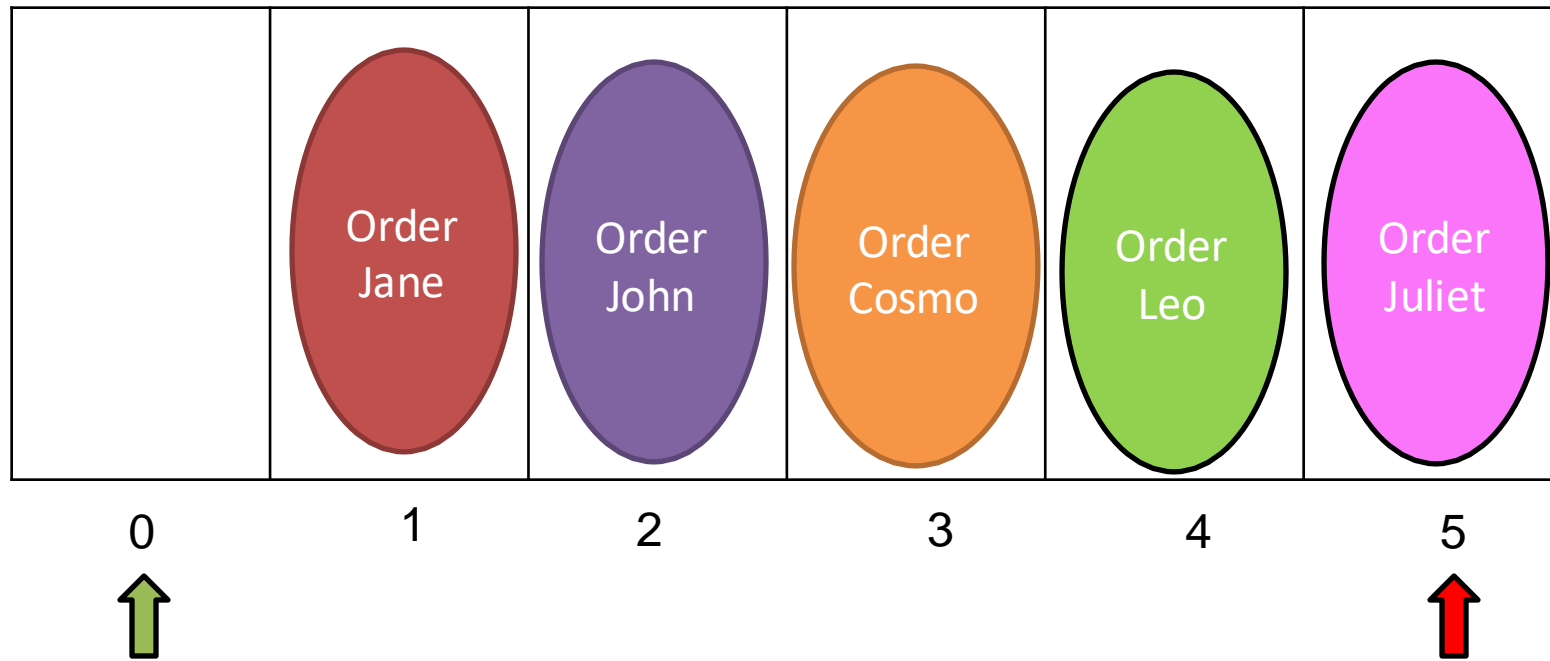
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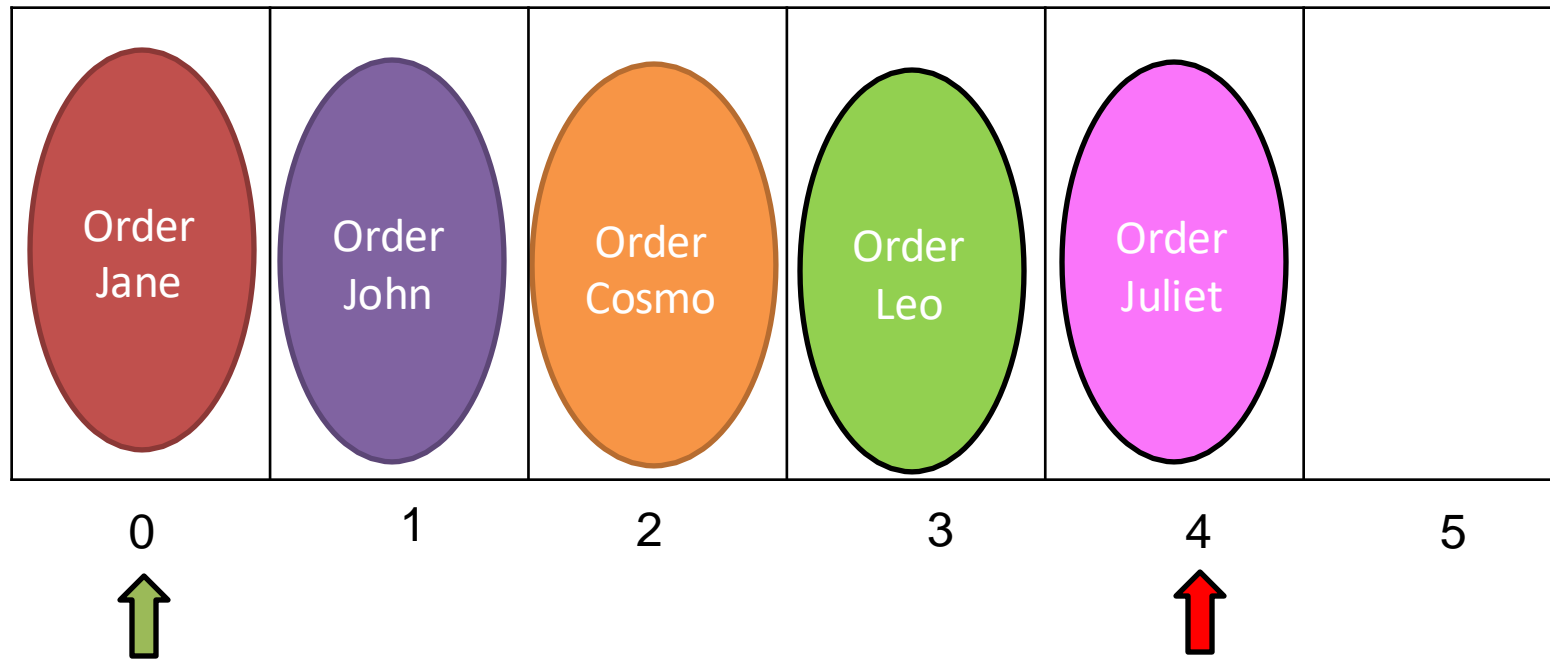
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Shift all of our data over one spot

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Dequeue?

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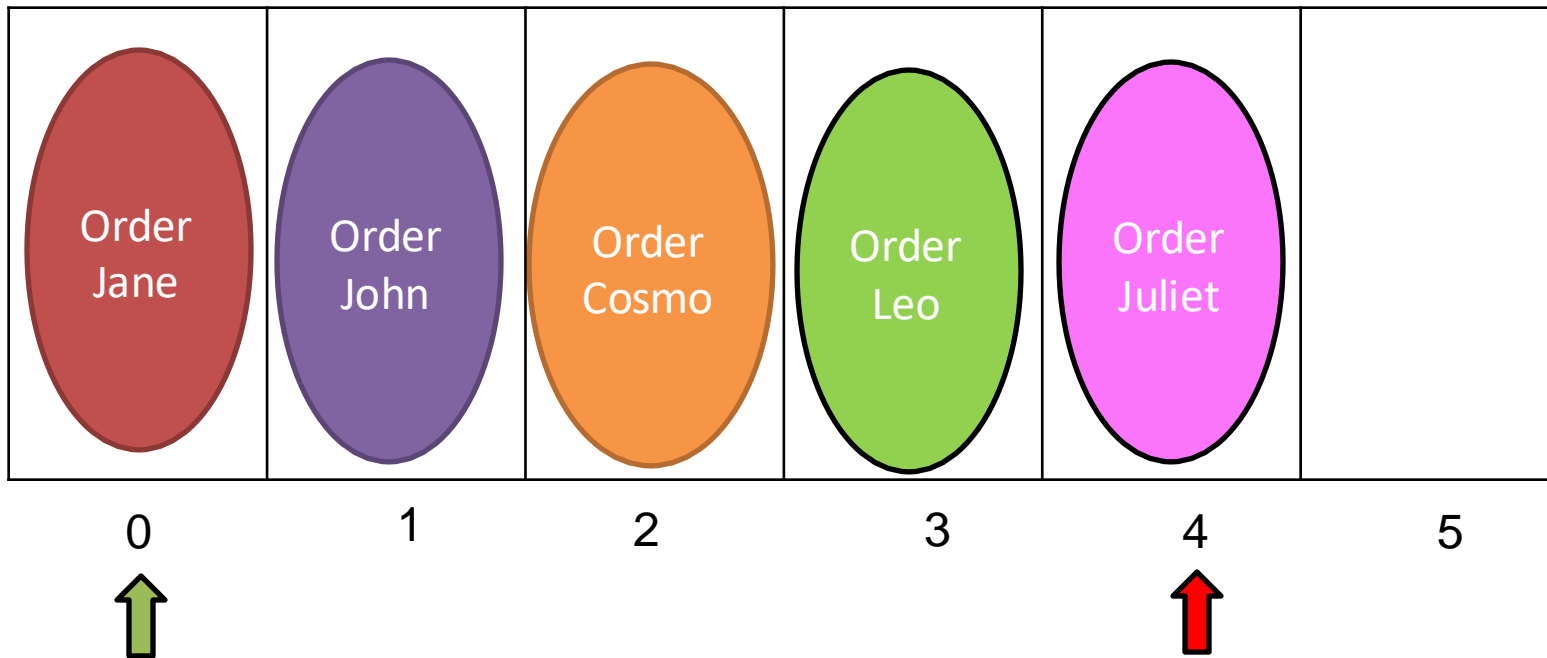
Shift all of our data over one spot

The front of our queue will **always** stay at zero

capacity = 6 front = 0
size = 5 rear = 4

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Suppose that we have a queue that can hold 6 elements



```
public Order dequeue() {  
    if (size == 0) {  
        System.out.println("Empty");  
        return null;  
    }  
  
    Order temp = data[0];  
  
    for (int i = 0; i < size - 1; i++) {  
        data[i] = data[i + 1];  
    }  
  
    data[size-1] = null;  
    size--;  
  
    return temp;  
}
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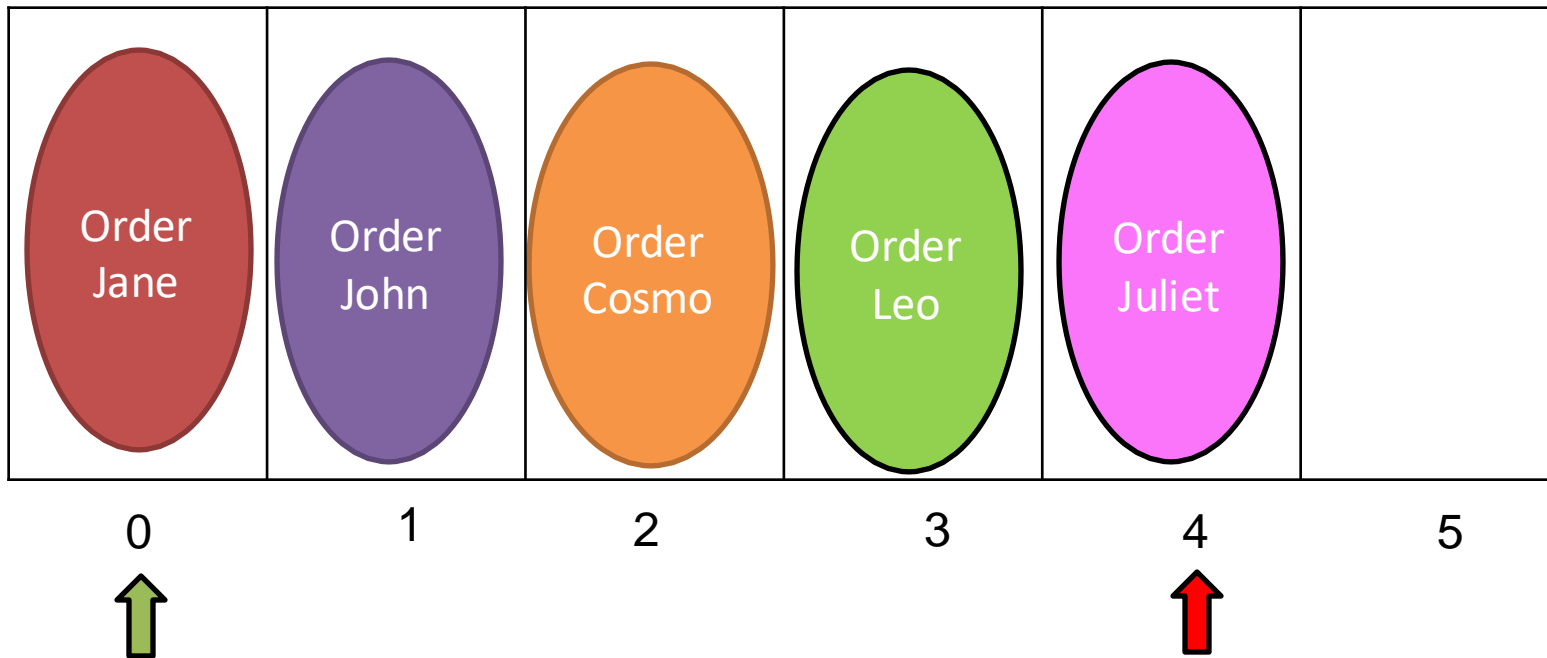
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Order temp =

Order
Jane



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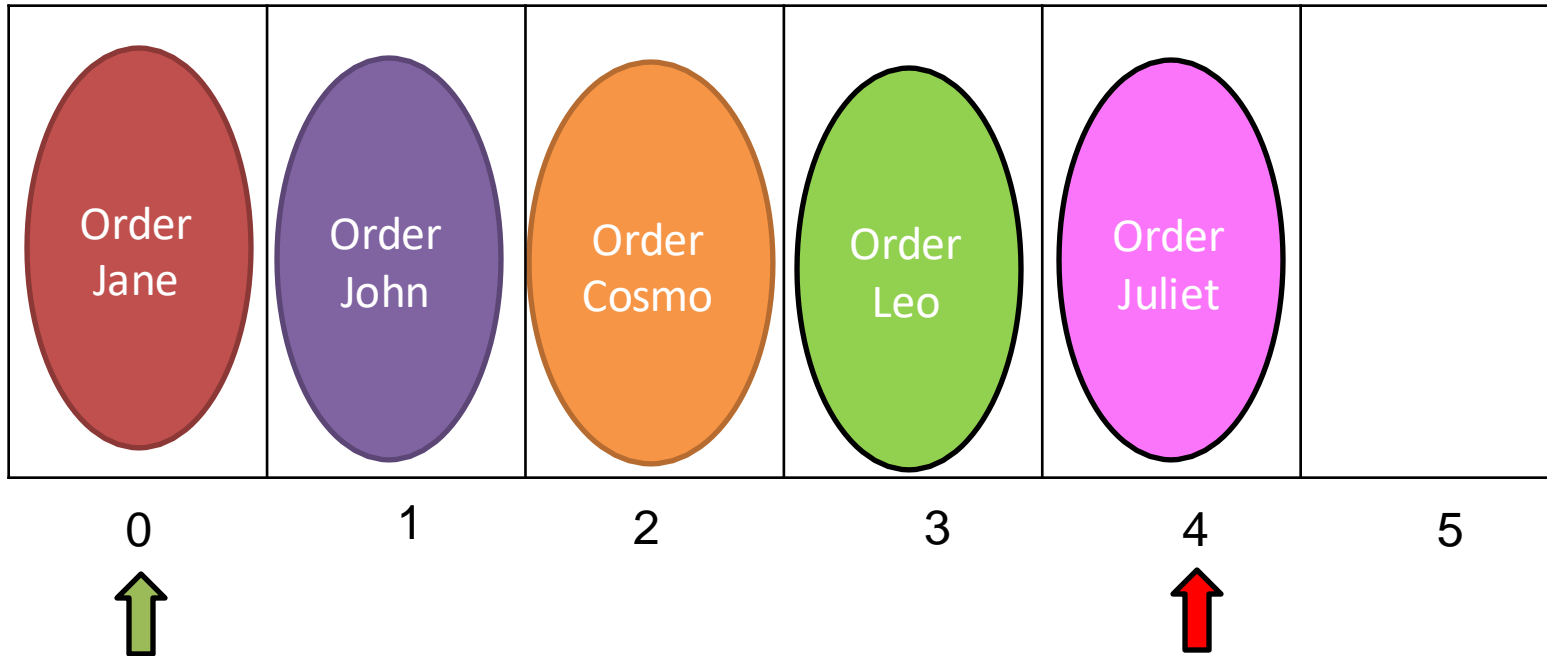
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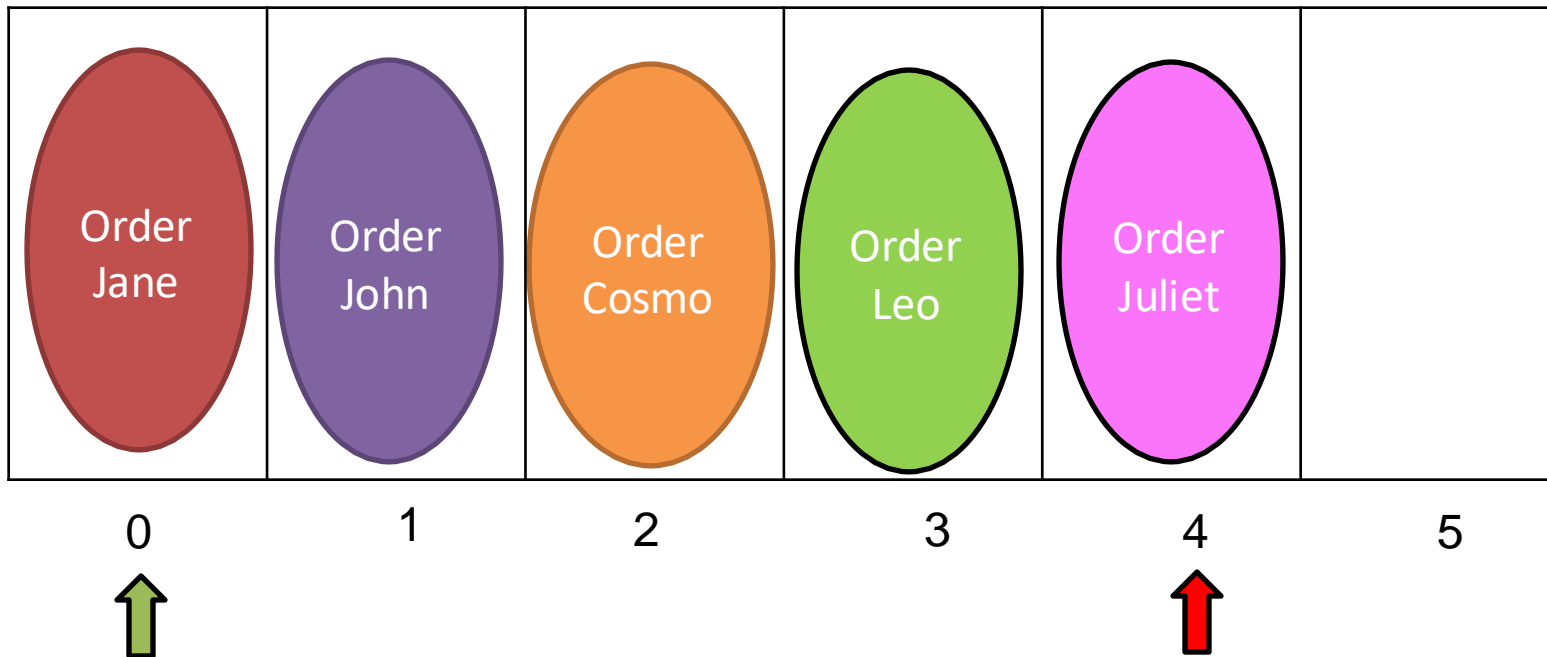
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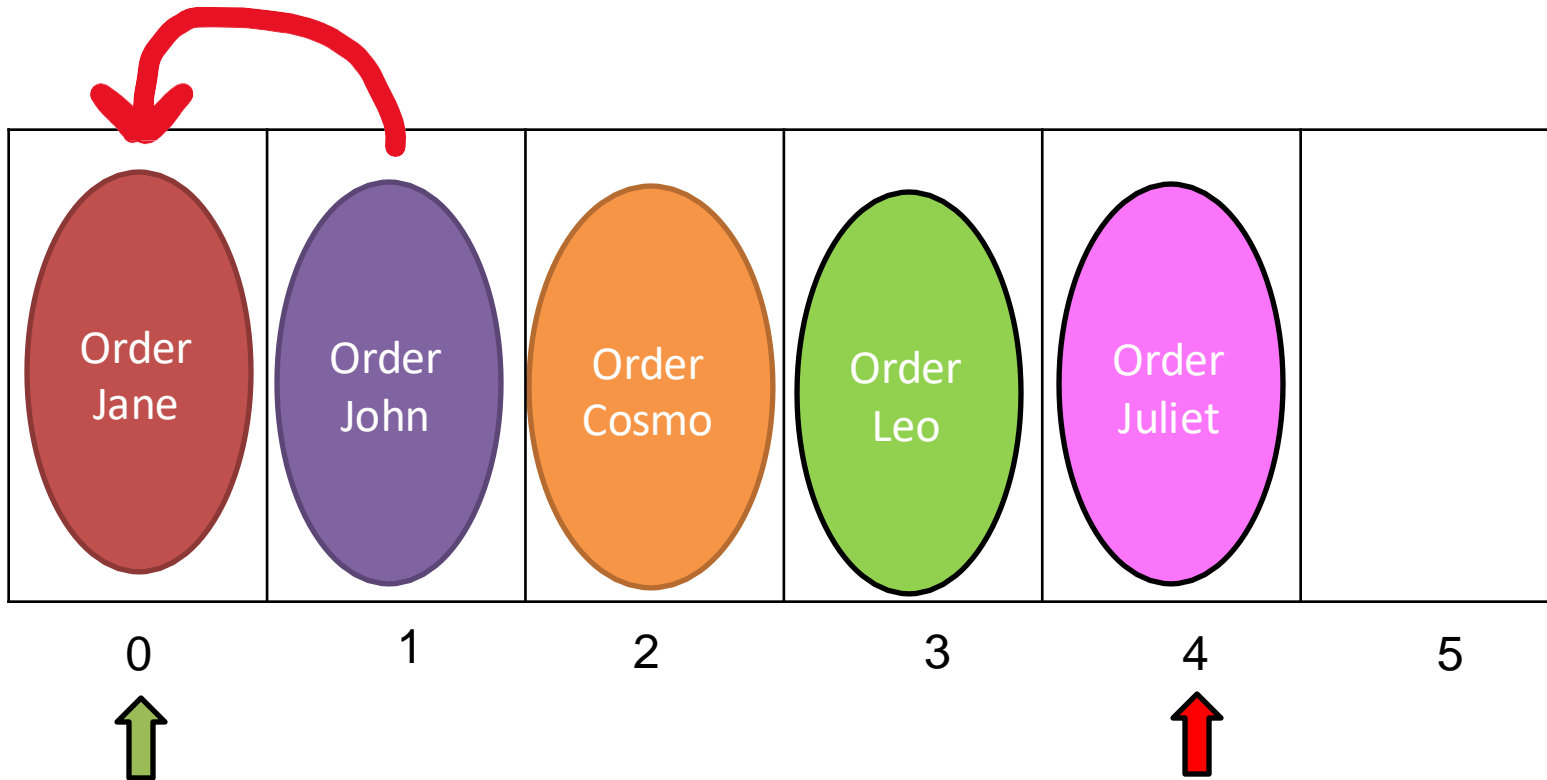
Shift everything over one spot

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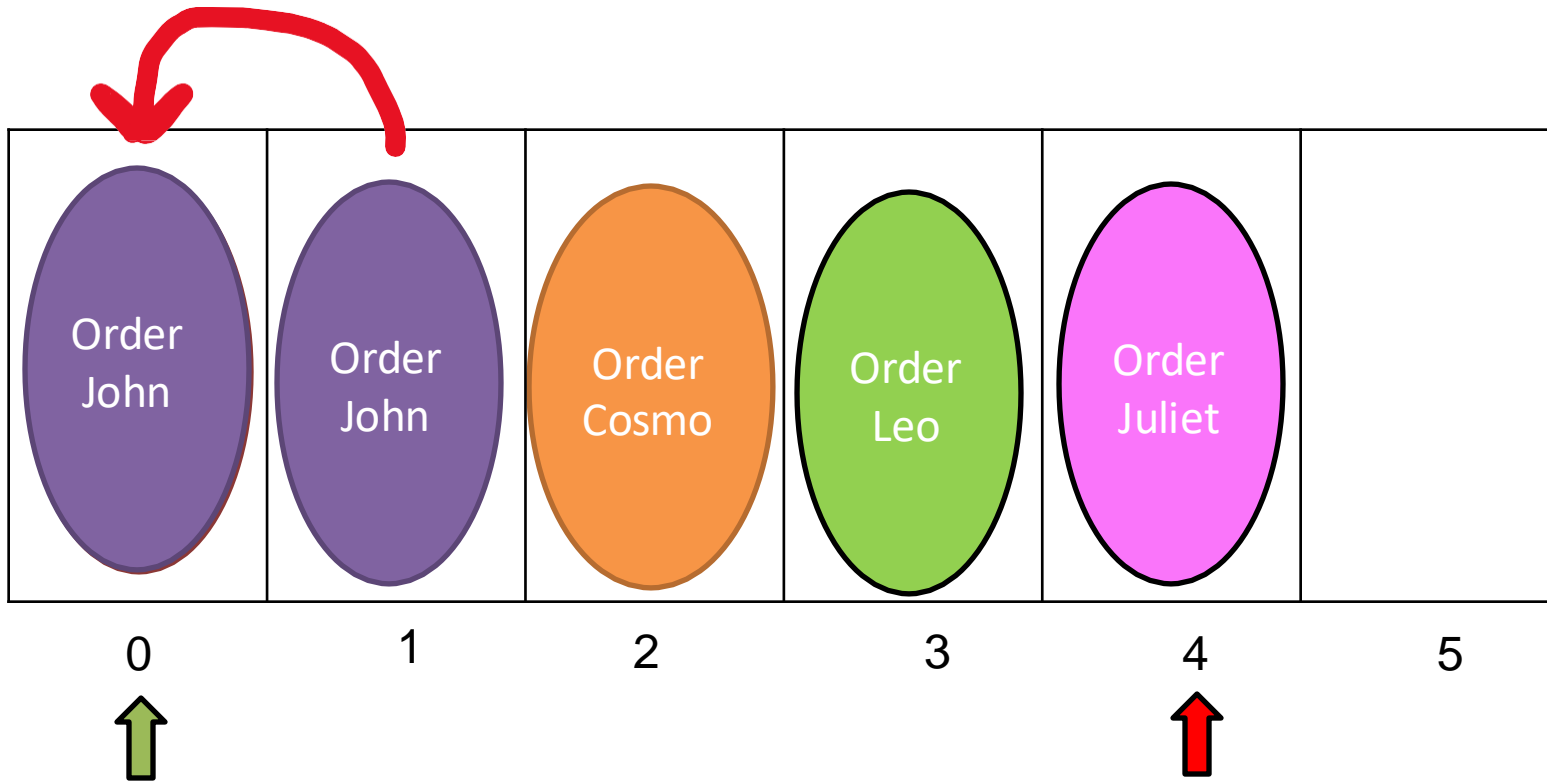
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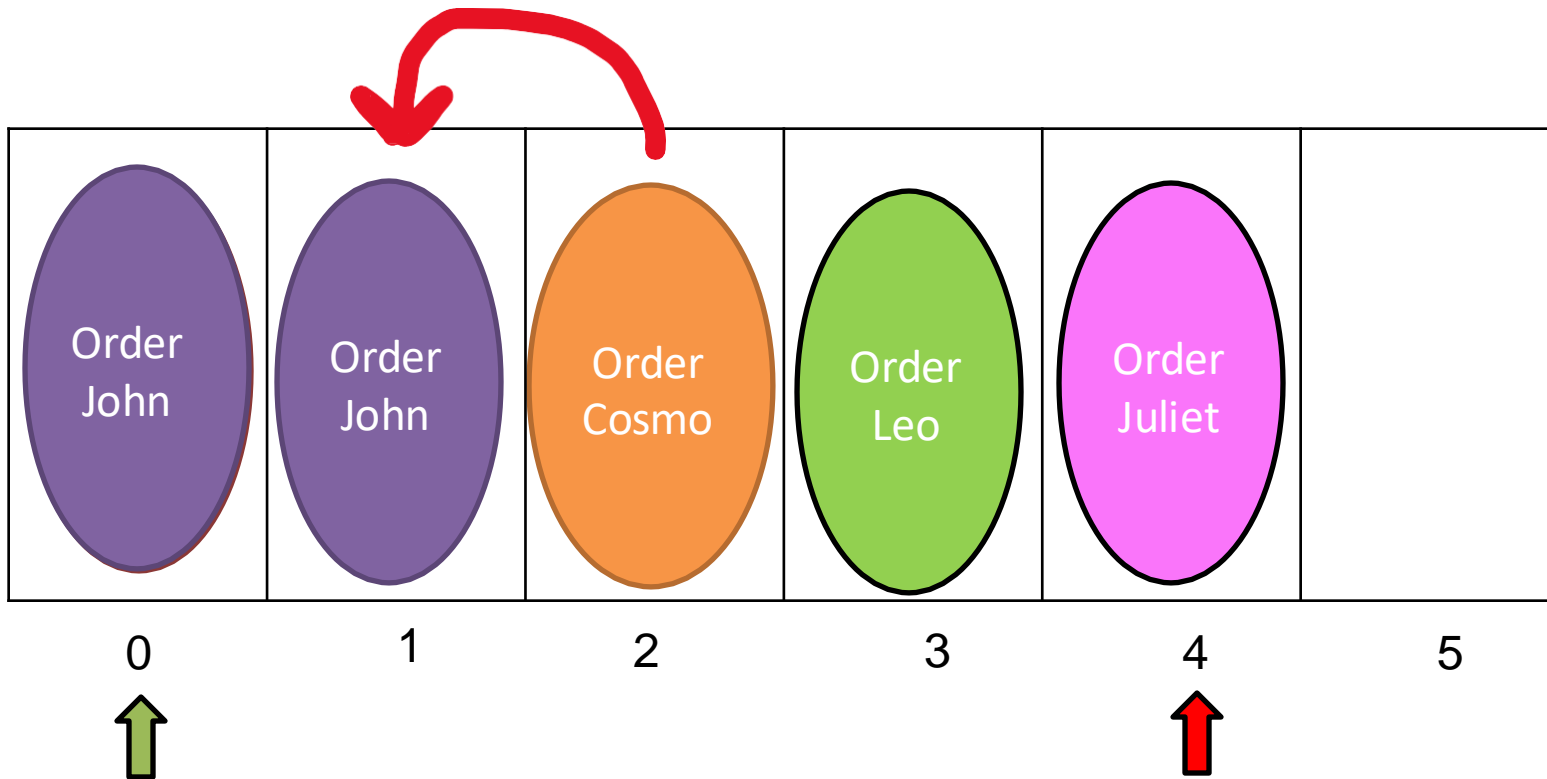
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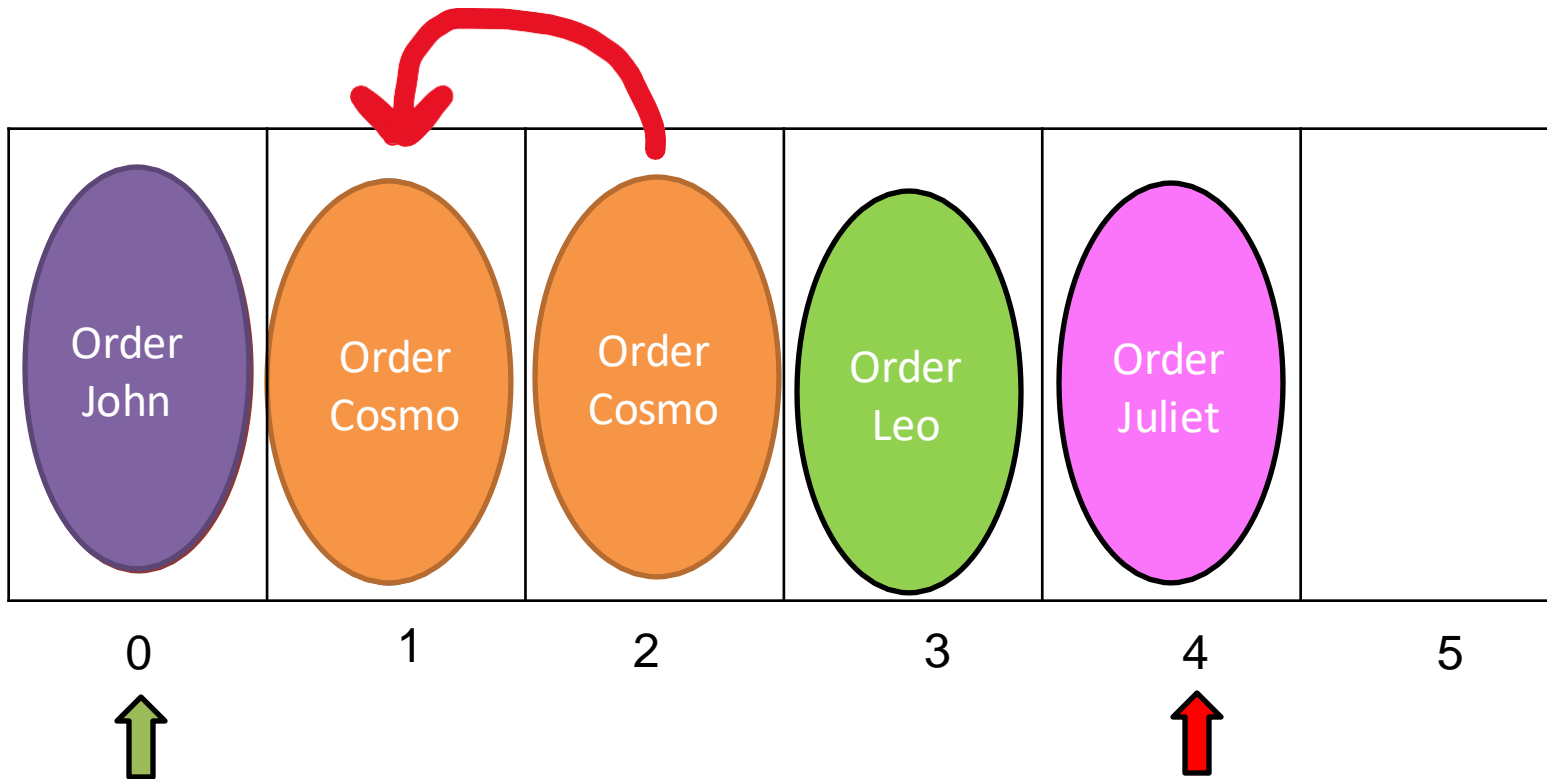
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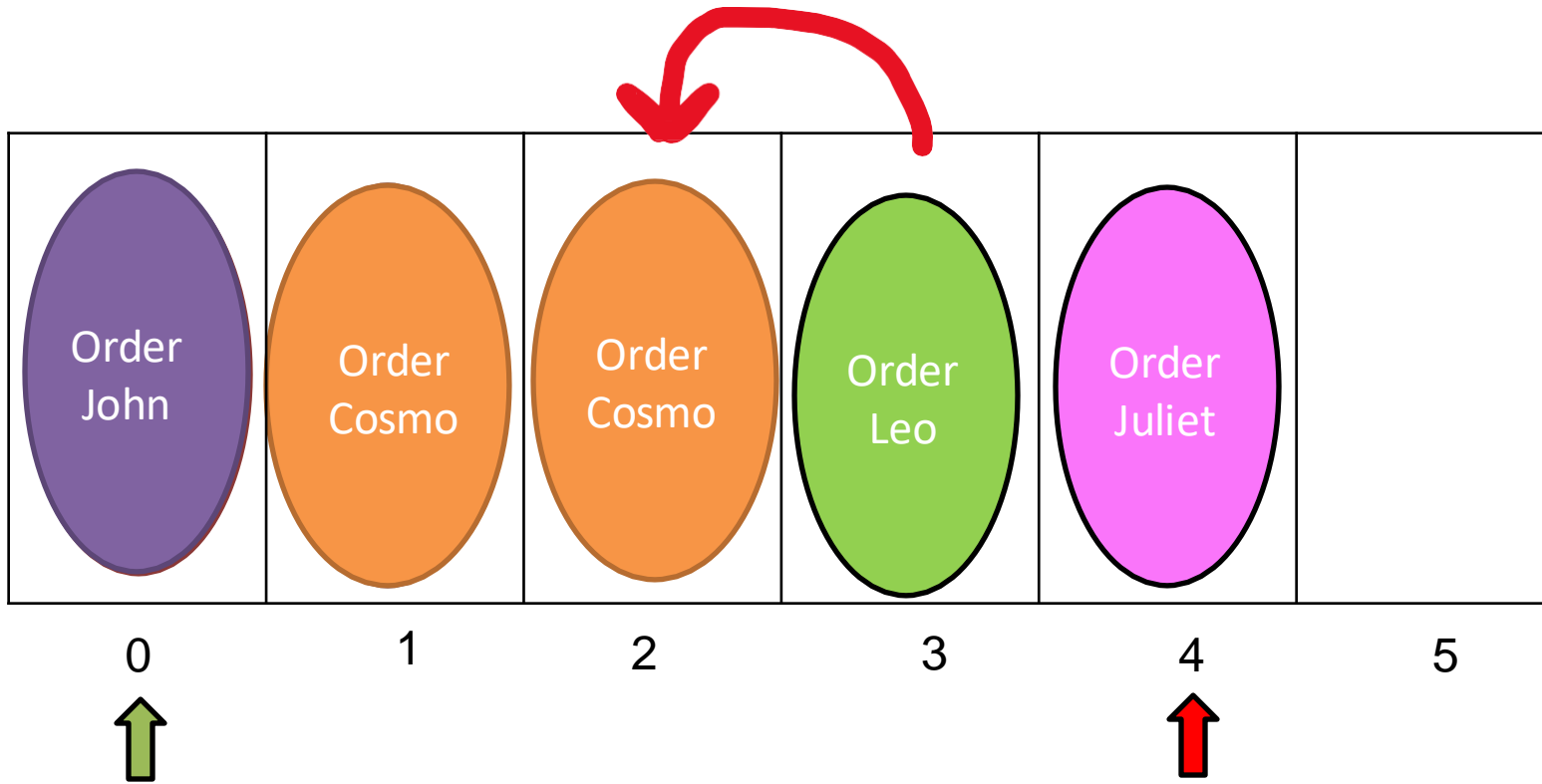
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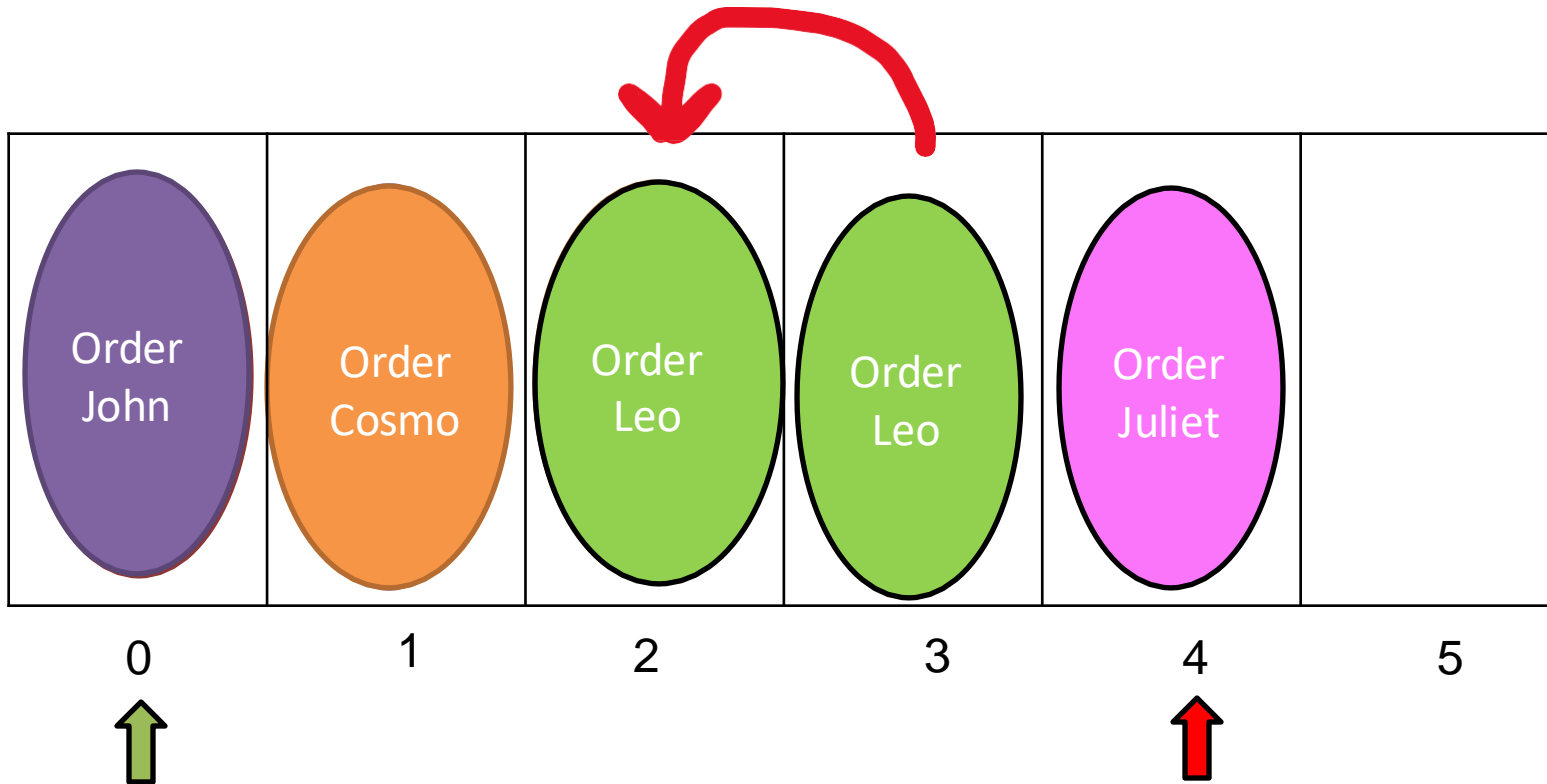
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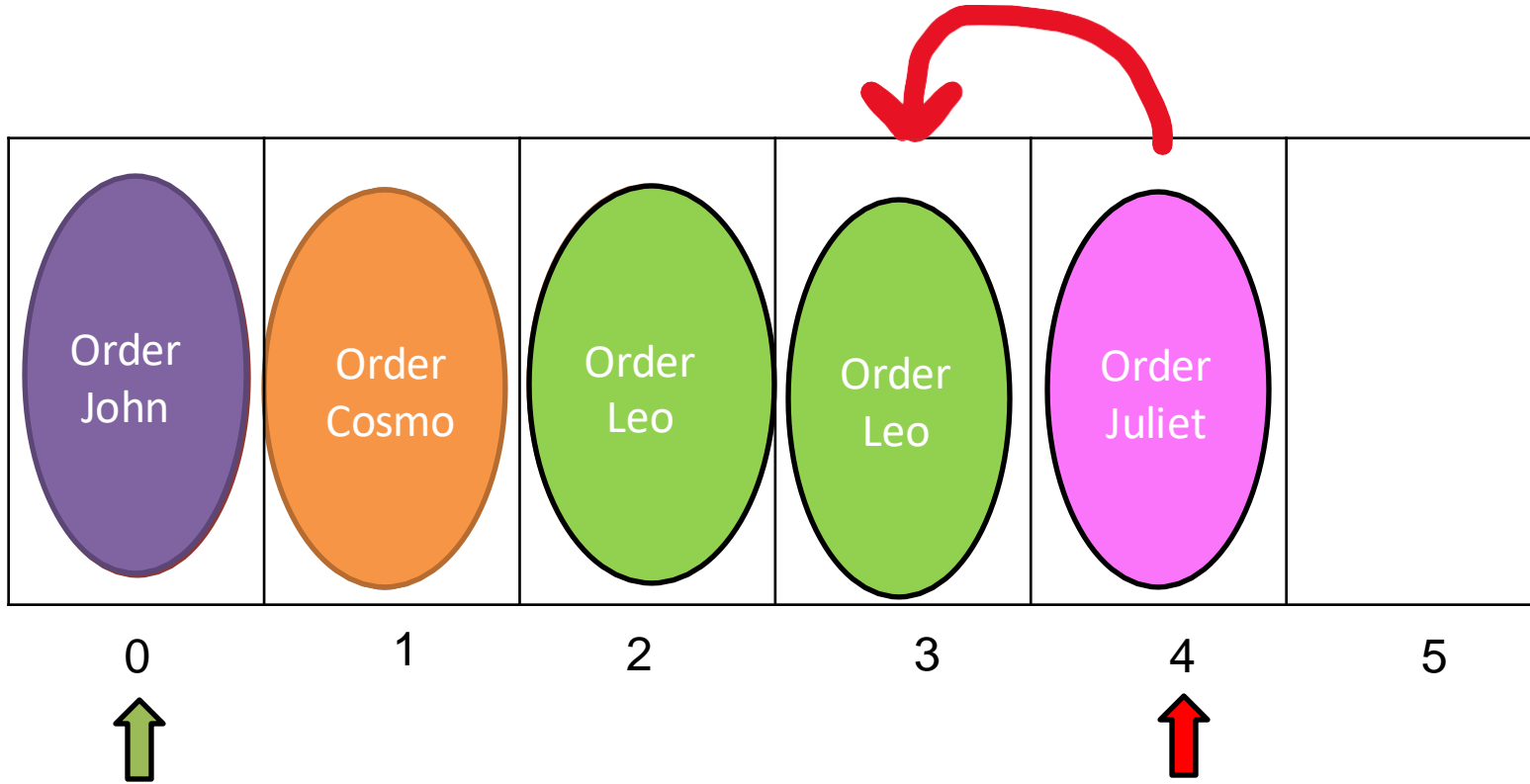
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public Order dequeue() {  
    if (size == 0) {  
        System.out.println("Empty");  
        return null;  
    }  
  
    Order temp = data[0];  
  
    for (int i = 0; i < size - 1; i++) {  
        data[i] = data[i + 1];  
    }  
  
    data[size-1] = null;  
    size--;  
  
    return temp;  
}
```

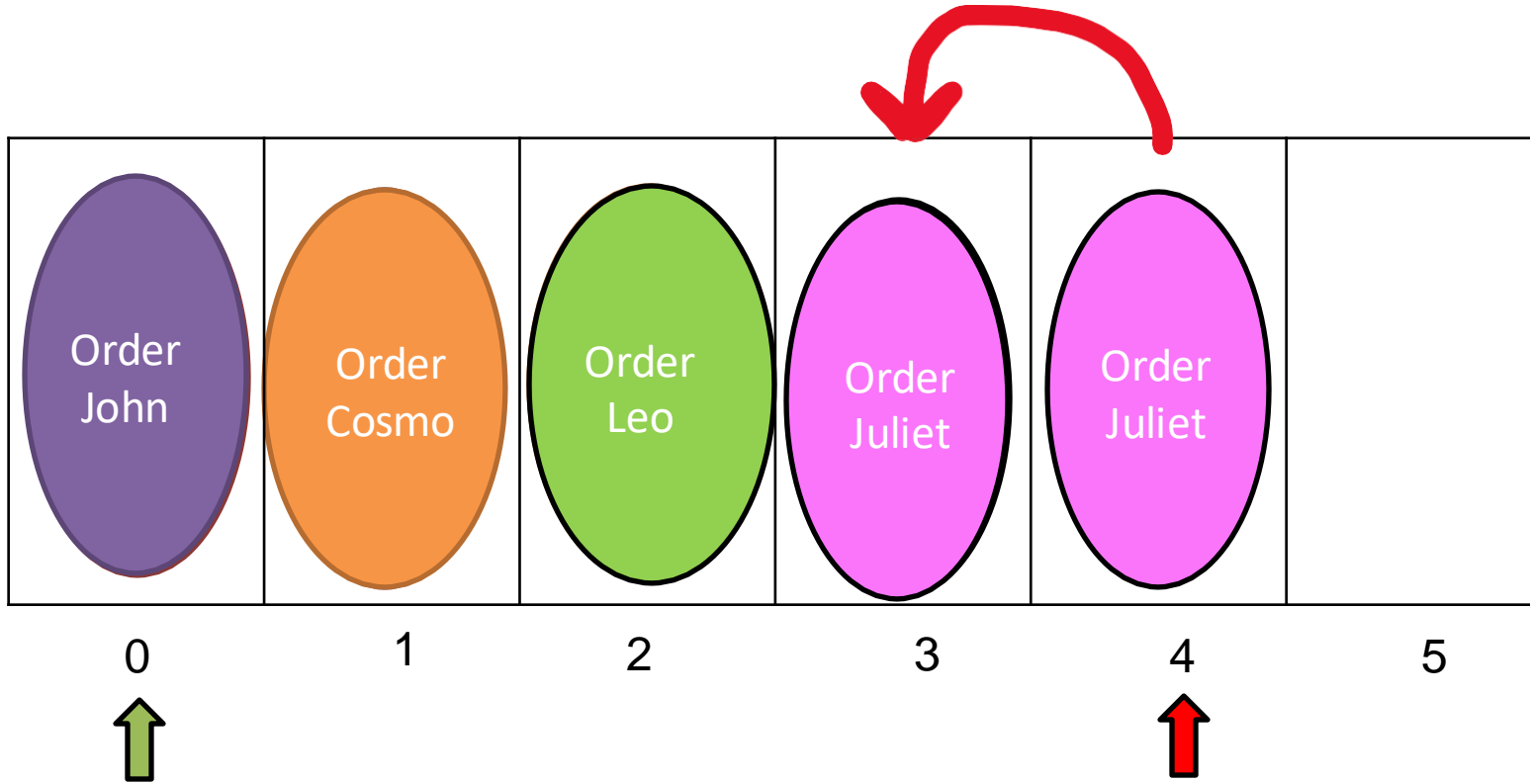
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Today, we will be implementing a Queue with an Array.

Suppose that we have a queue that can hold 6 elements

Order temp =

Order
Jane



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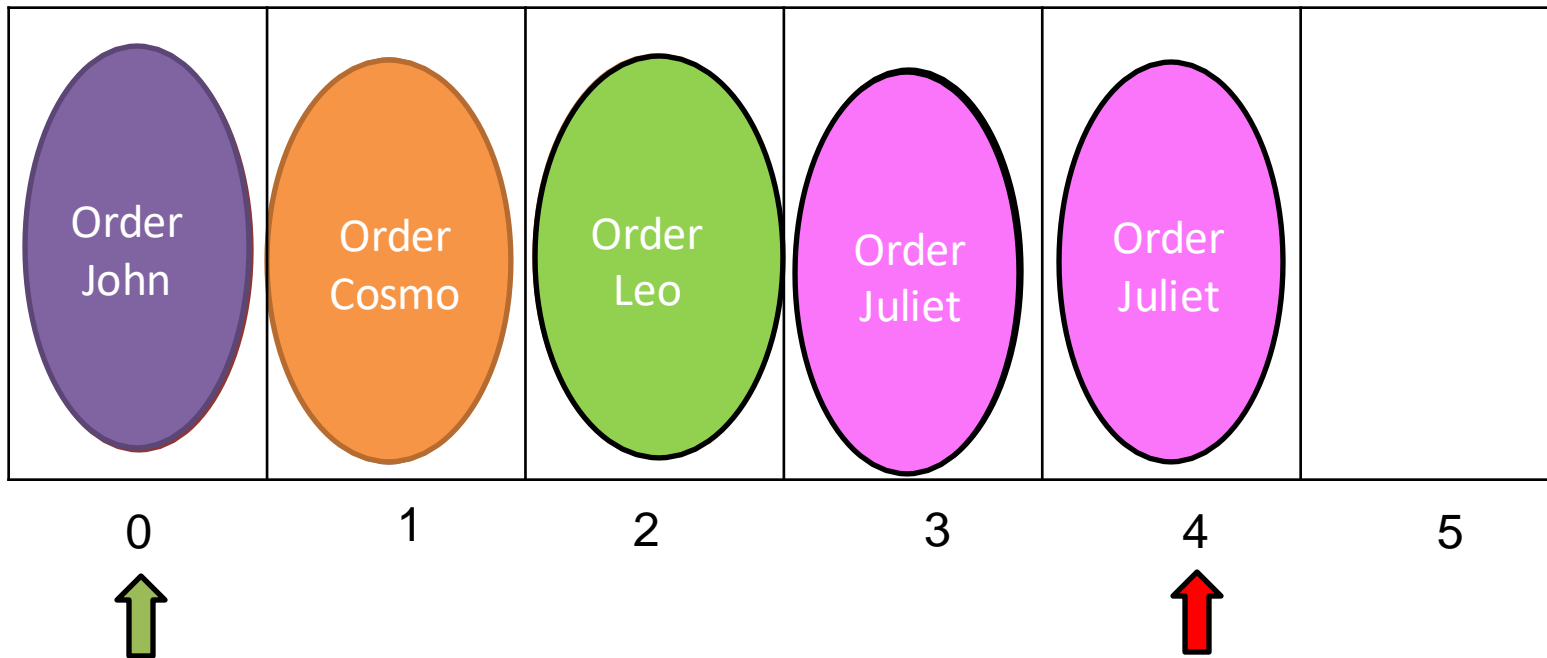
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    data[size-1] = null;  
    size--;  
  
    return temp;  
}
```

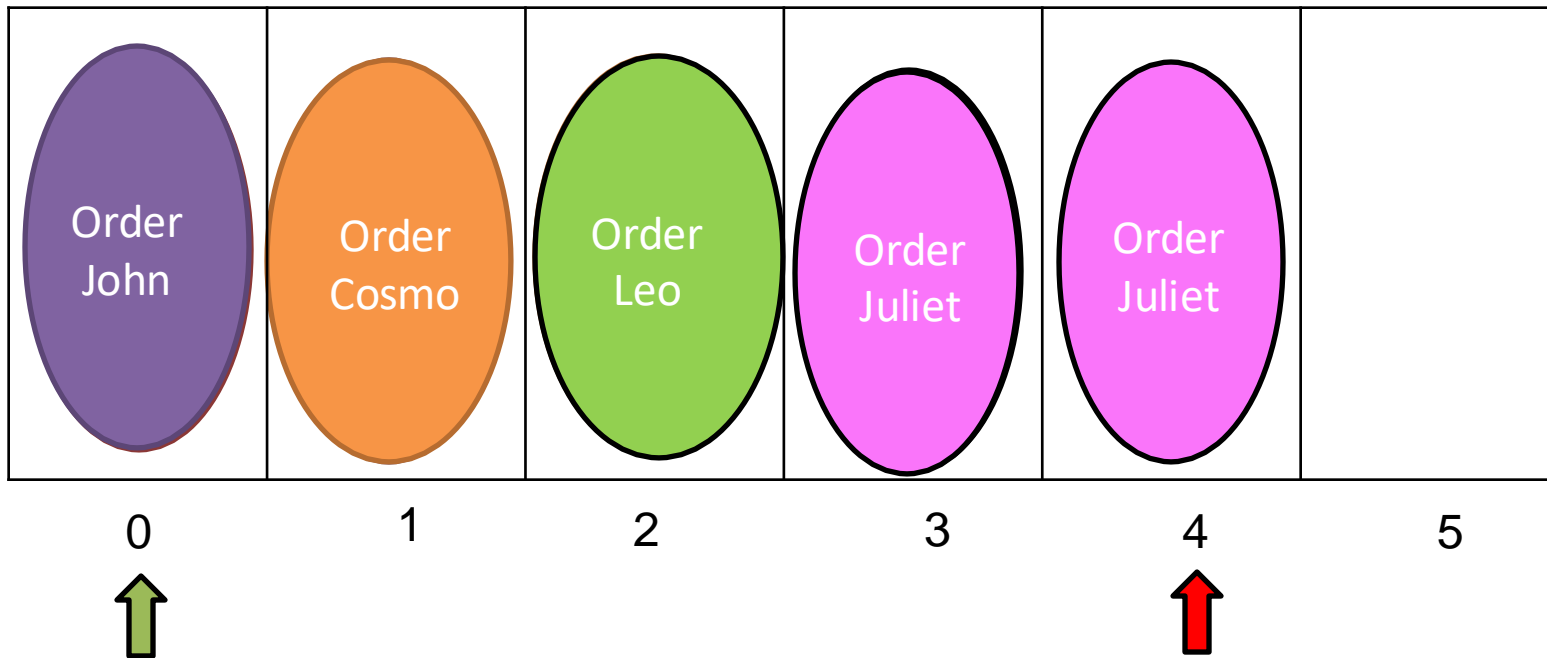
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    data[size-1] = null;  
    size--;  
  
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}
```

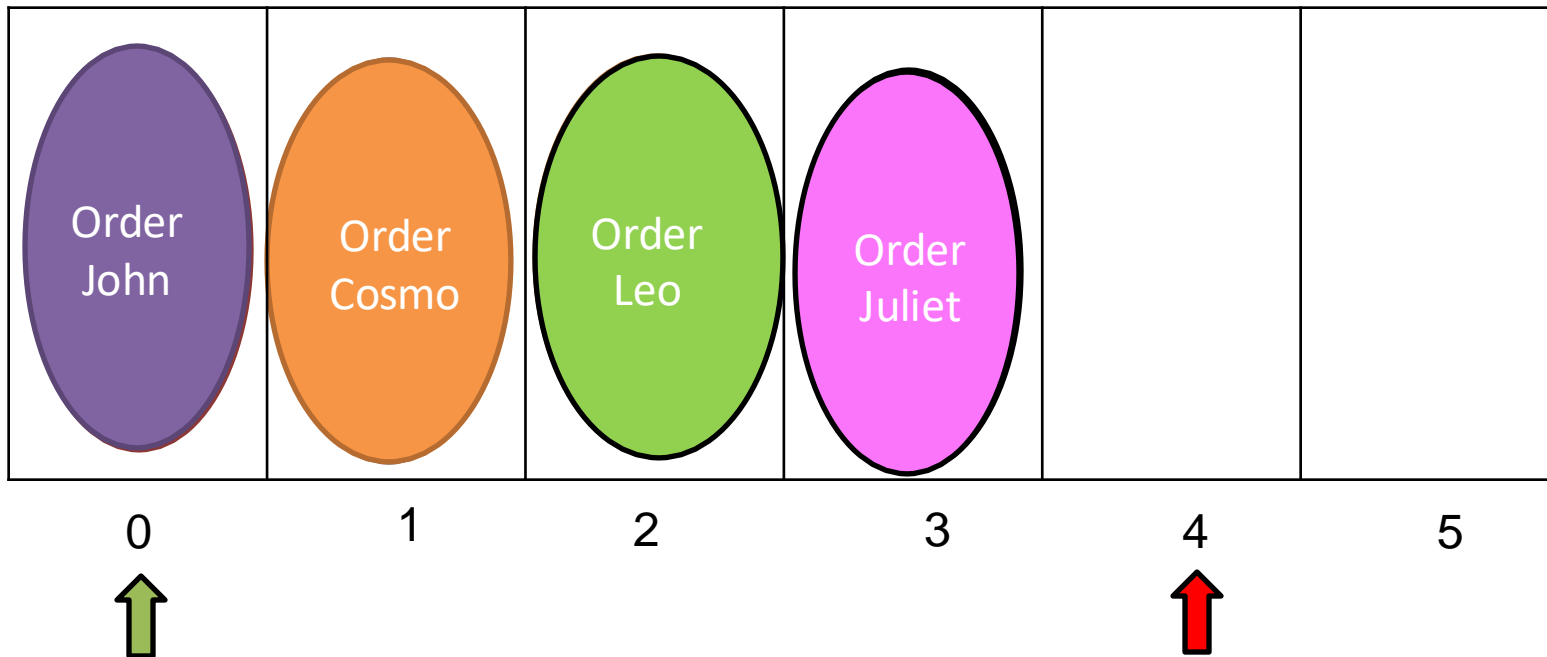
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    }  
  
    data[size-1] = null;  
    size--;  
  
    return temp;  
}
```

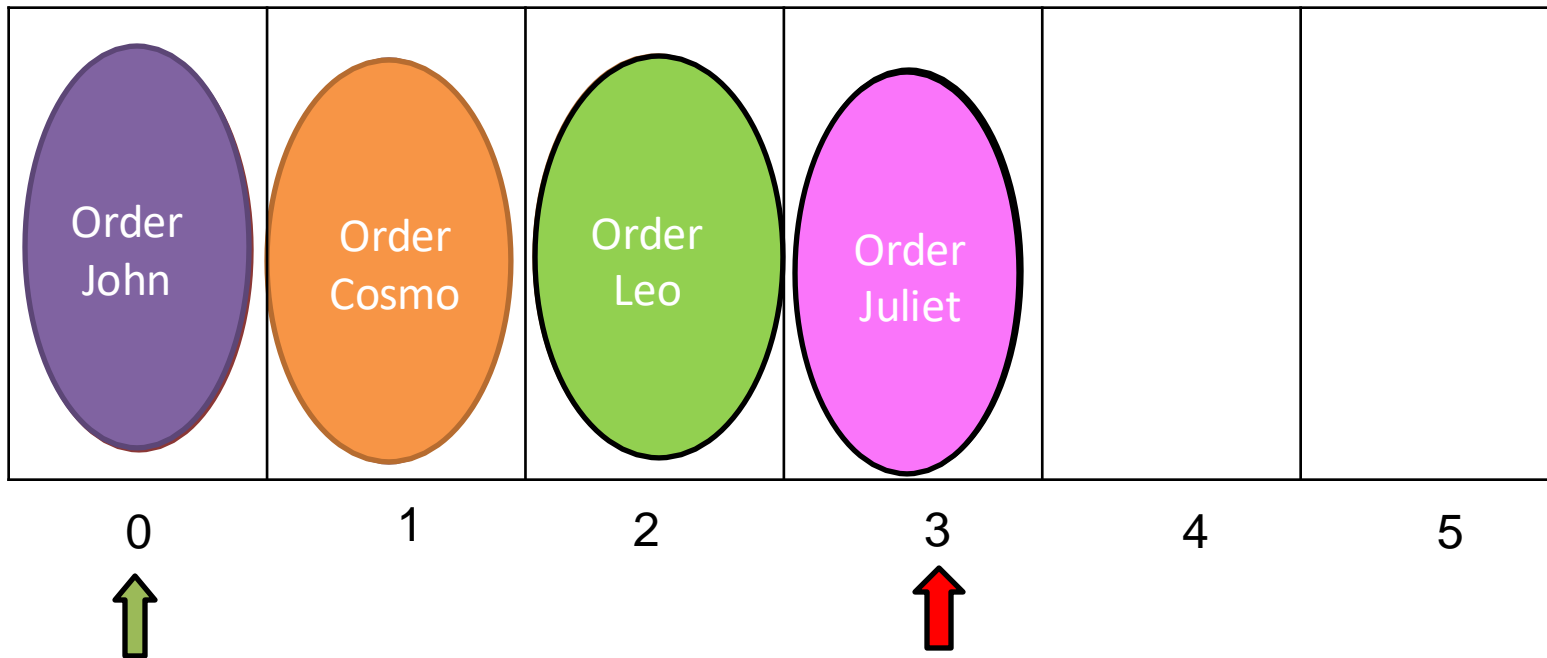
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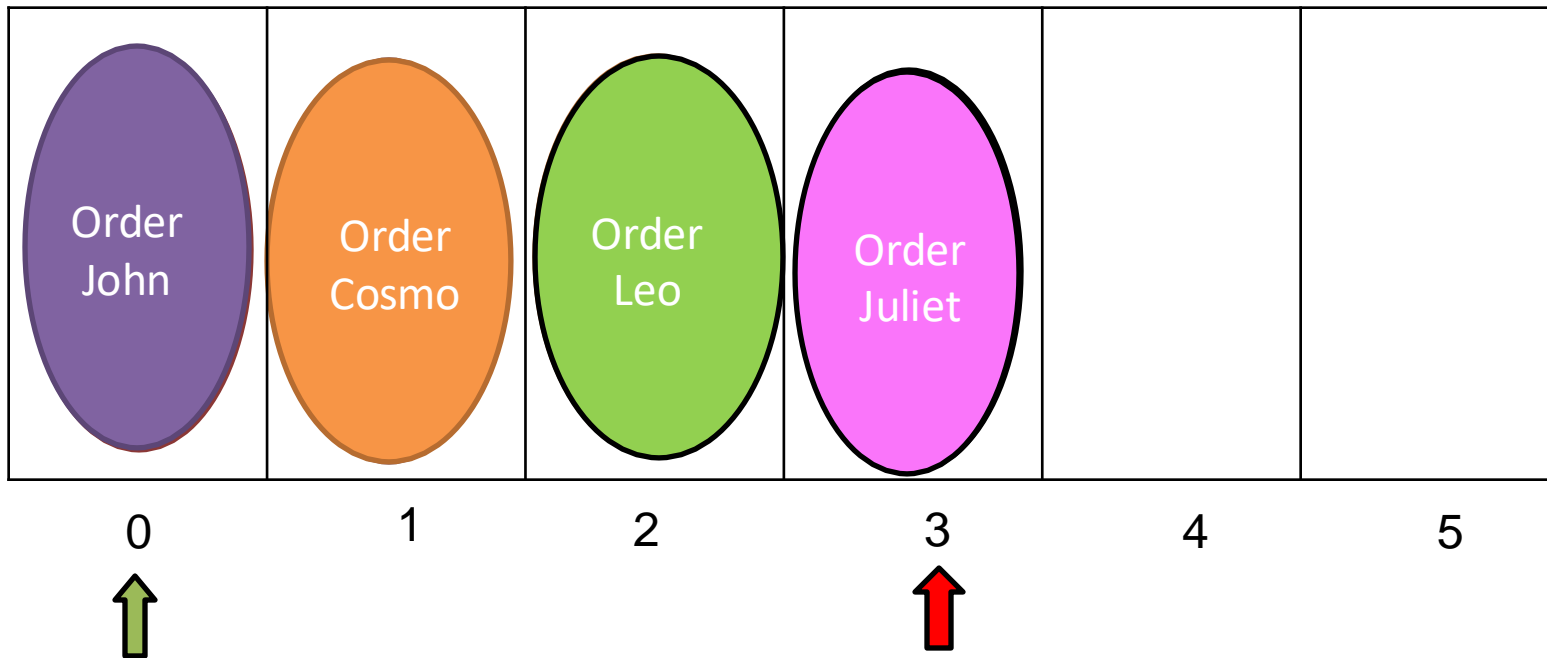


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    for (int i = 0; i < size - 1; i++) {  
        data[i] = data[i + 1];  
    }  
  
    data[size-1] = null;  
    size--;  
  
    return temp;  
}
```

capacity = 6 front = 0
size = 4 rear = 3

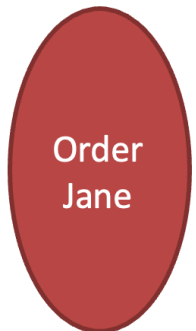
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Suppose that we have a queue that can hold 6 elements



```
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}
```

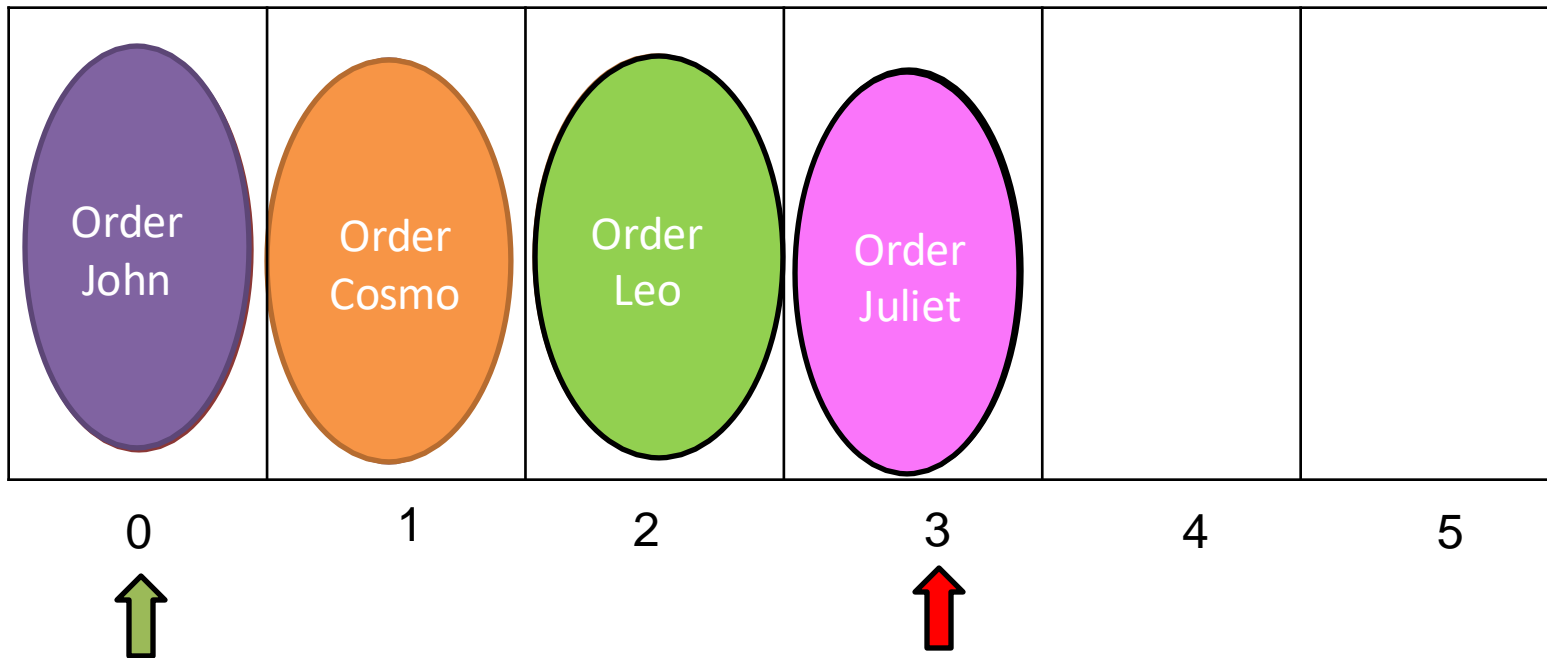
Order temp =



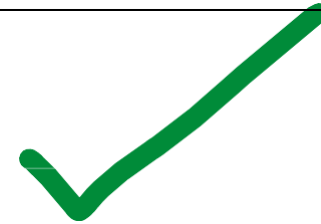
capacity = 6 front = 0
size = 4 rear = 3

Today, we will be implementing a Queue with an Array.

Suppose that we have a queue that can hold 6 elements



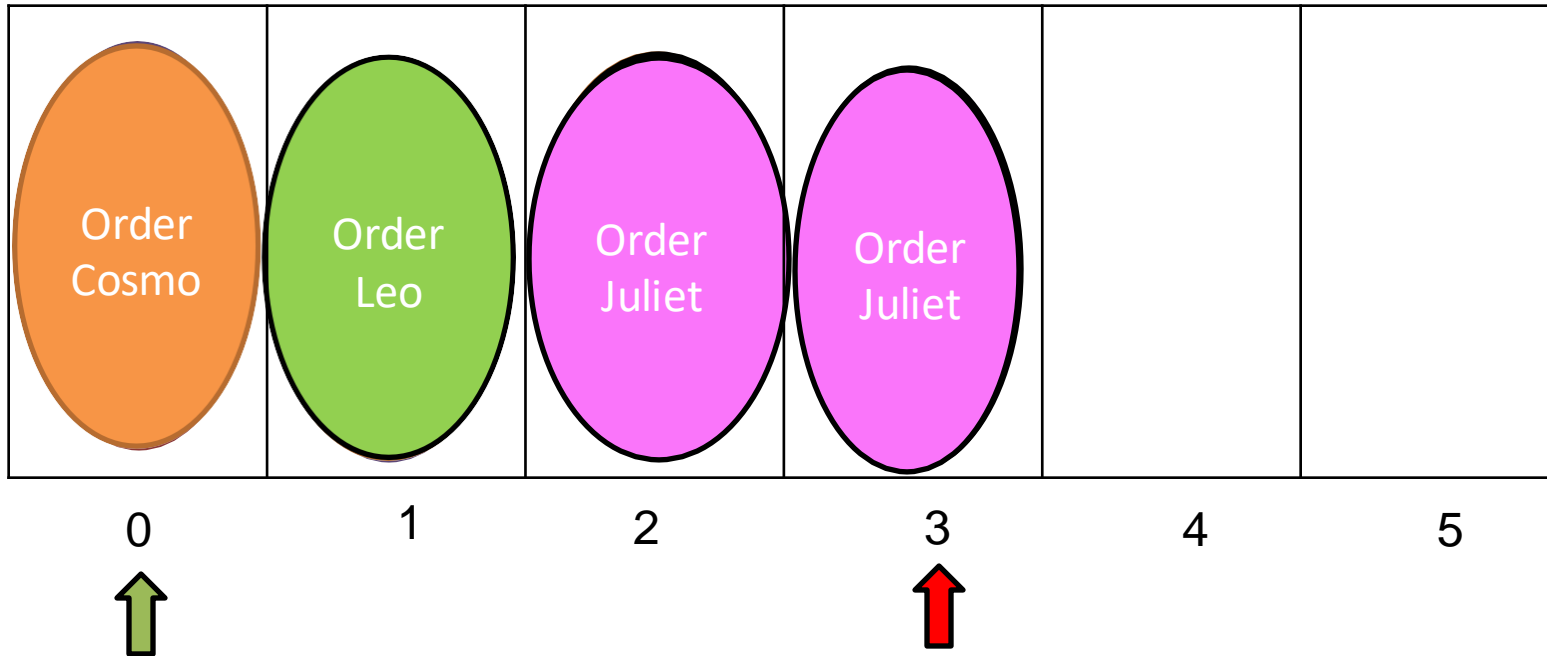
```
public Order dequeue() {  
    if (size == 0) {  
        System.out.println("Empty");  
        return null;  
    }  
  
    Order temp = data[0];  
  
    for (int i = 0; i < size - 1; i++) {  
        data[i] = data[i + 1];  
    }  
  
    data[size-1] = null;  
    size--;  
  
    return temp;  
}
```



capacity = 6 front = 0
size = 4 rear = 3

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Suppose that we have a queue that can hold 6 elements

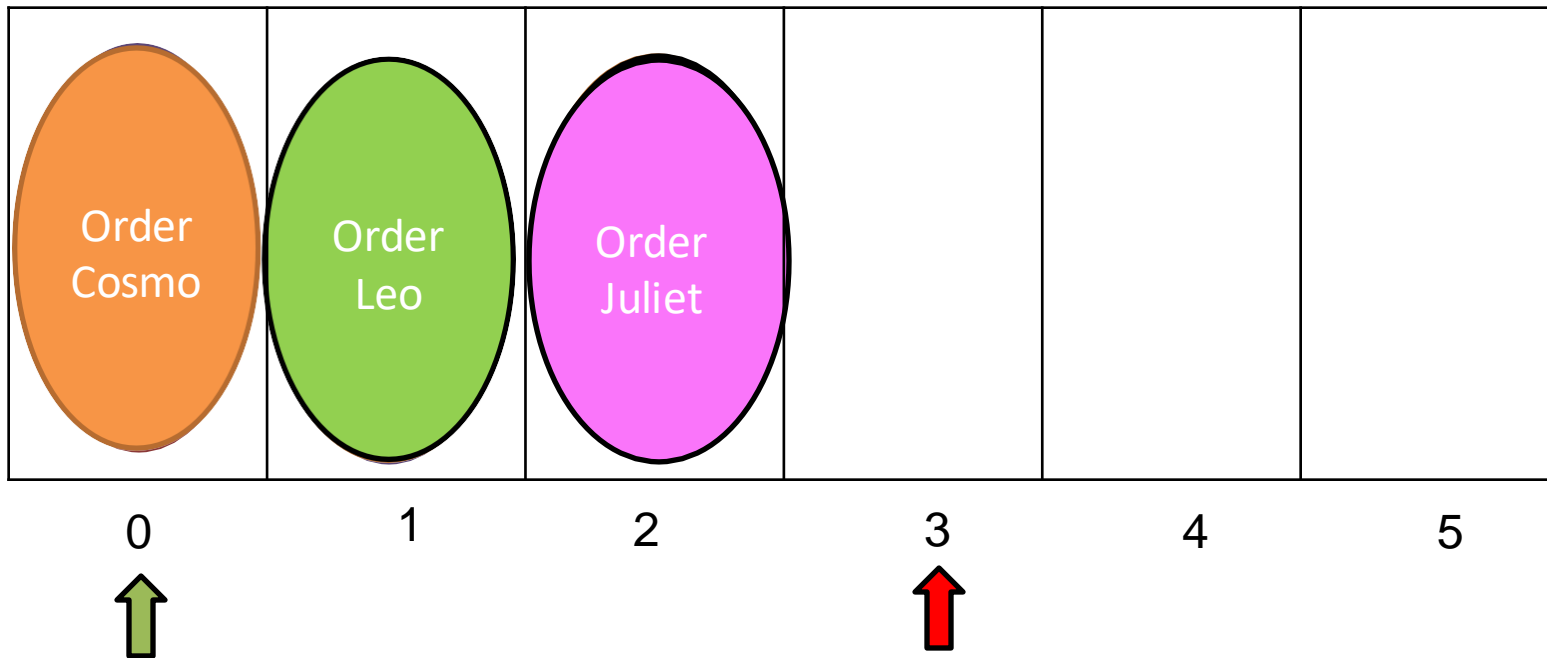


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    }  
  
    data[size-1] = null;  
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Suppose that we have a queue that can hold 6 elements

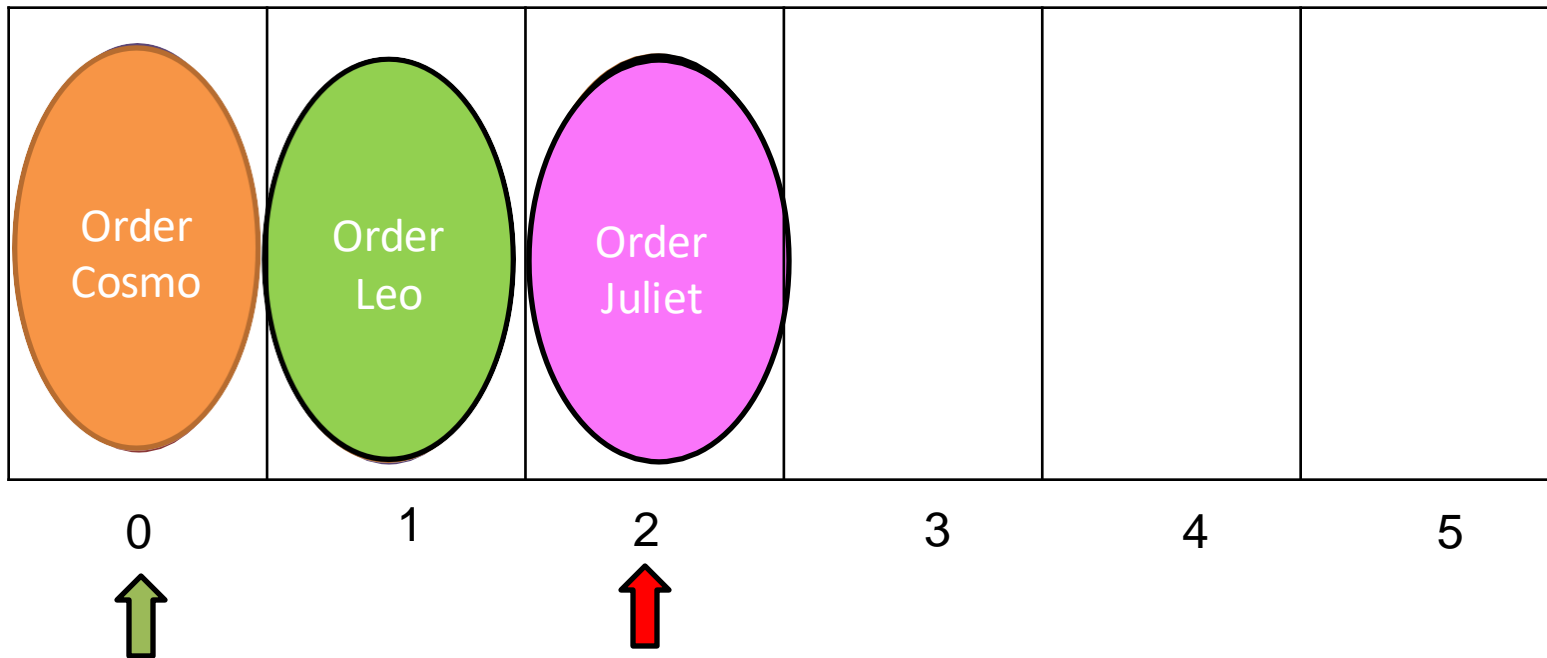


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        return null;  
    }  
  
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    }  
  
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    size--;  
  
    return temp;  
}
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capacity = 6 front = 0
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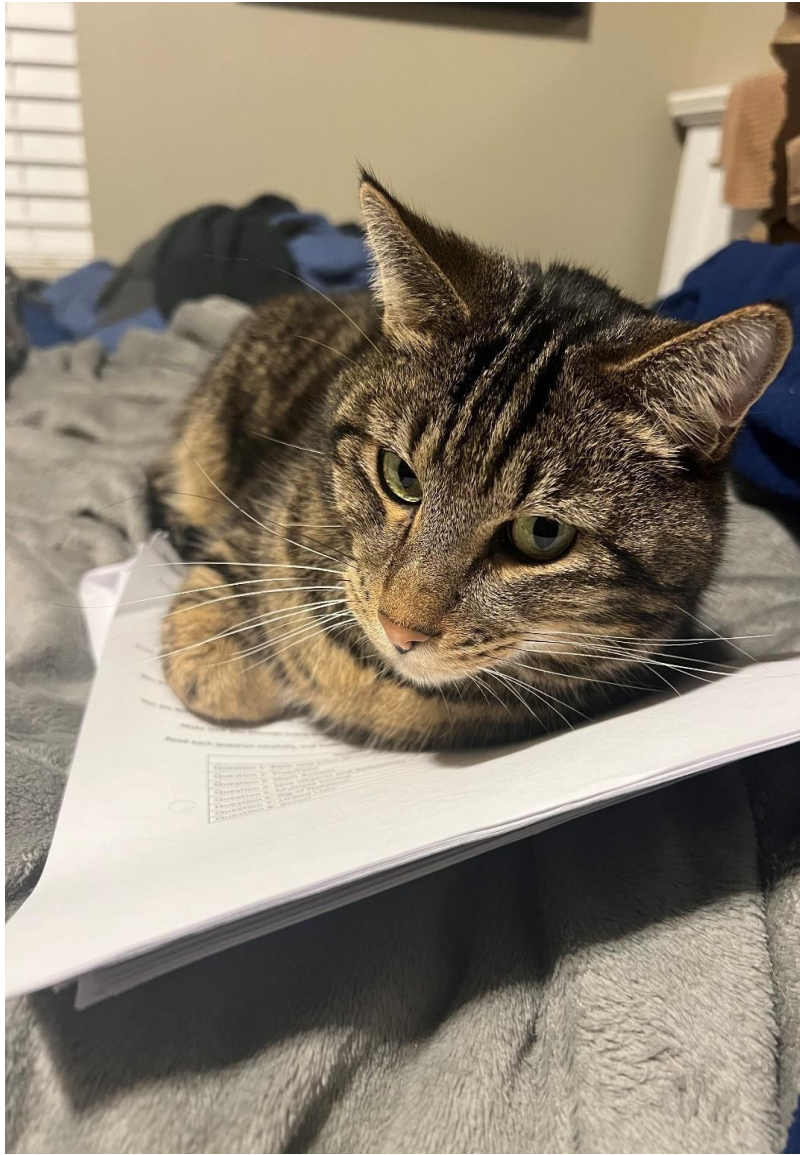
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    if (size == 0) {  
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        return null;  
    }  
  
    Order temp = data[0];  
  
    for (int i = 0; i < size - 1; i++) {  
        data[i] = data[i + 1];  
    }  
  
    data[size-1] = null;  
    size--;  
  
    return temp;  
}
```

capacity = 6 front = 0
size = 3 rear = 2



Runtime Analysis: Enqueue

```
public void enqueue(Order newOrder) {  
    if (size == capacity) {  
        System.out.println("Queue is full");  
        return;  
    }  
    data[size] = newOrder;  
    size ++;  
}
```

Runtime Analysis: Enqueue

```
public void enqueue(Order newOrder) {  
    if (size == capacity) { $O(1)$   
        System.out.println("Queue is full");  $O(1)$   
        return;  $O(1)$   
    }  
    data[size] = newOrder;  $O(1)$   
    size++;  $O(1)$ 
```

Runtime Analysis: Enqueue

```
public void enqueue(Order newOrder) {  
    if (size == capacity) { $O(1)$   
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        return;  $O(1)$   
    }  
    data[size] = newOrder;  $O(1)$   
    size++;  $O(1)$ 
```

**Total running time:
 $O(1)$**

Runtime Analysis: Dequeue

```
public Order dequeue() {  
    if (size == 0) {  
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        data[i] = data[i + 1];  
    }  
    data[size-1] = null;  
    size--;  
    return temp;  
}
```


Runtime Analysis: Dequeue

```
public Order dequeue() {  
    if (size == 0) { $O(1)$   
        System.out.println("Empty");  $O(1)$   
        return null;  $O(1)$   
    }  
    Order temp = data[0];  $O(1)$   
    for (int i = 0; i < size - 1; i++) { $O(N-1)$   
        data[i] = data[i + 1];  $O(1)$   
    }  
    data[size-1] = null;  $O(1)$   
    size--;  $O(1)$   
    return temp;  $O(1)$   
}
```

N = # elements
in our queue

Runtime Analysis: Dequeue

```
public Order dequeue() {  
    if (size == 0) {o(1)  
        System.out.println("Empty"); o(1)  
        return null; o(1)  
    }  
    Order temp = data[0]; o(1)  
    for (int i = 0; i < size - 1; i++) {o(N-1)  
        data[i] = data[i + 1]; o(1)  
    }  
    data[size-1] = null; o(1)  
    size--; o(1)  
    return temp; o(1)  
}
```

N = # elements
in our queue

**Total running time:
O(N)**

Runtime Analysis: Dequeue

Total running time:
 $O(N)$

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public Order dequeue() {  
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    }  
    Order temp = data[0];  $O(1)$   
    for (int i = 0; i < size - 1; i++) { $O(N-1)$   
        data[i] = data[i + 1];  $O(1)$   
    }  
    data[size-1] = null;  $O(1)$   
    size--;  $O(1)$   
    return temp;  $O(1)$   
}
```

This algorithm works fine, but the issue is that shifting data can be costly

(think about if this queue has 1,000,000 things in it → we must shift 999,999 elements!)

Runtime Analysis: Dequeue

Total running time:
 $O(N)$

```
public Order dequeue() {  
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        data[i] = data[i + 1];  $O(1)$   
    }  
    data[size-1] = null;  $O(1)$   
    size--;  $O(1)$   
    return temp;  $O(1)$   
}
```

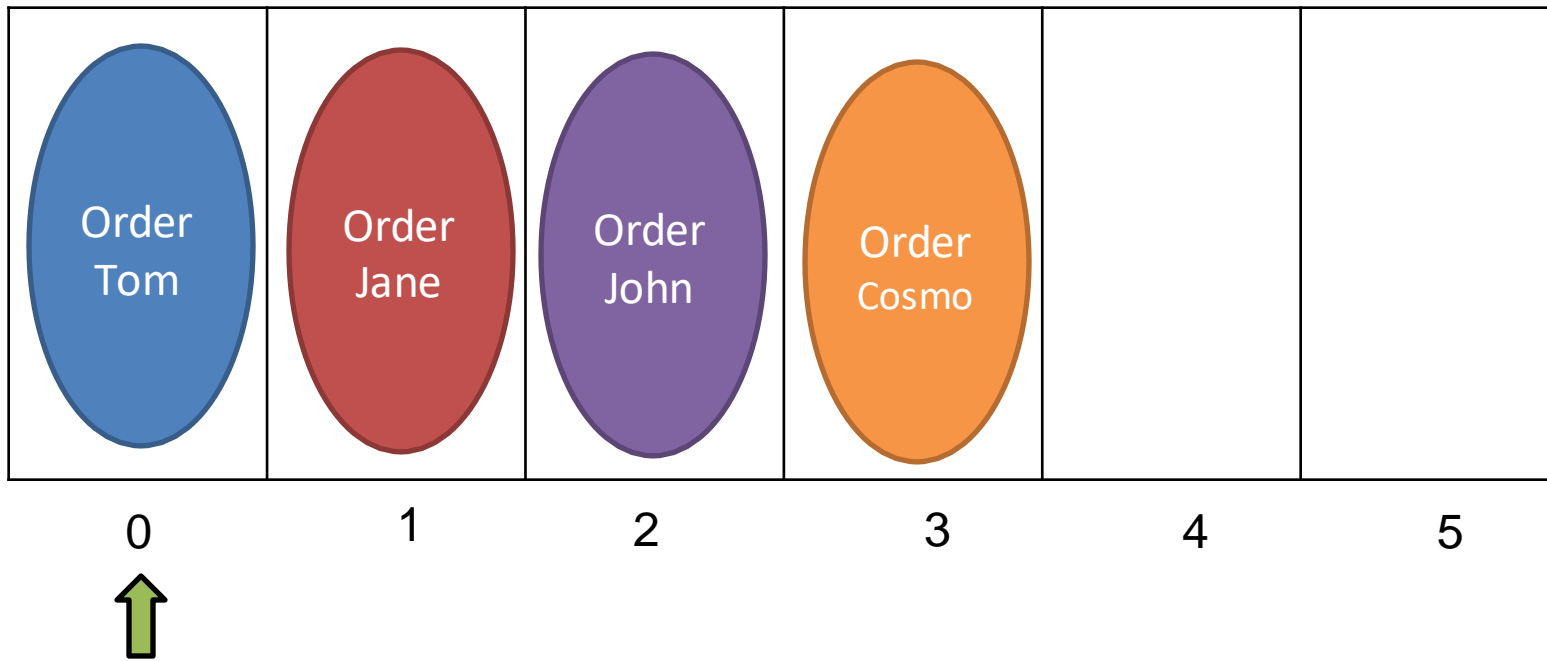
This algorithm works fine, but the issue is that shifting data can be costly

(think about if this queue has 1,000,000 things in it→ we must shift 999,999 elements!)

We prefer: Constant Time $O(1)$ > Linear Time $O(N)$

How to improve our queue?

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion



We are going to make use of the **modulus** (%) operator !

$$10 \% 6 = 4$$

$$3 \% 6 = 3$$

$$6 \% 6 = 0$$

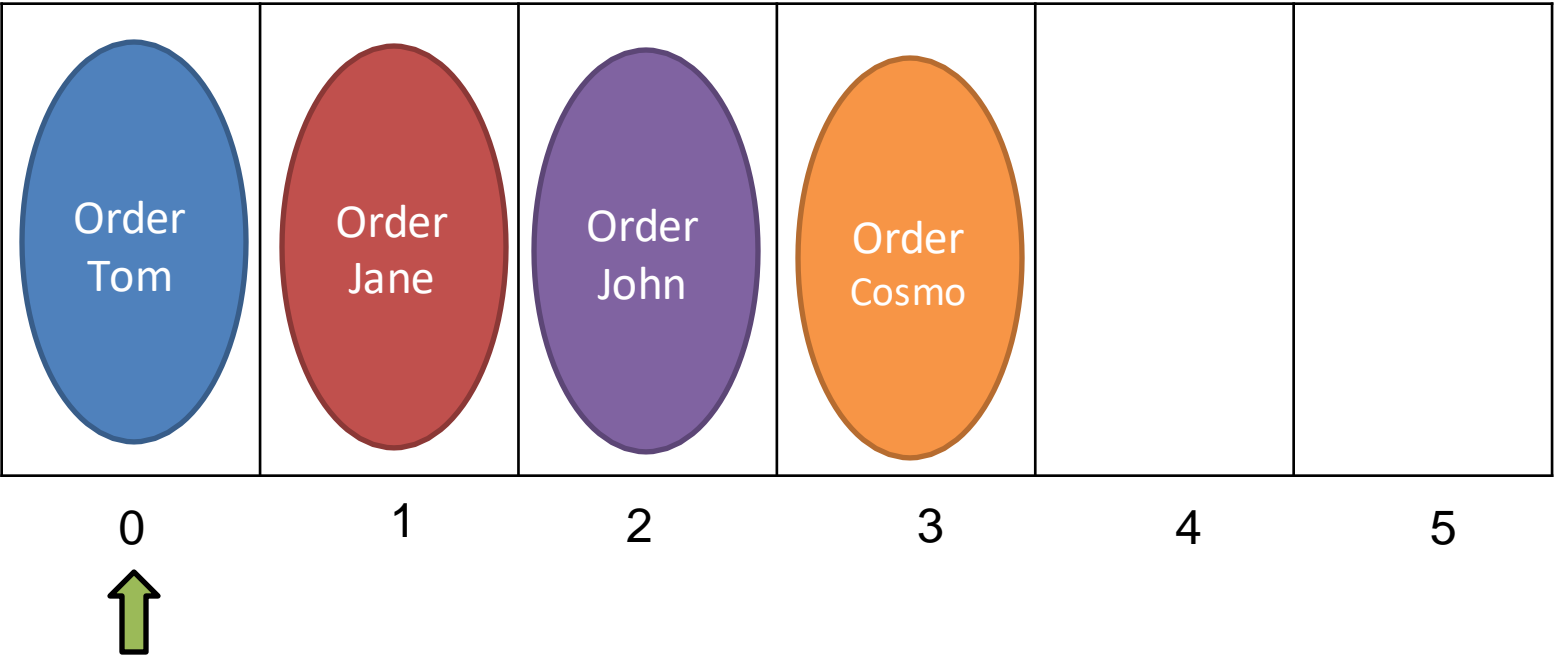
capacity = 6 front = 0
size = 4

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's enqueue

Here is the formula for determining where to insert the new element

$$\text{insert_spot} = (\text{front} + \text{size}) \% 6$$



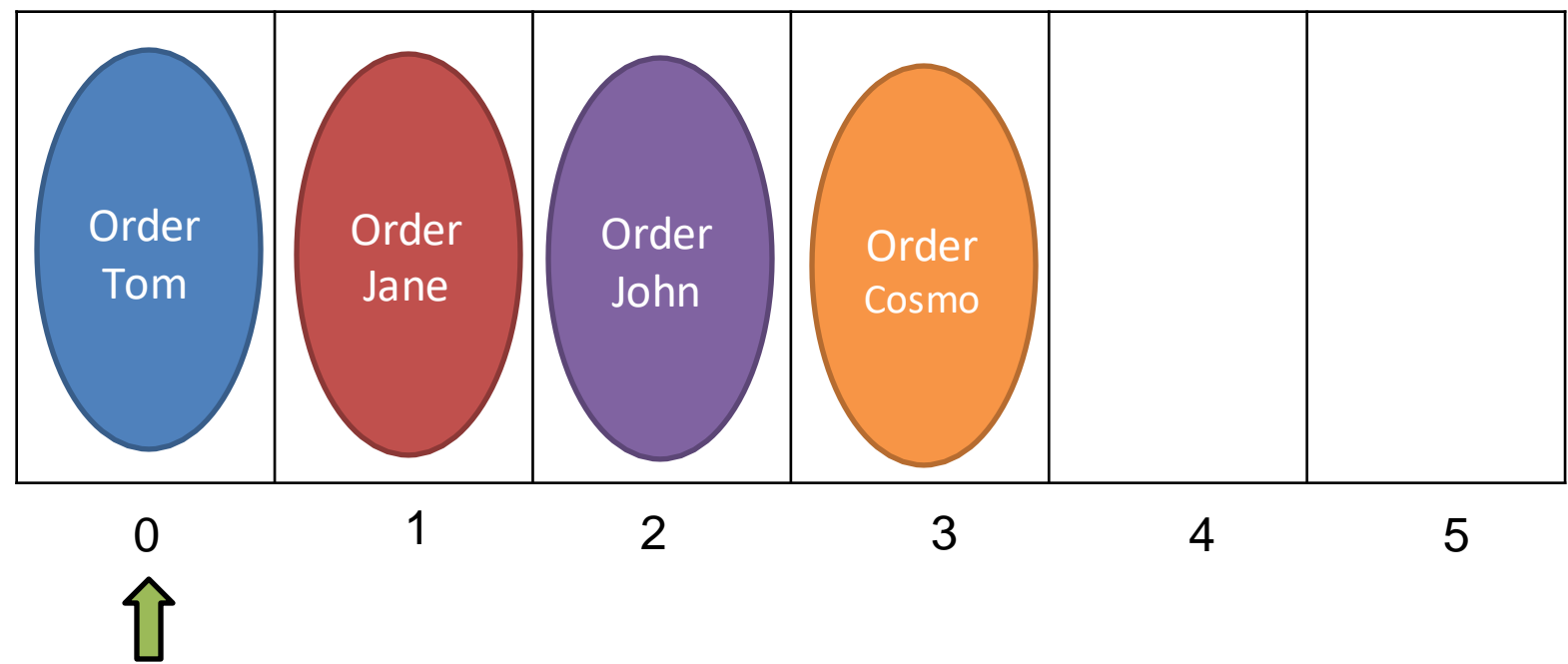
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Let's **enqueue**

Here is the formula for determining where to insert the new element

$$\text{insert_spot} = (\text{front} + \text{size}) \% 6$$



$(0 + 4) \% 6 = \text{Insert at spot 4}$

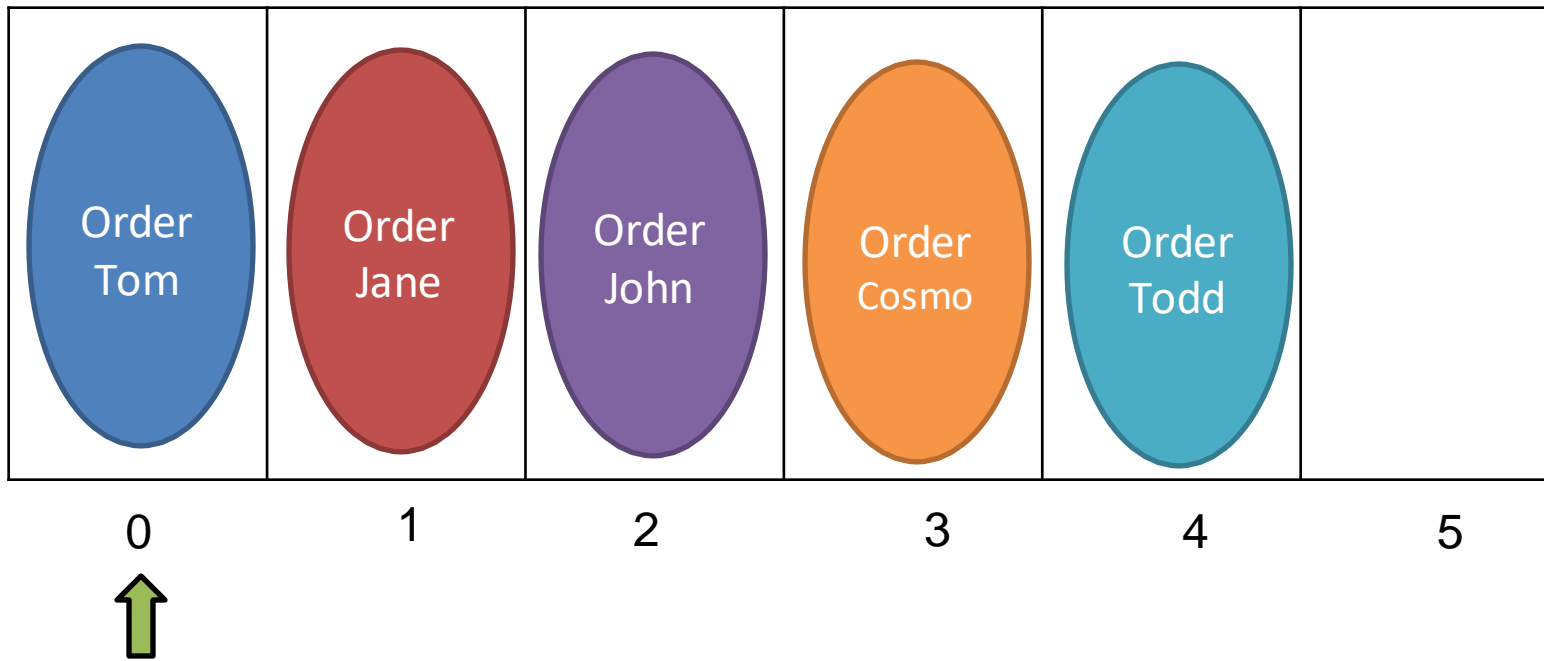
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size = 4 insert_spot = 4

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$$\text{insert_spot} = (\text{front} + \text{size}) \% 6$$



capacity = 6

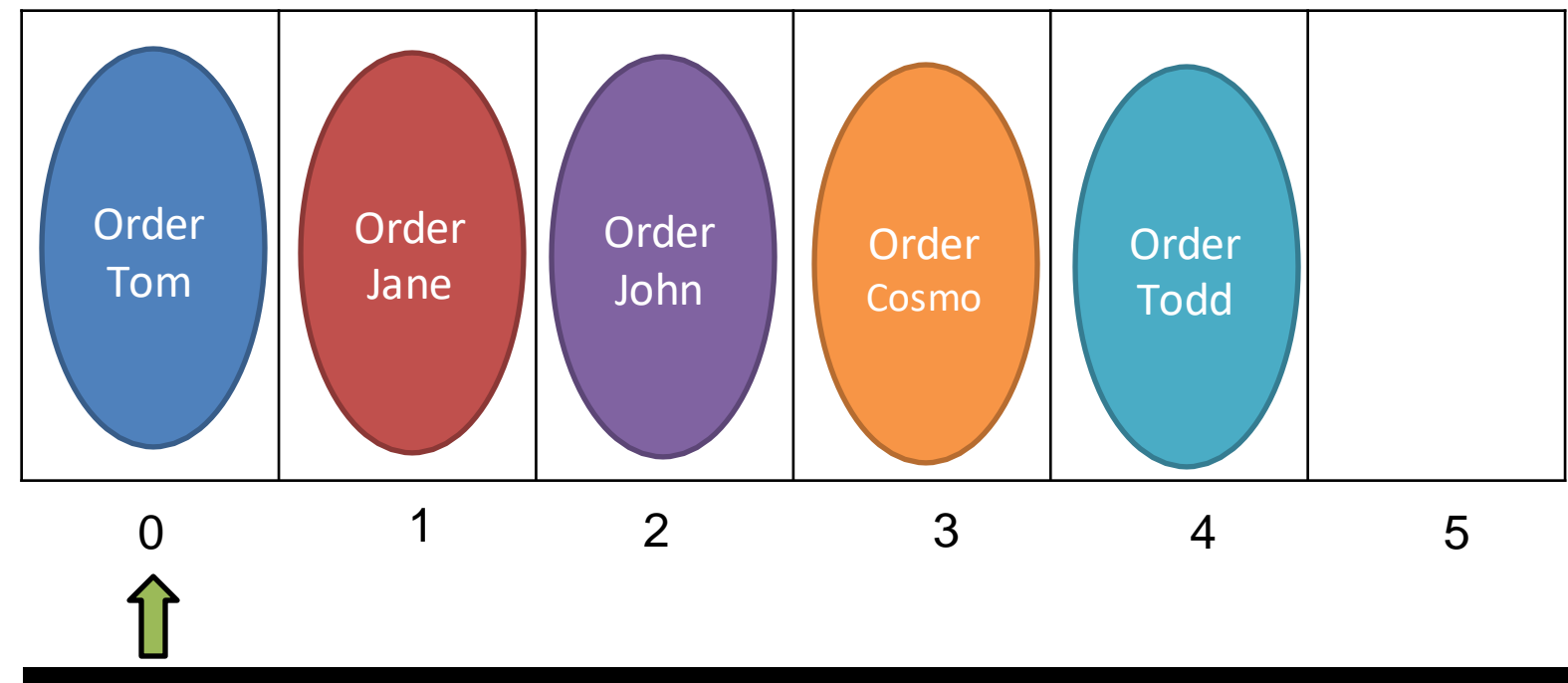
front = 0

size = 4

insert_spot = 4

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's **dequeue**

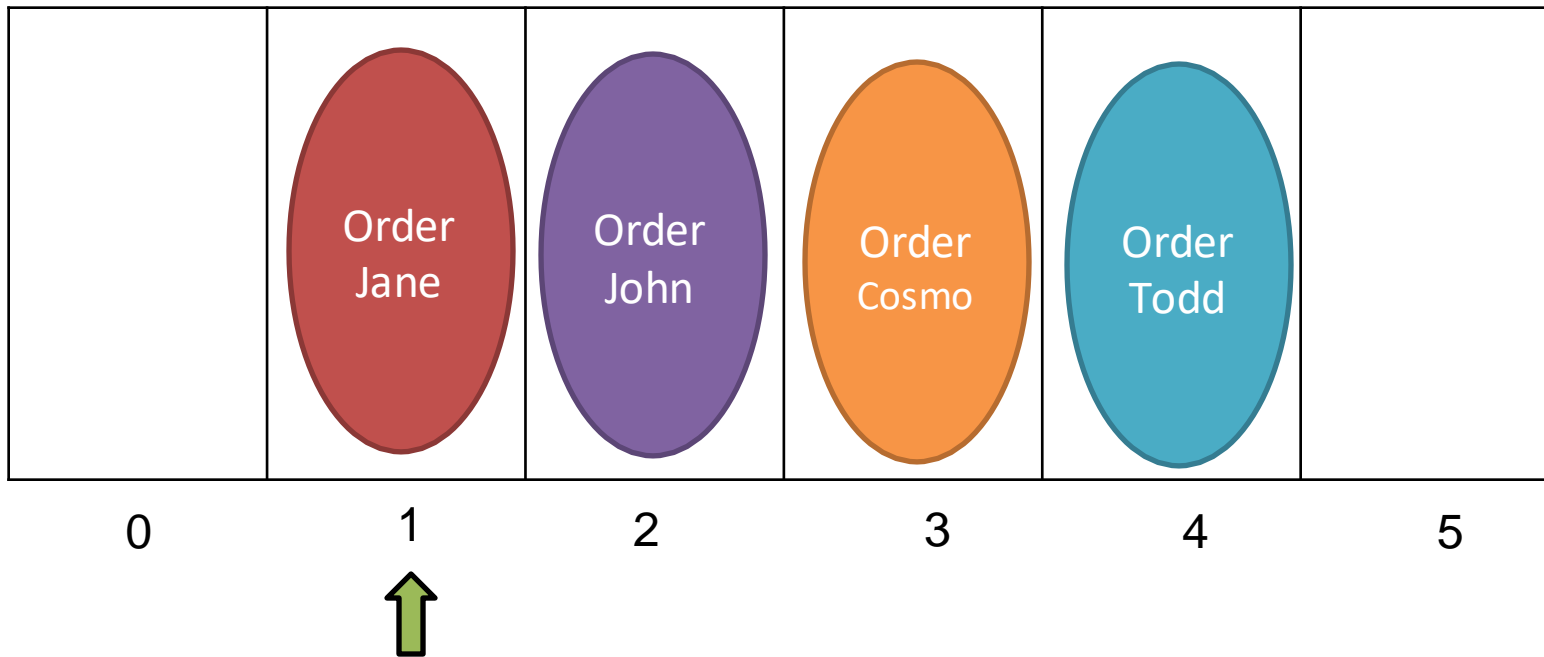


```
data[front] = null
```

capacity = 6 front = 0
size = 4 insert_spot = 4

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's **dequeue**



```
data[front] = null
```

```
front = (front + 1) % 6
```

move the front pointer to the next element
 $= (0 + 1) \% 6 = 1$

```
capacity = 6
```

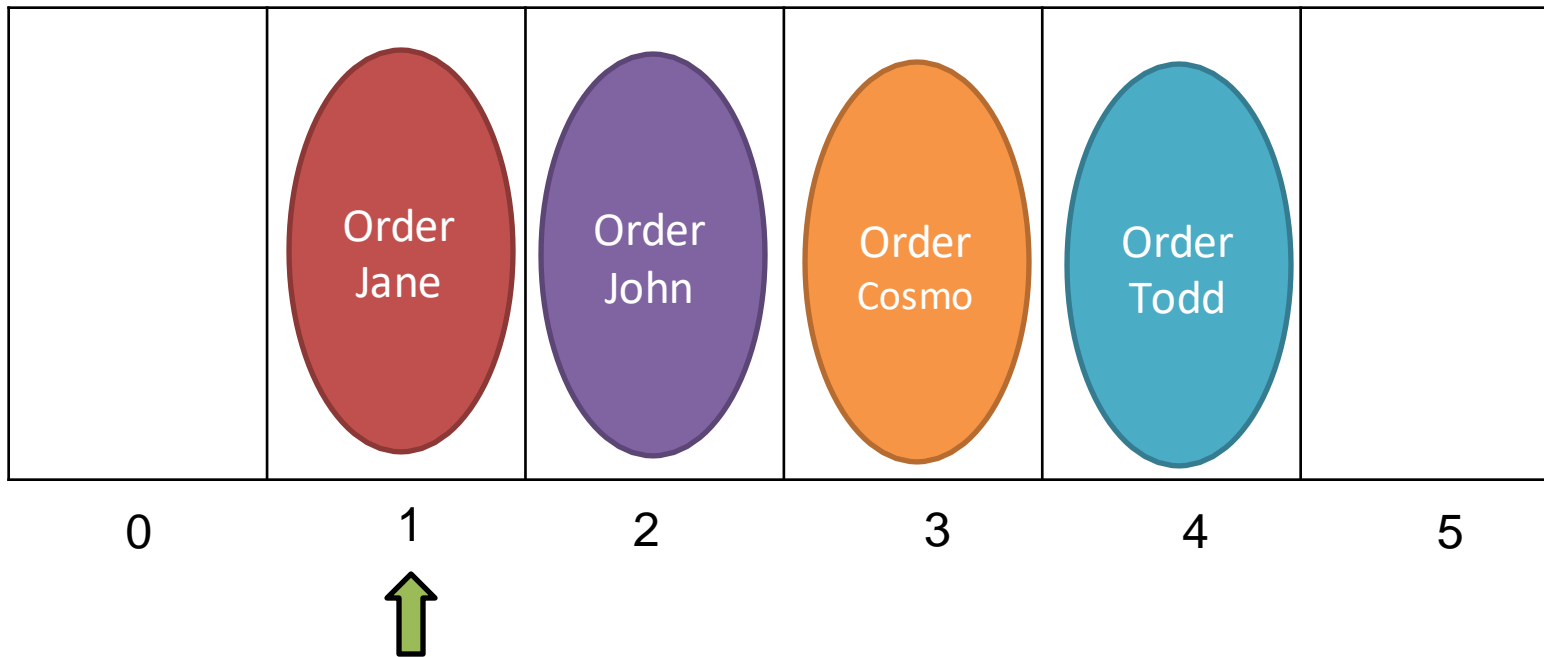
```
front = 1
```

```
size = 4
```

```
insert_spot = 4
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's **dequeue** (again)



```
data[front] = null
```

```
front = (front + 1) % 6
```

move the front pointer to the next element
 $= (0 + 1) \% 6 = 1$

```
capacity = 6
```

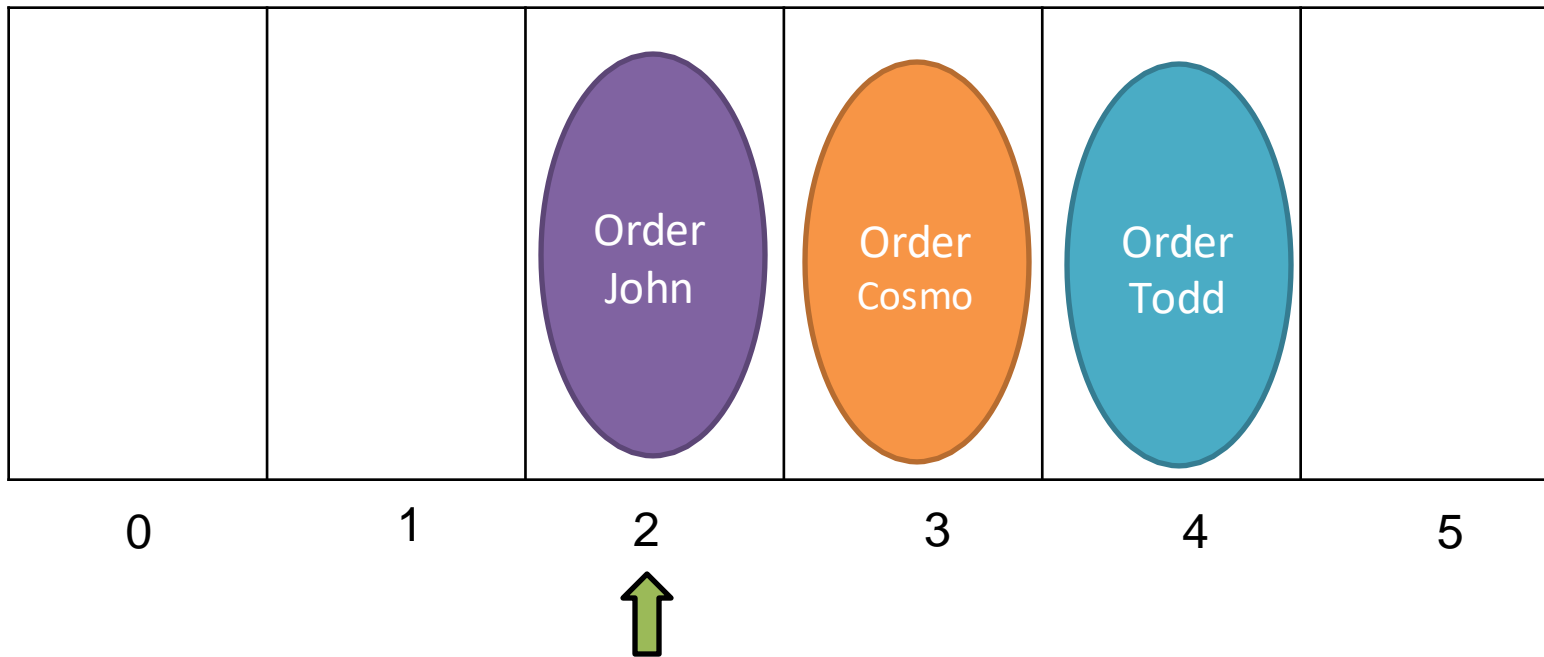
```
front = 1
```

```
size = 4
```

```
insert_spot = 4
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's **dequeue** (again)



```
data[front] = null
```

```
front = (front + 1) % 6
```

move the front pointer to the next element
 $= (1 + 1) \% 6 = 2$

```
capacity = 6
```

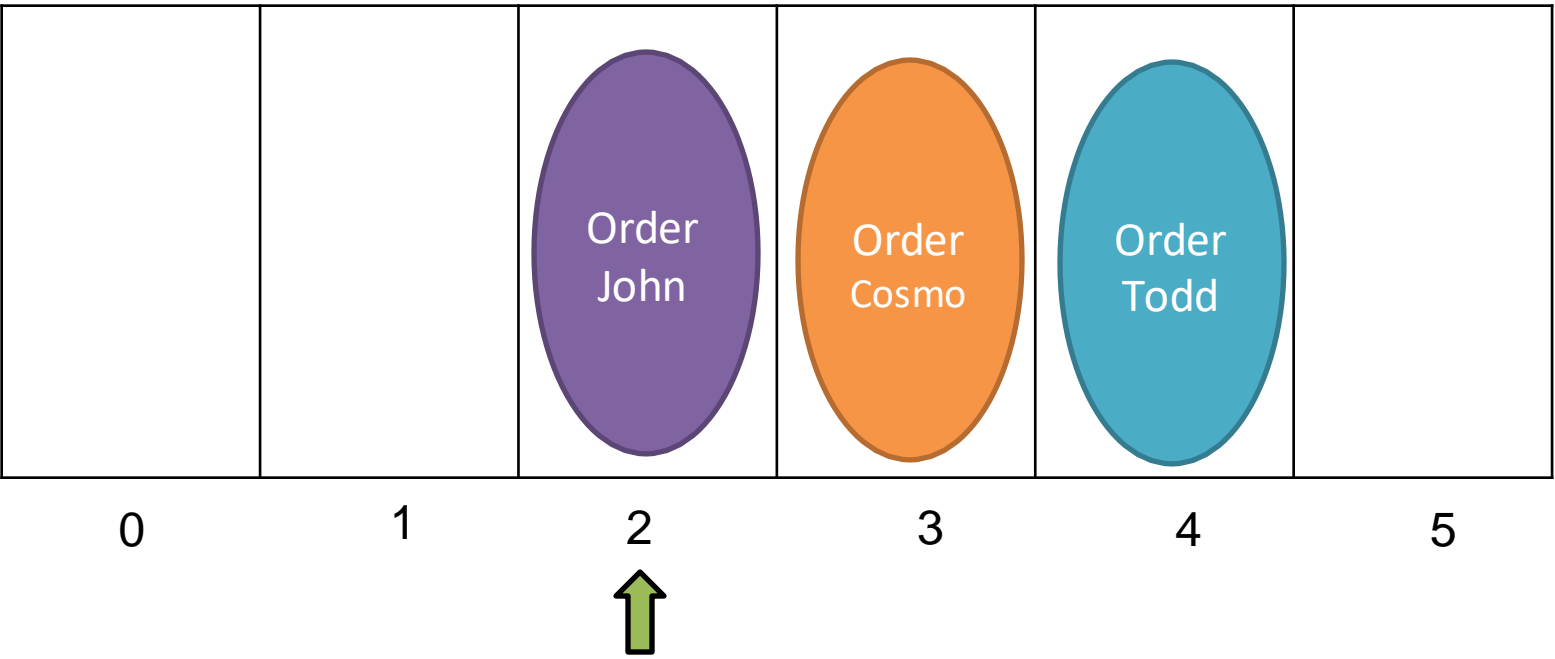
```
front = 2
```

```
size = 3
```

```
insert_spot = 4
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's enqueue (again)



$insert_spot = (front + size) \% 6$

$insert_spot = (2 + 3) \% 6$

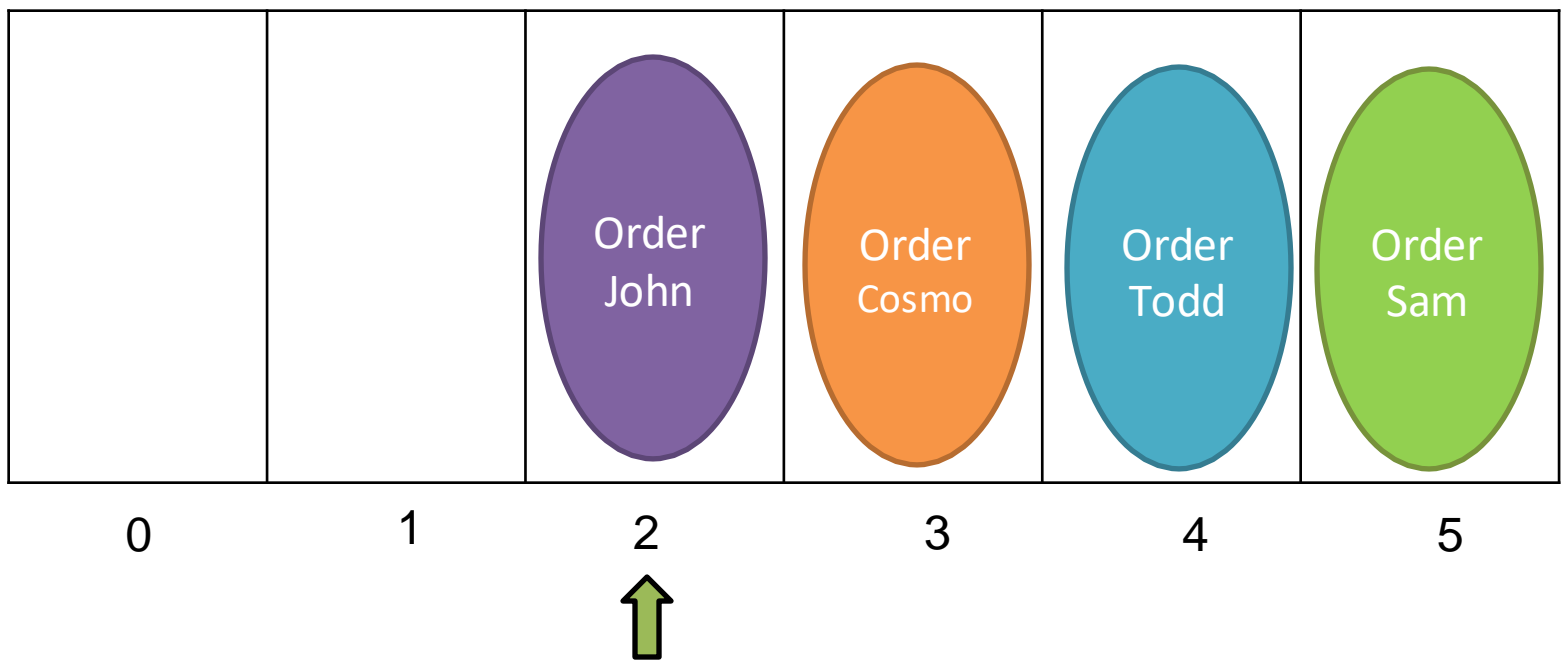


$5 \% 6 = 5$

capacity = 6 front = 2
size = 3 insert_spot = 5

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's enqueue (again)



$$\text{insert_spot} = (\text{front} + \text{size}) \% 6$$

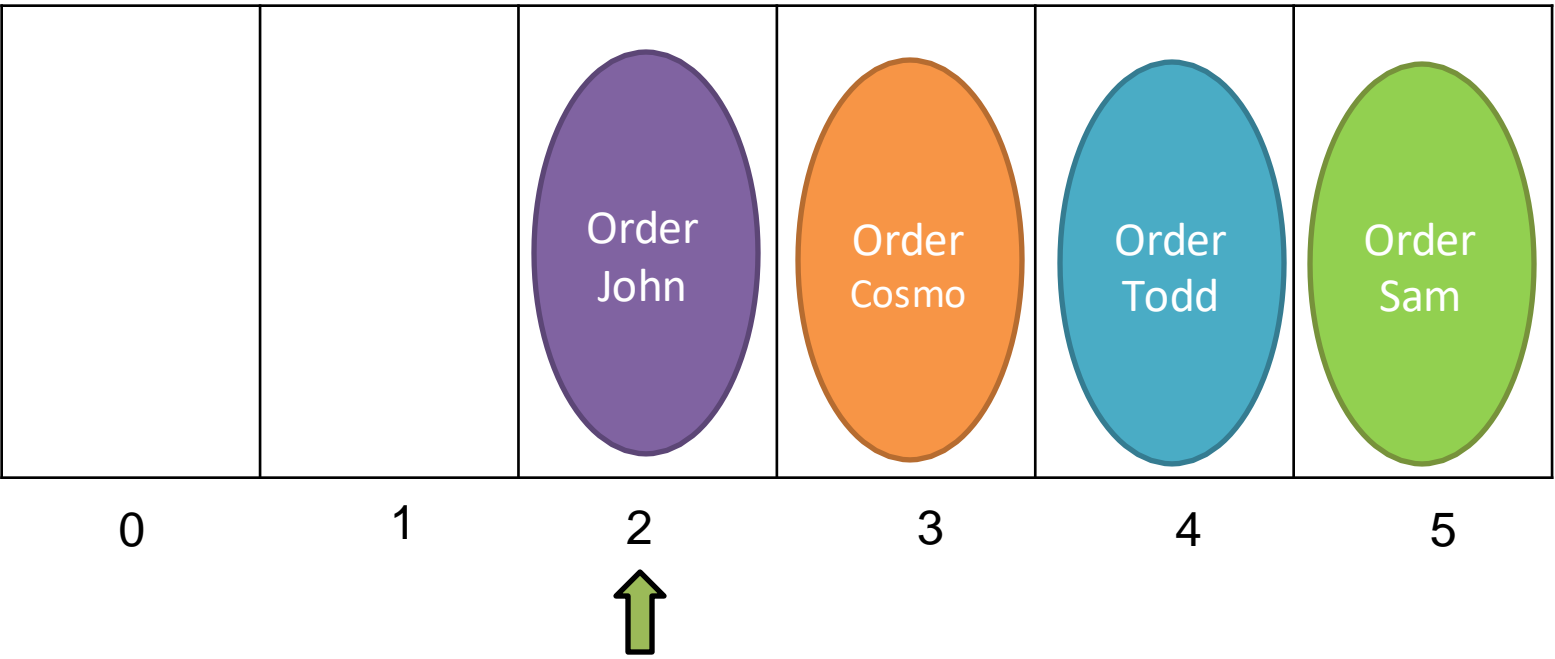
$$\text{insert_spot} = (2 + 3) \% 6$$

$$5 \% 6 = 5$$

capacity = 6 front = 2
size = 4 insert_spot = 5

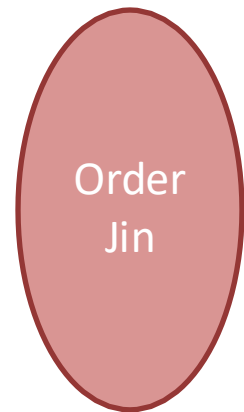
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Let's enqueue (again)



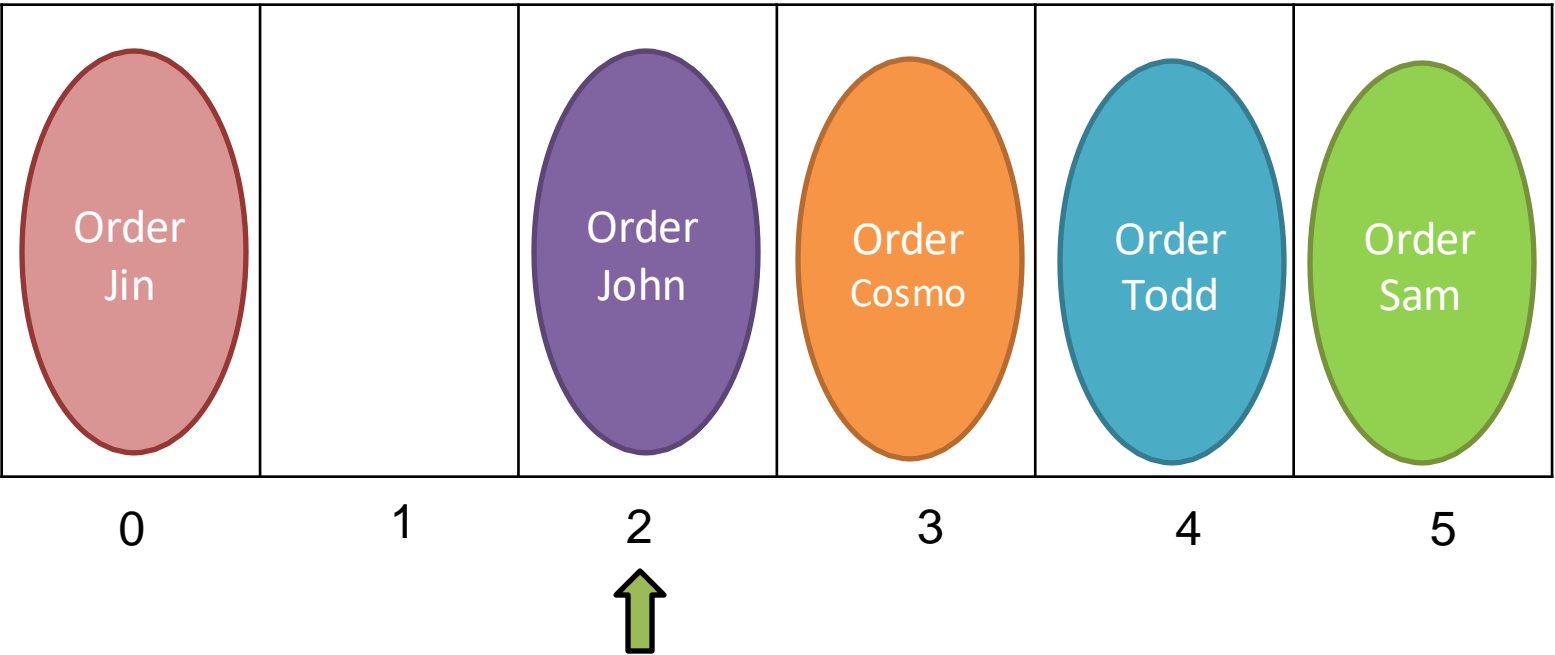
$$\text{insert_spot} = (\text{front} + \text{size}) \% 6$$
$$(2 + 4) \% 6 = 0$$

capacity = 6 front = 2
size = 4 insert_spot = 0



A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

Let's enqueue (again)

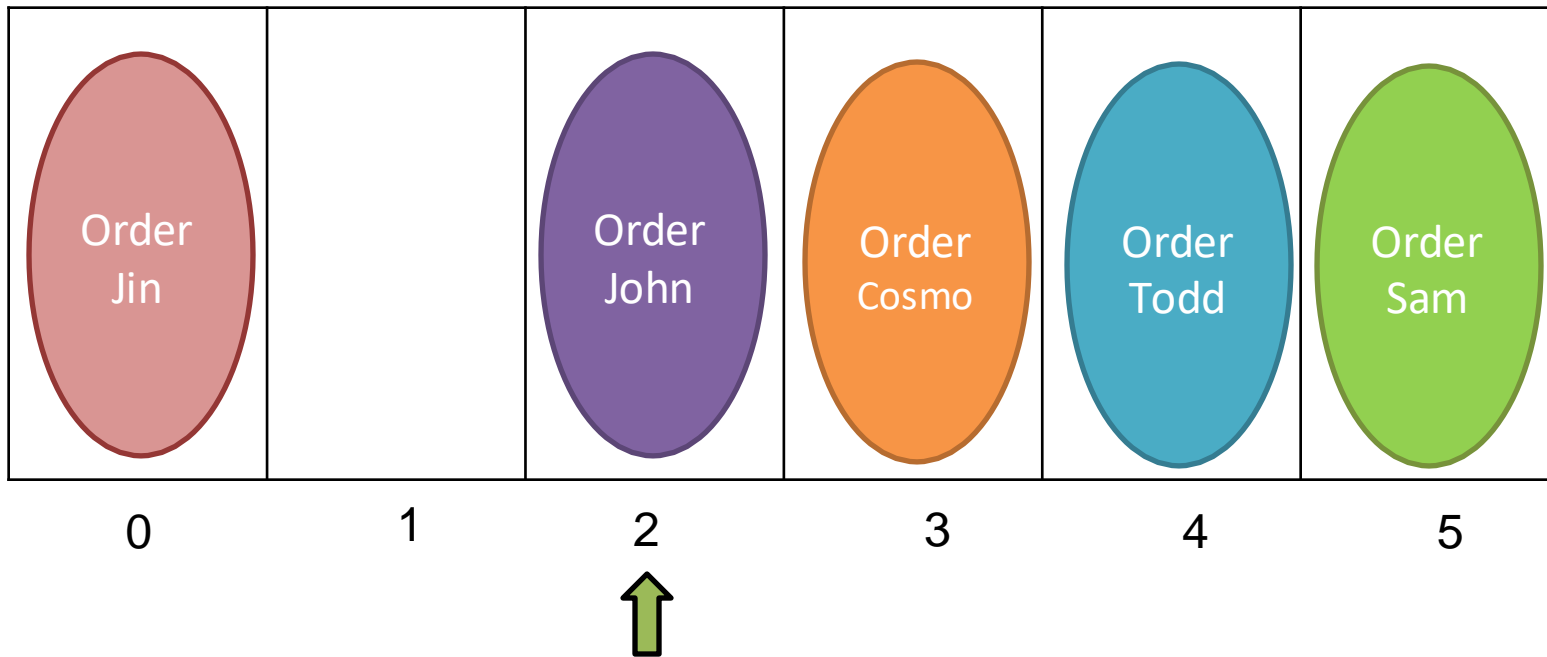


$$\text{insert_spot} = (\text{front} + \text{size}) \% 6$$
$$(2 + 4) \% 6 = 0$$

The modulus operator allows us to “**wrap around**” in our array!

capacity = 6 front = 2
size = 4 insert_spot = 0

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion



Let's **dequeue** (again)

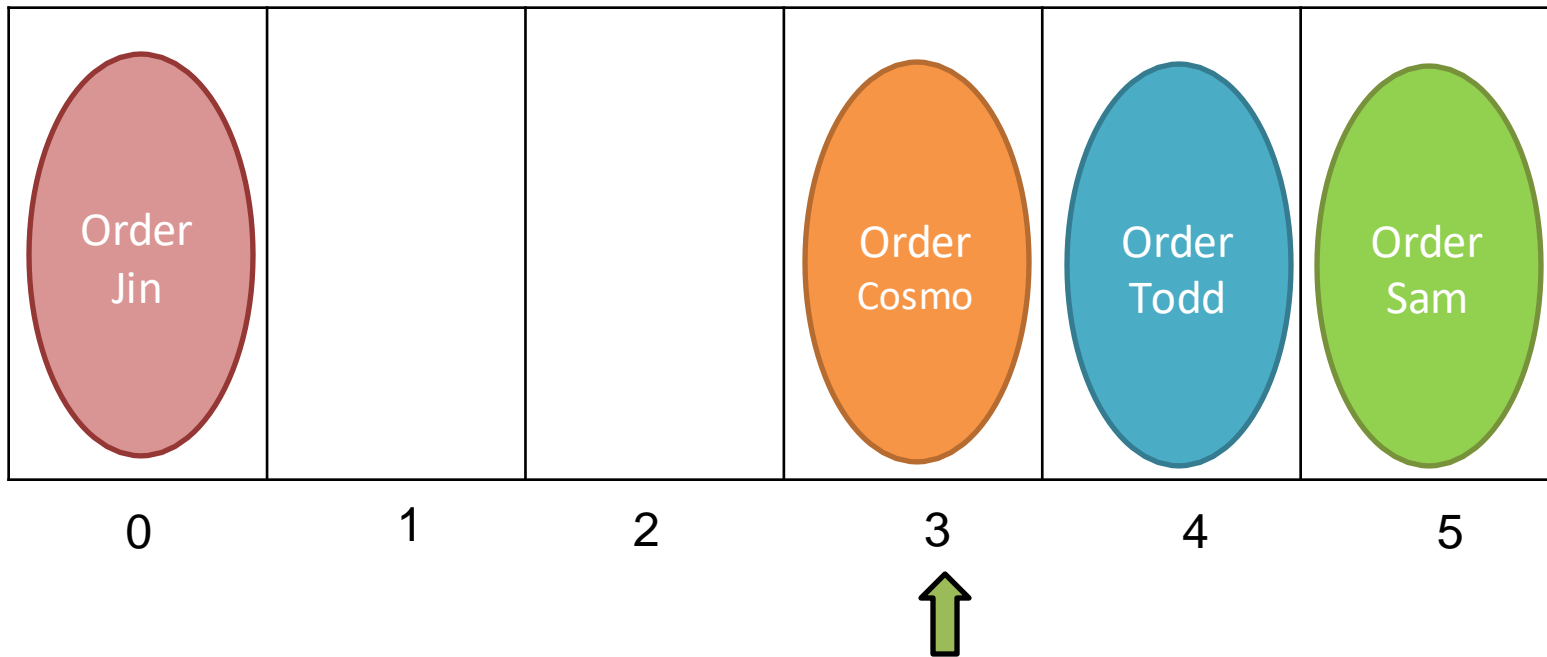
```
data[front] = null
```

```
front = (front + 1) % 6
```

The modulus operator allows us to “**wrap around**” in our array!

```
capacity = 6    front = 2  
size = 4        insert_spot = 0
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion



Let's **dequeue** (again)

```
data[front] = null
```

```
front = (front + 1) % 6
```

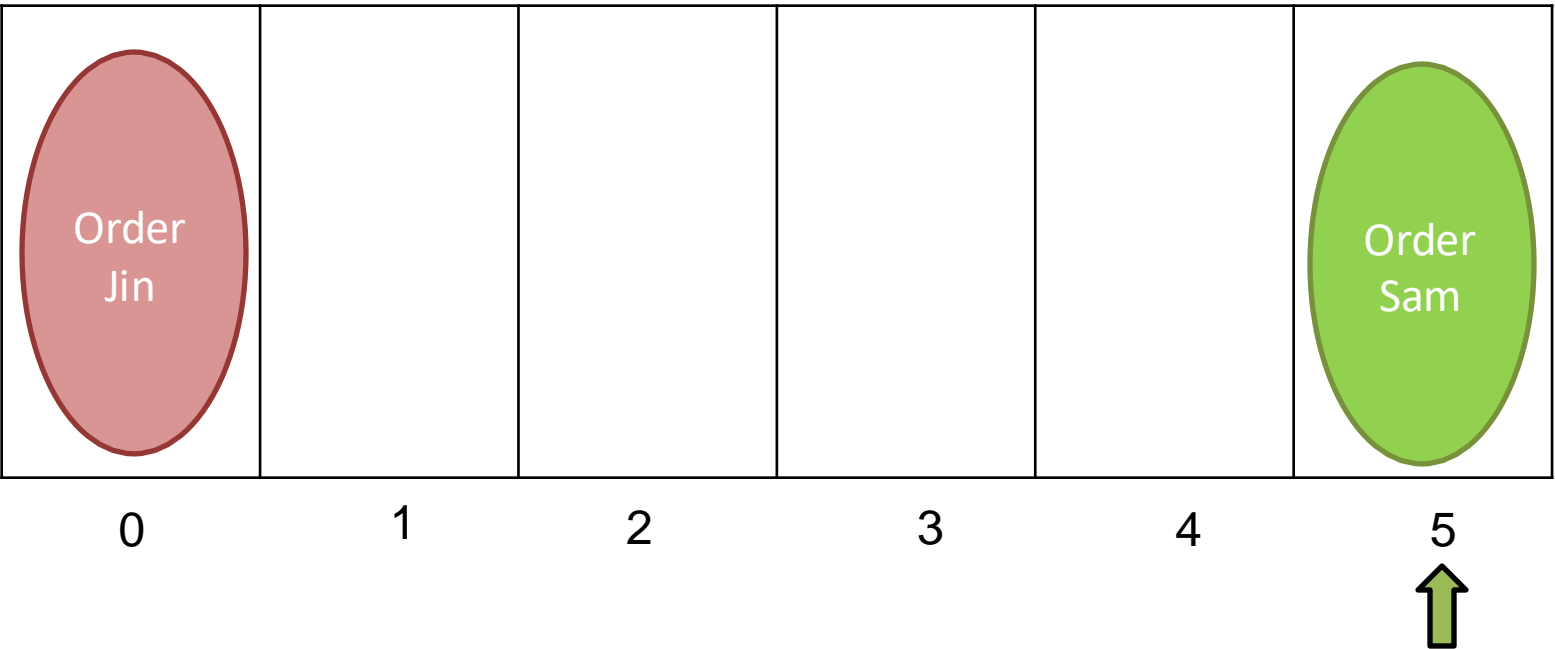
$(2+1) \% 6 = 3$

The modulus operator allows us to “**wrap around**” in our array!

```
capacity = 6    front = 3  
size = 4        insert_spot = 0
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion

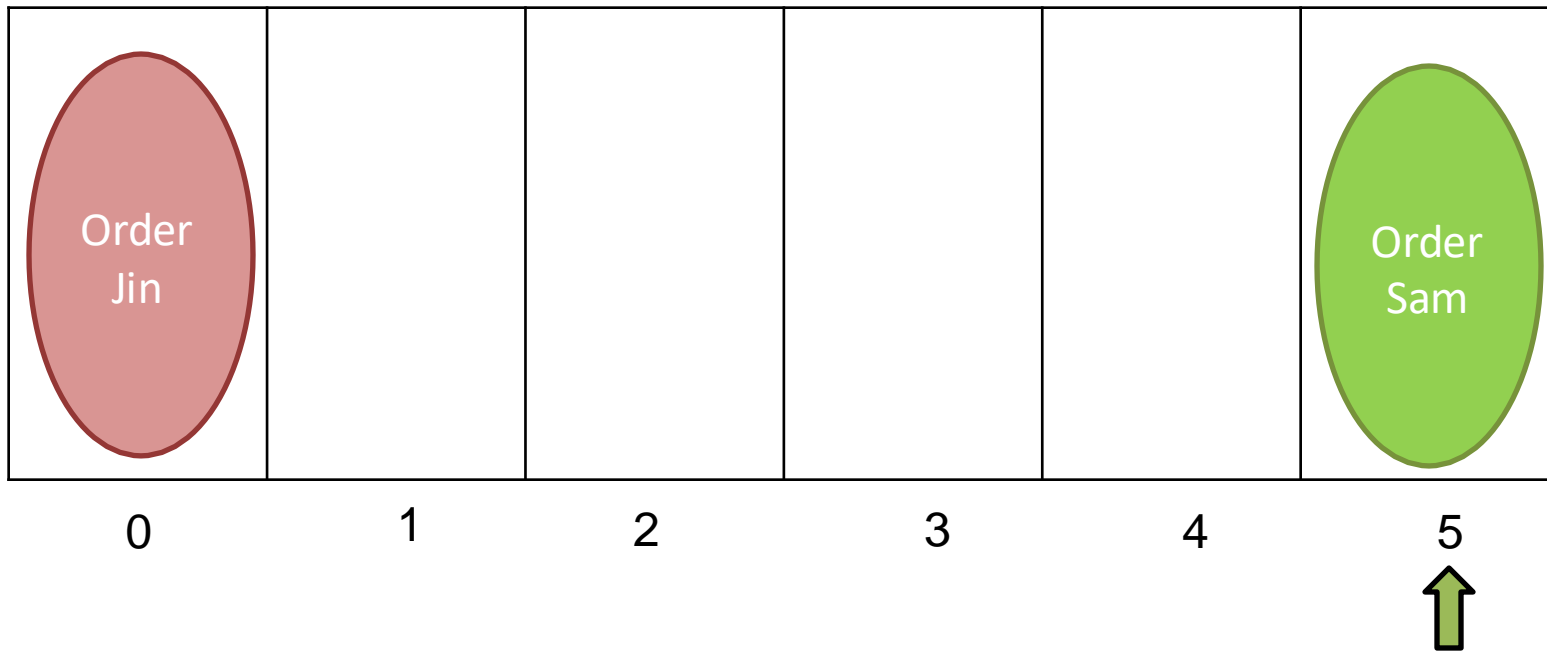
Let's **dequeue** (again)



```
data[front] = null  
front = (front + 1) % 6
```

```
capacity = 6    front = 5  
size = 2        insert_spot = 0
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion



Let's **dequeue** (again)

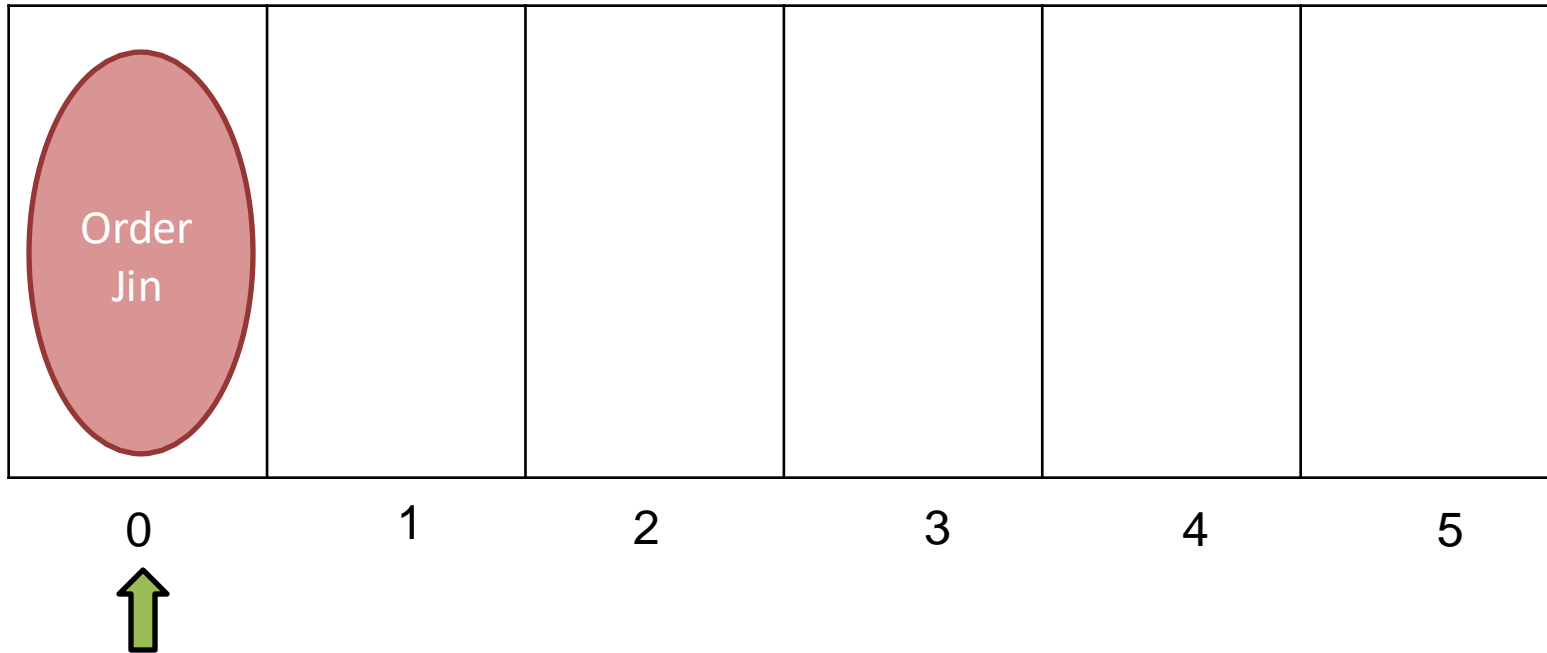
```
data[front] = null
```

```
front = (front + 1) % 6
```

Front = (5 + 1) % 6 = 0

```
capacity = 6    front = 5  
size = 2       insert_spot = 0
```

A **Queue** is a data structure that holds data, but operates in a First-in First-out (**FIFO**) fashion



Let's **dequeue** (again)

```
data[front] = null
```

```
front = (front + 1) % 6
```

Front = (5 + 1) % 6 = 0

```
capacity = 6    front = 0  
size = 1       insert_spot = 0
```

```
public void enqueue(Order newOrder) {  
    if (size == capacity) {  
        System.out.println("Queue is full");  
        return;  
    }  
    else {  
        int insert_spot = (front + size) % capacity;  
        data[insert_spot] = newOrder;  
        size++;  
        System.out.println("Added " + newOrder.getName() + " at index #" + insert_spot + "\n");  
    }  
}
```

```
public Order dequeue() {  
    if (size == 0) {  
        System.out.println("Queue is empty");  
        return null;  
    }  
    Order temp = data[front];  
  
    data[front] = null;  
    front = (front + 1) % capacity;  
    size--;  
  
    return temp;  
}
```

Queue Runtime Analysis

```
public QueueLinkedList() {  
    this.orders = new LinkedList<Order>();  
    this.size = 0;  
}
```

```
public QueueArray2() {  
    this.orders = new Order[6];  
    this.size = 0;  
    this.front = 0;  
    this.capacity = this.orders.length; //6  
}
```

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue		
Dequeue		
Peek		
Print Queue		

Queue Runtime Analysis

```
public QueueLinkedList() {  
    this.orders = new LinkedList<Order>();  
    this.size = 0;  
}
```

$O(1)$

```
public QueueArray2() {  
    this.orders = new Order[6];  
    this.size = 0;  
    this.front = 0;  
    this.capacity = this.orders.length; //6  
}
```

$O(n)$, $n = | \text{array} |$

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue		
Dequeue		
Peek		
Print Queue		

Queue Runtime Analysis

```
public void enqueue(Order newOrder) {  
  
    this.orders.addLast(newOrder);  
    this.size++;  
  
}
```

```
public void enqueue(Order newOrder) {  
  
    if(this.size == this.capacity) {  
        System.out.println("Error... queue is full");  
        return;  
    }  
  
    int insert_spot = (front + size) % capacity;  
    this.orders[insert_spot] = newOrder;  
  
    this.size++;  
    System.out.println("Added " + newOrder.getName() + " at index #" + insert_spot);  
}
```

	Linked List	Array
Creation	O(1)	O(n)
Enqueue		
Dequeue		
Peek		
Print Queue		

Queue Runtime Analysis

```
public void enqueue(Order newOrder) {  
    this.orders.addLast(newOrder);  $O(1)$   
    this.size++;  $O(1)$   
}
```

```
public void enqueue(Order newOrder) {  
    if(this.size == this.capacity) {  
        System.out.println("Error... queue is full");  $O(1)$   
        return;  
    }  
  
    int insert_spot = (front + size) % capacity;  $O(1)$   
    this.orders[insert_spot] = newOrder;  $O(1)$   
  
    this.size++;  $O(1)$   
    System.out.println("Added " + newOrder.getName() + " at index #" + insert_spot);  $O(1)$   
}
```

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue	$O(1)$	$O(1)$
Dequeue		
Peek		
Print Queue		

Queue Runtime Analysis

```
public Order dequeue() {  
    if(this.size != 0) {  
        Order removed = this.orders.removeFirst();  
        System.out.println(removed.getName() + "'s order  
size--;  
return removed;  
    }  
    else {  
        return null;  
    }  
}
```

```
public void dequeue() {  
    if(this.size == 0) {  
        System.out.println("Error... queue is empty");  
        return;  
    }  
    else {  
        Order o = this.orders[front];  
        this.orders[front] = null;  
        front = (front + 1) % capacity;  
        this.size--;  
        System.out.println(o.getName() + "'s order was removed");  
    }  
}
```

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue	$O(1)$	$O(1)$
Dequeue		
Peek		
Print Queue		

Queue Runtime Analysis

```
public Order dequeue() {  
    if(this.size != 0) {  
        Order removed = this.orders.removeFirst();  
        O(1) System.out.println(removed.getName() + "'s order  
        size--;  
        return removed;  
    }  
    else {  
        return null; O(1)  
    }  
}
```

```
public void dequeue() {  
    if(this.size == 0) {  
        System.out.println("Error... queue is empty"); O(1)  
        return;  
    }  
    else {  
        Order o = this.orders[front];  
        this.orders[front] = null;  
        front = (front + 1) % capacity; O(1)  
        this.size--;  
        System.out.println(o.getName() + "'s order was removed");  
    }  
}
```

	Linked List	Array
Creation	O(1)	O(n)
Enqueue	O(1)	O(1)
Dequeue	O(1)	O(1)
Peek		
Print Queue		

Queue Runtime Analysis

```
return this.orders.getFirst()
```

```
return this.orders[front]
```

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue	$O(1)$	$O(1)$
Dequeue	$O(1)$	$O(1)$
Peek		
Print Queue		

Queue Runtime Analysis

`return this.orders.getFirst()` **O(1)**

`return this.orders[front]` **O(1)**

	Linked List	Array
Creation	O(1)	O(n)
Enqueue	O(1)	O(1)
Dequeue	O(1)	O(1)
Peek	O(1)	O(1)
Print Queue		

Queue Runtime Analysis

```
public void printQueue() {  
    int counter = 1;  
    for(Order each_order: this.orders) {  
        each_order.printOrder(counter);  
        counter++;  
    }  
}
```

```
public void printQueue() {  
  
    int start = front;  
    int counter = 1;  
    int n = 0;  
    while(n != this.size) {  
        System.out.println(counter + ". " + this.orders[start].getName());  
        start = (start + 1) % capacity;  
        counter++;  
        n++;  
    }  
}
```

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue	$O(1)$	$O(1)$
Dequeue	$O(1)$	$O(1)$
Peek	$O(1)$	$O(1)$
Print Queue		

Queue Runtime Analysis

```
public void printQueue() {  
    int counter = 1; O(1)  
    for(Order each_order: this.orders) {O(n)  
        O(1) each_order.printOrder(counter);  
        O(1) counter++;  
    }  
}
```

n = # of elements in queue

```
public void printQueue() {  
    int start = front; O(1)  
    int counter = 1; O(1)  
    int n = 0; O(1)  
    while(n != this.size) { O(n)  
        System.out.println(counter + ". " + this.orders[start].getName());  
        O(1) start = (start + 1) % capacity;  
        counter++;  
        n++;  
    }  
}
```

n = # of elements in queue

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue	$O(1)$	$O(1)$
Dequeue	$O(1)$	$O(1)$
Peek	$O(1)$	$O(1)$
Print Queue	$O(n)$	$O(n)$

Takeaway: Adding and removing elements from a **queue** runs in constant time ($O(1)$)

(FIFO)

Takeaway: Adding and removing elements from a **stack** runs in constant time ($O(1)$)

(LIFO)

Queue Runtime Analysis

	Linked List	Array
Creation	$O(1)$	$O(n)$
Enqueue	$O(1)$	$O(1)$
Dequeue	$O(1)$	$O(1)$
Peek	$O(1)$	$O(1)$
Print Queue	$O(n)$	$O(n)$

Stack Runtime Analysis

	Linked List	Array
Creation	$O(1)$	$O(n)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$