

CSCI 132:

Basic Data Structures and Algorithms

Recursion (Part 3)

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Fall 2024

Announcements

Lab 10 posted

Program 4 due Nov. 15th



Permutations

Calculation of the number of ways a particular *set* can be arranged

$${}_nP_r = \frac{n!}{(n - r)!}$$

${}_nP_r$ = permutation

n = total number of objects

r = number of objects selected

Permutations

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Set: a collection of distinct unordered items

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Set: a collection of *distinct* unordered items

Ex:

{1, 2, 3, 4}

{‘H’, ‘I’}

{A, B, C, D}

{“I”, “L”, “A”, “N”}

{1.4, 3.6, 9.5}

{“R”, “E”, “S”}

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CSCI 246 Discrete Structures: 3 Credits (3 Lec)

PREREQUISITE: [M 171Q](#) or [M 165Q](#)

COREQUISITE: [CSCI 132](#). (F, Sp, Su) This course covers logic, discrete probability, recurrence relations, Boolean algebra, sets, relations, counting, functions, maps, Big-O notation, proof techniques including induction, and proof by contradiction

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Calculation of the number of ways a particular set can be arranged

Ex: “ABC”

A B C

A C B

B A C

B C A

C A B

C B A

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Calculation of the number of ways a particular set can be arranged

Ex: "ABC"

- 1 A B C
- 2 A C B
- 3 B A C
- 4 B C A
- 5 C A B
- 6 C B A

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Permutations

Calculation of the number of ways a particular set can be arranged

Ex: "ABC"

- 1 A B C
- 2 A C B
- 3 B A C
- 4 B C A
- 5 C A B
- 6 C B A

$$3! = 3 * 2 * 1 = 6$$

$${}_nP_r = \frac{n!}{(n - r)!}$$

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Permutations

Calculation of the number of ways a particular set can be arranged

Ex: “ABC” → “ABCD”

What if we add one more letter?

Permutations

What if we add one more letter?

Calculation of the number of ways a particular set can be arranged

Ex: "ABC" → "ABCD"

ABCD	BACD	CABD	DABC
ABDC	BADC	CADB	DACB
ACBD	BCAD	CBAD	DBAC
ACDB	BCDA	CBDA	DBCA
ADBC	BDAC	CDAB	DCAB
ADCB	BDCA	CDBA	DCBA

Permutations

What if we add one more letter?

Calculation of the number of ways a particular set can be arranged

Ex: “ABC” → “ABCD”

1	ABCD	7	BACD	13	CABD	19	DABC
2	ABDC	8	BADC	14	CADB	20	DACB
3	ACBD	9	BCAD	15	CBAD	21	DBAC
4	ACDB	10	BCDA	16	CBDA	22	DBCA
5	ADBC	11	BDAC	17	CDAB	23	DCAB
6	ADCB	12	BDCA	18	CDBA	24	DCBA

Permutations

What if we add one more letter?

Calculation of the number of ways a particular set can be arranged

Ex: "ABC" → "ABCD"

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2	ABDC	8	BADC	14	CADB	20	DACB
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4	ACDB	10	BCDA	16	CBDA	22	DBCA
5	ADBC	11	BDAC	17	CDAB	23	DCAB
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$$4! = 4 * 3 * 2 * 1 = 24$$

Powerball (Real)

Rules:

- select five numbers between 1 and 69 for the white balls
- select one number between 1 and 26 for the red Powerball

Match	Prize	Odds
	Grand Prize	1 in 292,201,338.00
	\$1,000,000	1 in 11,688,053.52
	\$50,000	1 in 913,129.18
	\$100	1 in 36,525.17
	\$100	1 in 14,494.11
	\$7	1 in 579.76
	\$7	1 in 701.33
	\$4	1 in 91.98
	\$4	1 in 38.32

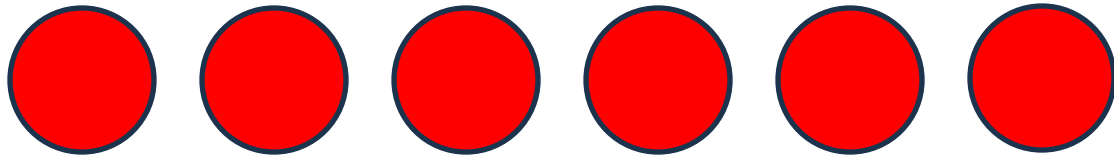
The overall odds of winning a prize are 1 in 24.87.
The odds presented here are based on a \$2 play (rounded to two decimal places).



Powerball (CSCI 132 Version)

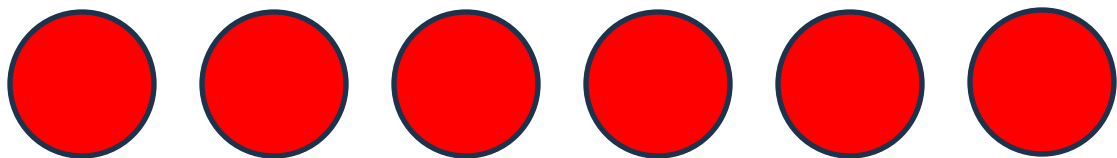
Rules:

- select 6 numbers between 1 and 6
- no repeats, numbers must appear in the correct order



Powerball (CSCI 132 Version)

- Rules:
- select 6 numbers between 1 and 6
 - no repeats, numbers must appear in the correct order



Potential winning numbers ex:

1	2	3	4	5	6
6	5	4	3	2	1

5	2	4	1	3	6
2	4	6	1	3	5

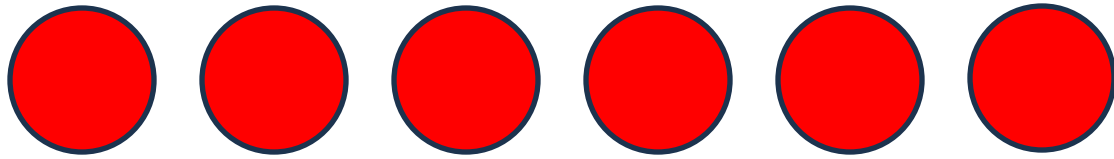


Powerball (CSCI 132 Version)

Rules:

select 6 numbers between 1 and 6

no repeats, numbers must appear in the correct order



Base case?

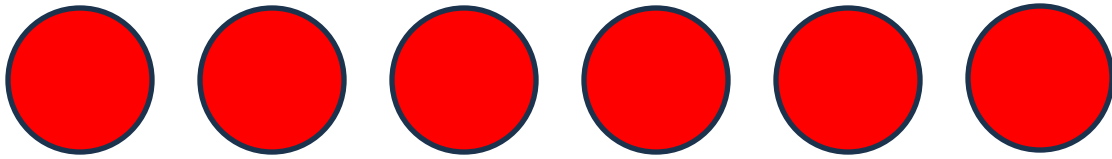
Recursive case?



Powerball (CSCI 132 Version)

Rules:

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- no repeats, numbers must appear in the correct order



Base case?

Check if the length of the current permutation matches the length of the input characters (6)

Recursive case?

Iterate through each value in our values array [1-6].

If the character is not already in the current permutation, append it and makes a recursive call to continue building the permutation

Ex: calculating permutations of “123”

Base case:

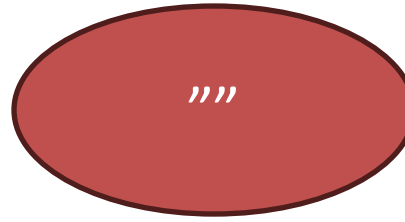
```
len("") == len("123")
```

Recursive case:

```
for chars:
```

```
    if char not in perm:  
        genPerms()
```

Ex: calculating permutations of "123"



Base case:

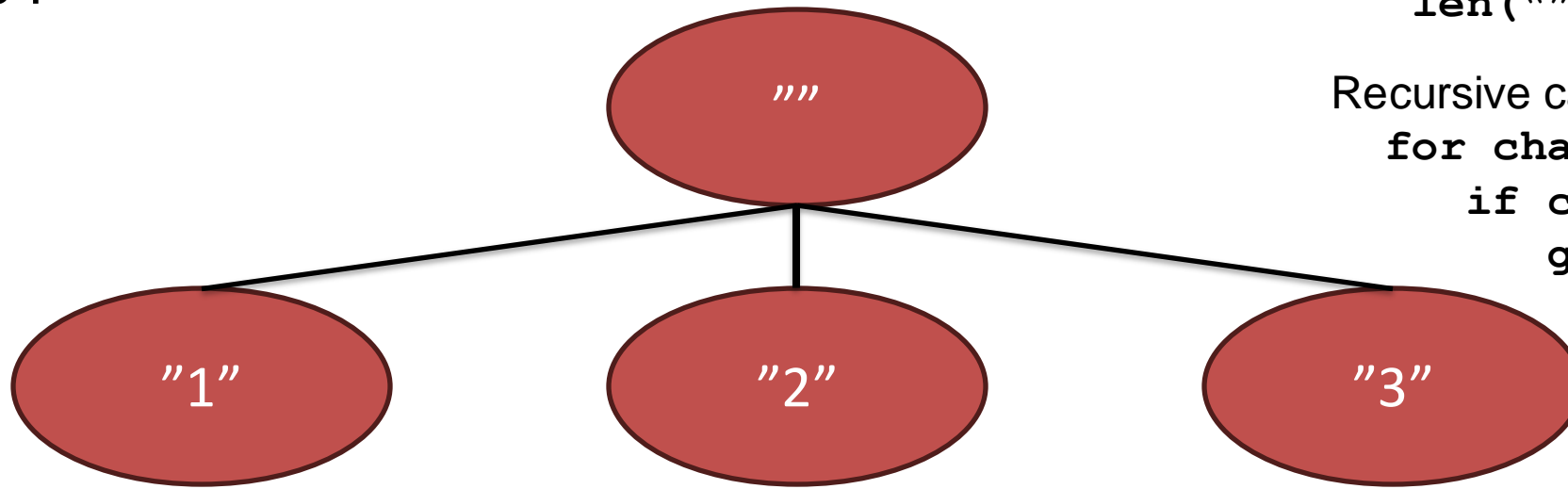
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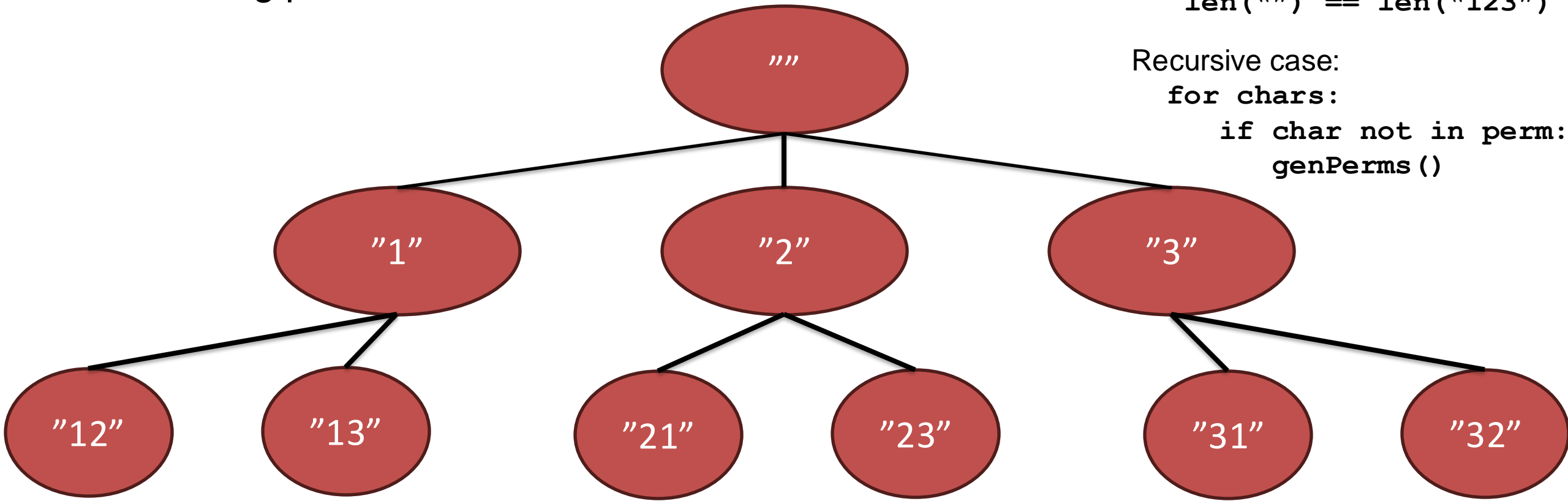
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`for chars:`
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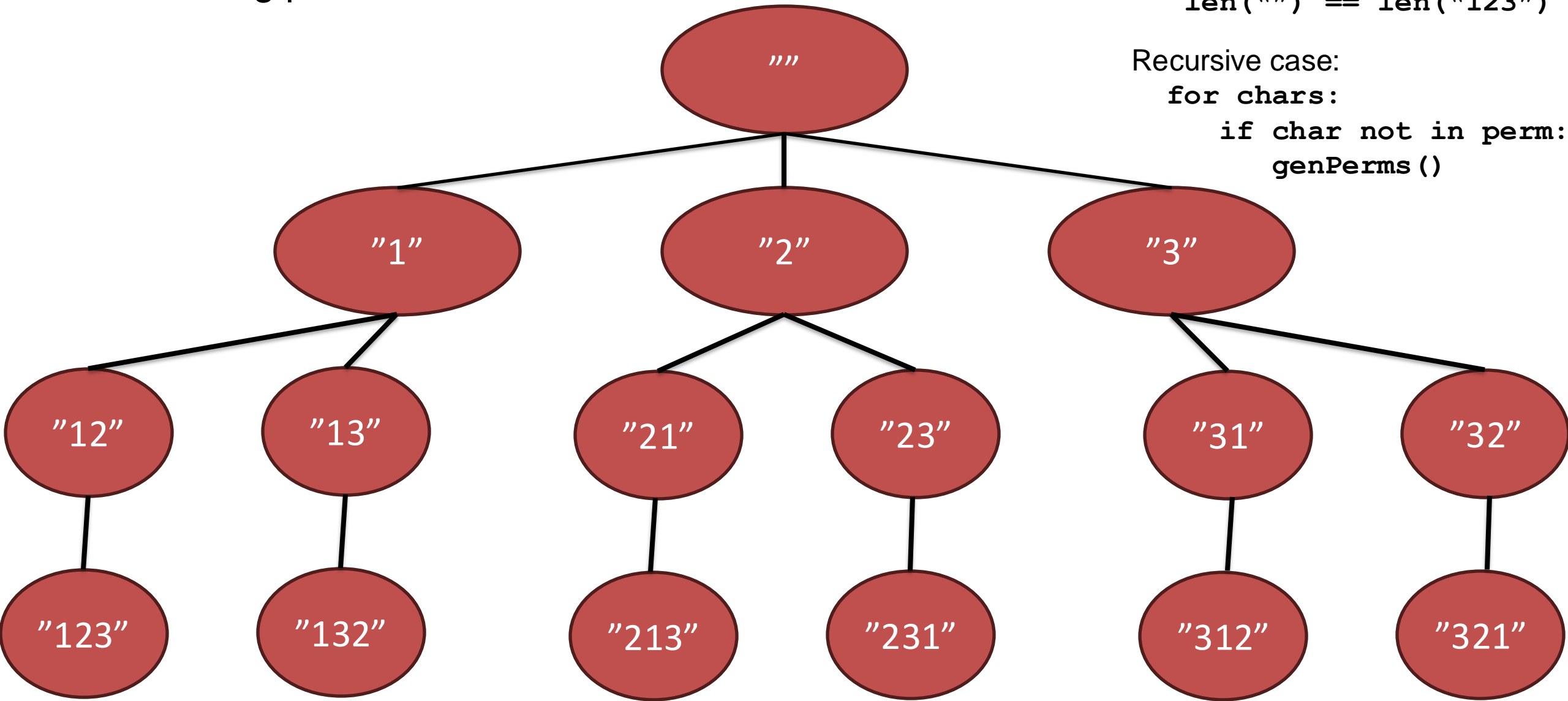
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Ex: calculating permutations of "123"

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for chars:
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Demo

Lab 10