CSCI 132:
Basic Data Structures and Algorithms

Recursion (Part 2)

Reese Pearsall

Spring 2024

Announcements

Lab 10 due **tomorrow**
→ Lowest lab grade gets dropped at end of semester

No in-person lecture on Wednesday

Counting number of characters

Count “X” : “xooxo” → 2
“xxxxx” → 5
“abcdf” → 0

Base Case:

Recursive Case:

Counting number of characters

Count “X” : “xooxo” → 2
“xxxxx” → 5
“abcdf” → 0

Base Case:

If we ever have a string length of 0, return 0

Recursive Case:

Look at the first character, if it is an “X” return 1 and recurse
Look at the first character, if it is not an “X” return 0 and recurse

countX(“oxxo”)

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“**o**xxo”)

0 + countX(“xxo”)

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“**o**xxo”)

0 + countX(“**x**xo”)

1 + countX(“xo”)

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + countX(“xo”)

1 + countX(“o”)

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + countX(“xo”)

1 + countX(“o”)

0 + countX(“”)

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + countX(“xo”)

1 + countX(“o”)

0 + countX(“”)

0

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + countX(“xo”)

1 + countX(“o”)

0 + 0

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + countX(“xo”)

1 + 0

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + countX(“xo”)

1 + 0

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + countX(“xxo”)

1 + 1

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

countX(“oxxo”)

0 + 2

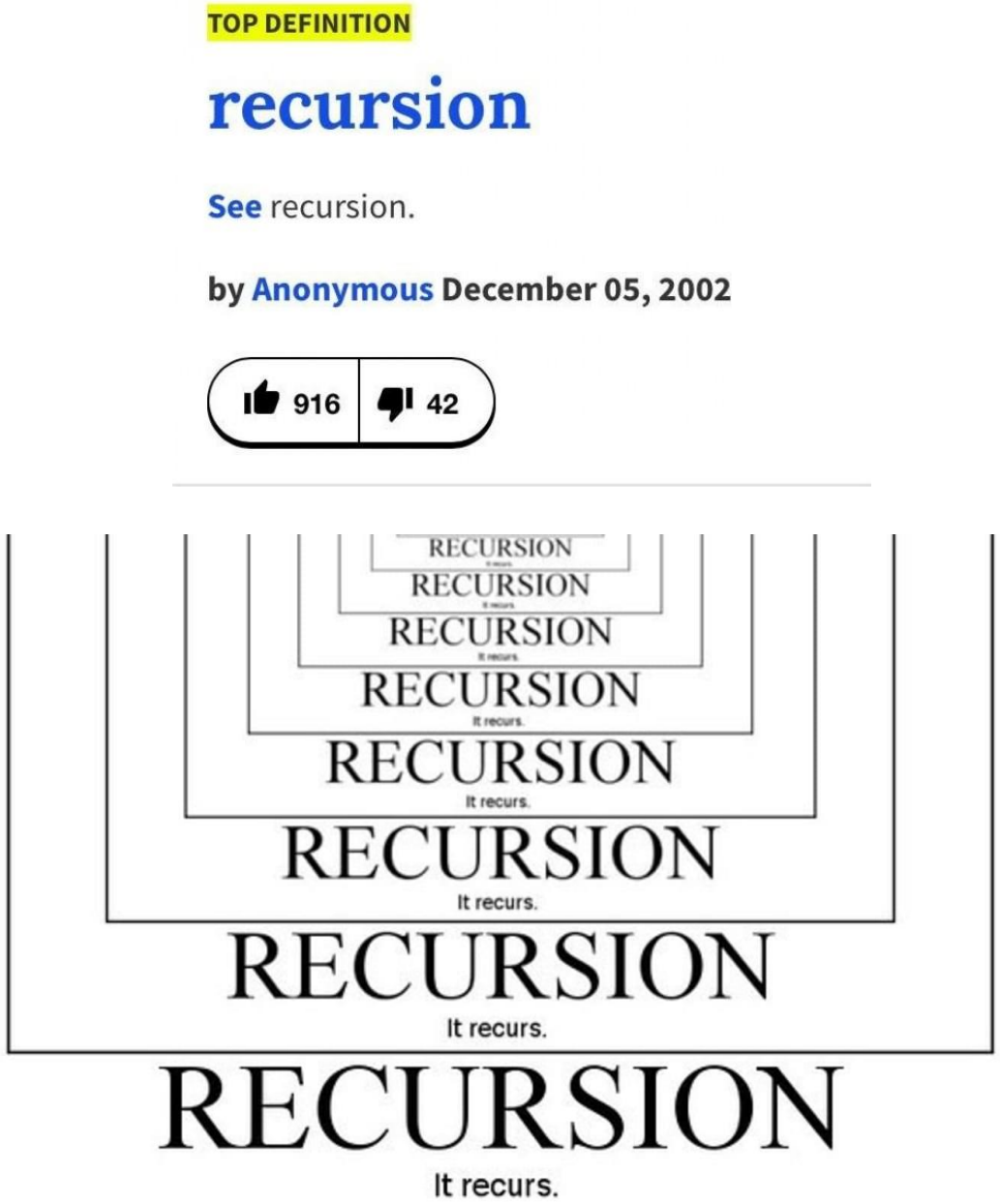
```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x’){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

Final answer = 2

```
public static int countX(String str) {
    if(str.length() == 0){
        return 0;
    }
    if(str.charAt(0) == 'x'){
        return 1 + countX(str.substring(1));
    }
    else{
        return 0 + countX(str.substring(1));
    }
}
```

Recursion is a problem-solving technique that involves a *method calling itself* to solve some smaller problem

```
static int factorial(int n)
    {
        if (n == 0)
            return 1;

        return n * factorial(n - 1);
    }
```

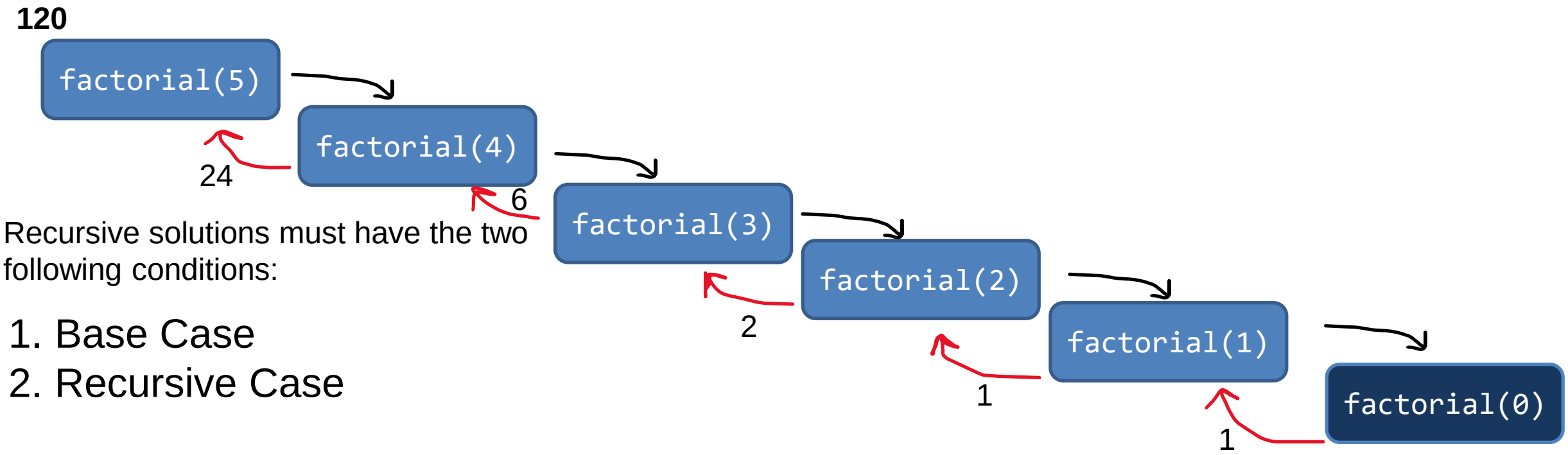


```
static int factorial(int n)
    {
        if (n == 0)
            return 1;

        return n * factorial(n - 1);
    }
```

(base case)

(recursive case)

We can solve the factorial for n by solving smaller problems (factorial of n-1) !



Recursive solutions must have the two following conditions:

1. Base Case
2. Recursive Case

Example #1: Star String

Write a method that will take a string `s` as an argument. This method should return the string, but with a star character (*) between matching characters

aabbcc → a*ab*bc*c
abcdd → abcd*d
abcd → abcd

Base Case?

Recursive Case?

Example #1: Star String

Write a method that will take a string `s` as an argument. This method should return the string, but with a star character (*) between matching characters

aabbcc → a*ab*bc*c
abcdd → abcd*d
abcd → abcd

Base Case?

If the length of the string is 1, return the current string (we can't go any smaller)

Recursive Case?

Look at the first two characters of the string. Return the first character (and a * if needed), call the method again, but pass it the string without the first character

Example #1: Star String

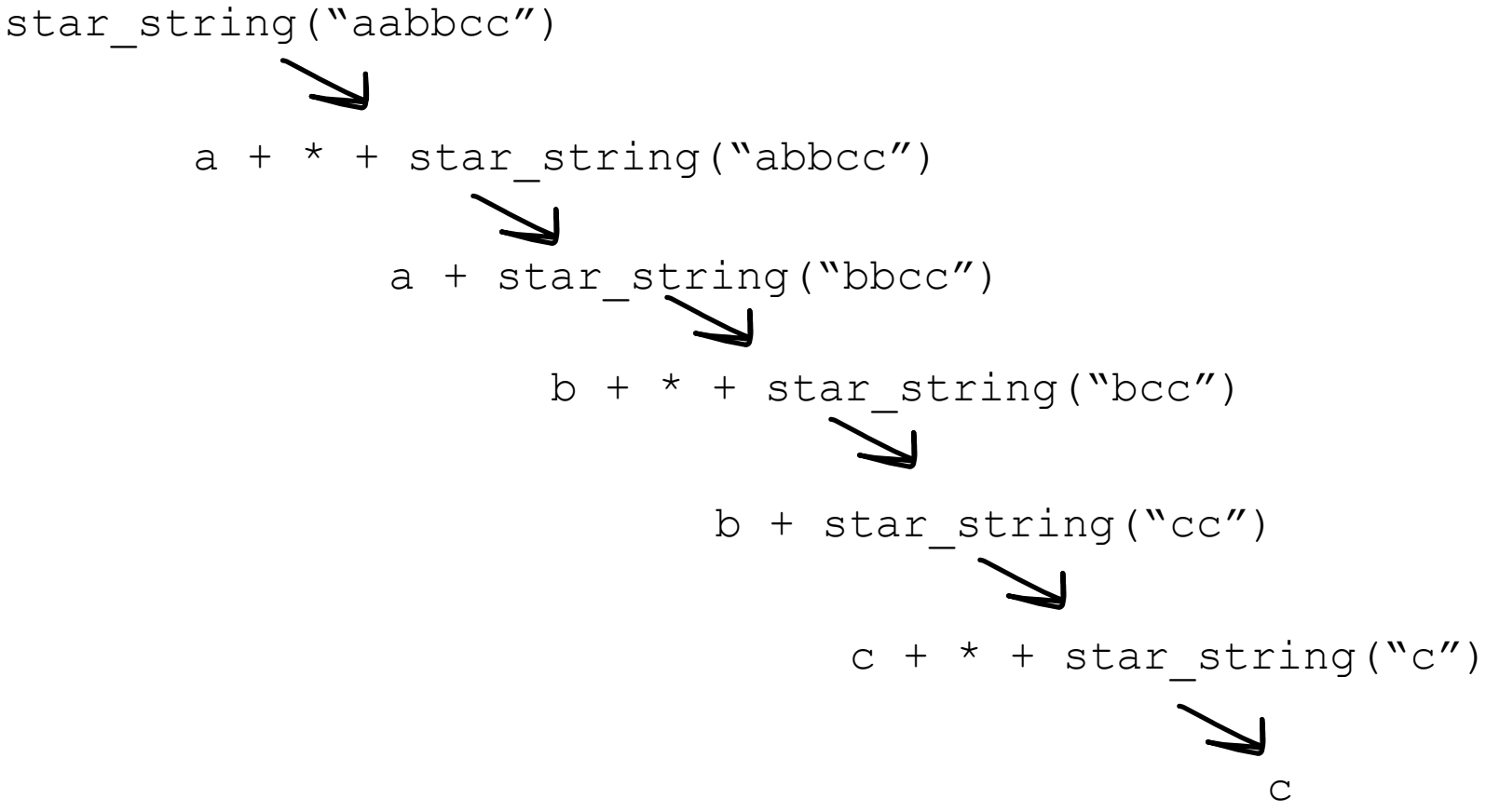
Write a method that will take a string `s` as an argument. This method should return the string, but with a star character (*) between matching characters

```
public static String star_string(String s) {
  if(s.length() == 1) {
    return s;
  }
  else {
     if(s.charAt(0) == s.charAt(1)) {
        return s.charAt(0) + "*" + star_string(s.substring(1));
     }
     else {
        return s.charAt(0) + star_string(s.substring(1));
     }
  }
}
```

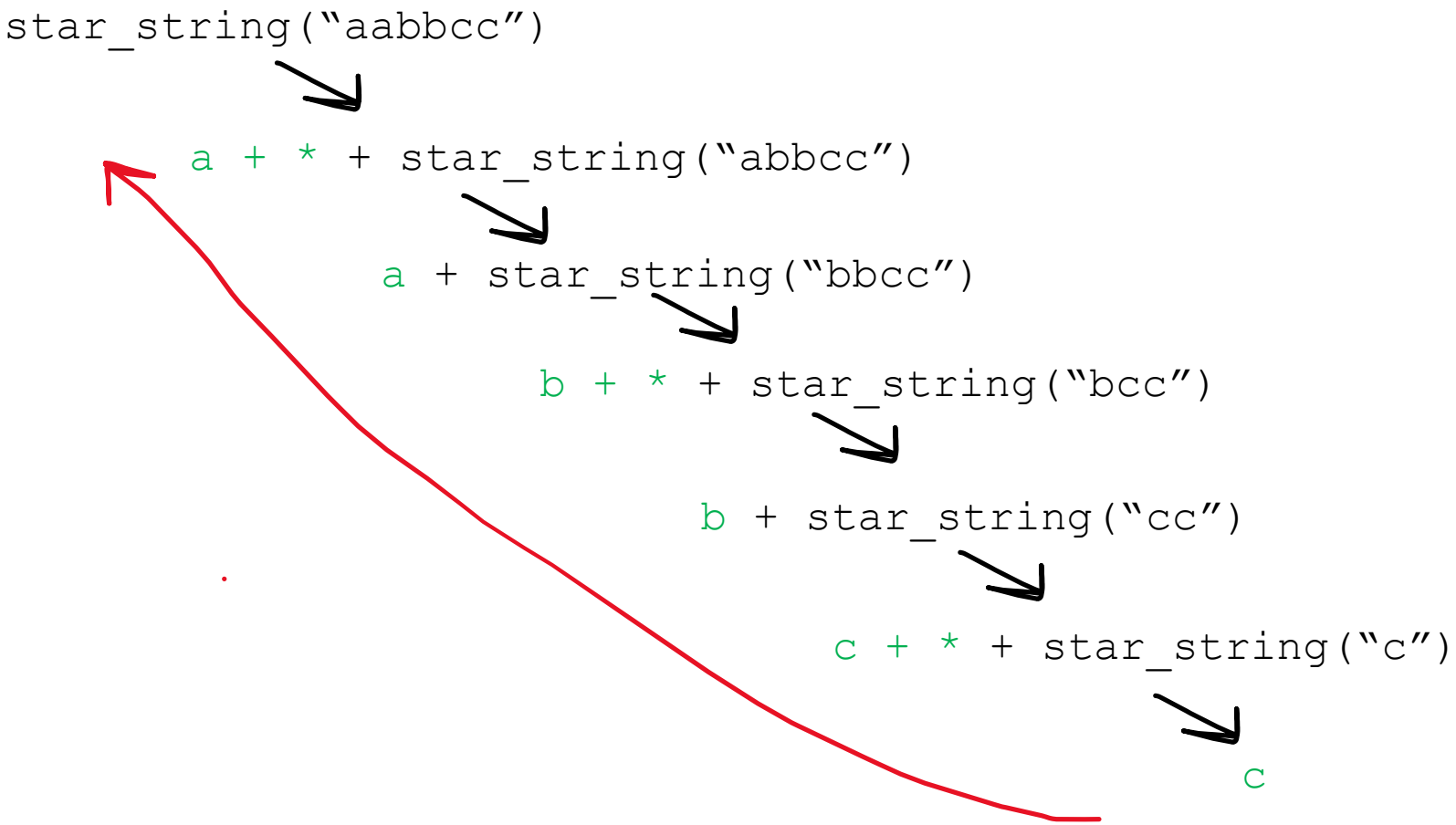
Base Case

Recursive Case

Example #1: Star String



Example #1: Star String



a+*a+b+*+b+c+*c = **a*ab*bc*c**

Example #2: Printing a Linked List

Goal: Print contents of linked list using recursion

Base Case?

Recursive Case?

Example #2: Printing a Linked List

Goal: Print contents of linked list using recursion

Base Case?

If the size of the LL is 1, print the only node

Recursive Case?

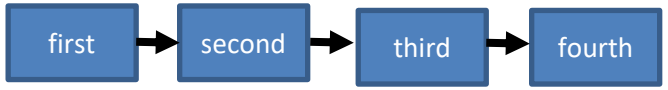
Remove head node, print it, and pass the new LL to the recursive method

```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

print_LL(

)

```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
```

print_LL(first → second → third → fourth)

print_LL(second → third → fourth)

```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
second
```

print_LL(first → second → third → fourth)

print_LL(second → third → fourth)

print_LL(third → fourth)

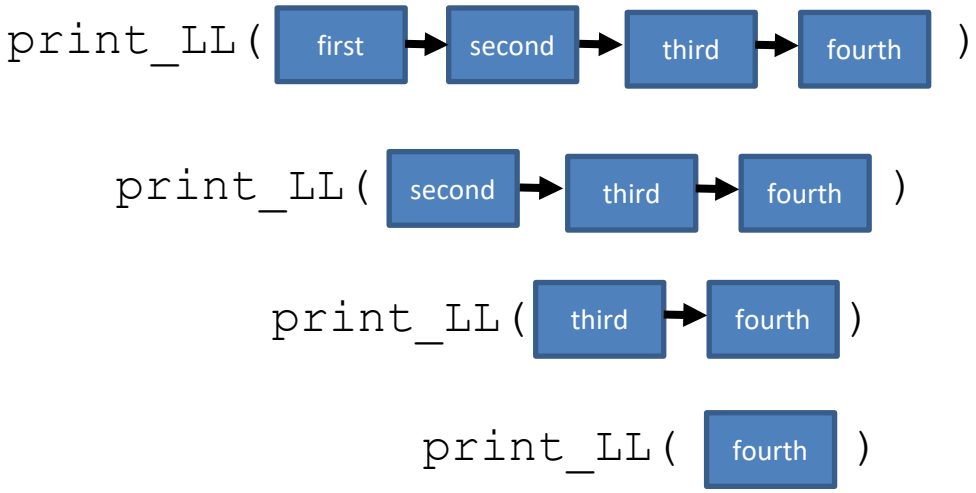
```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
Second
third
```



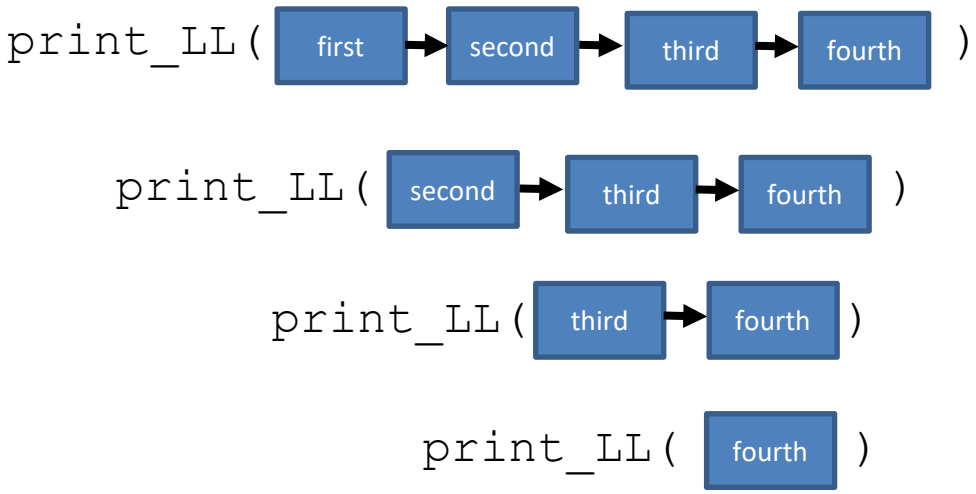
```java
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
Second
third
```



Base case!!

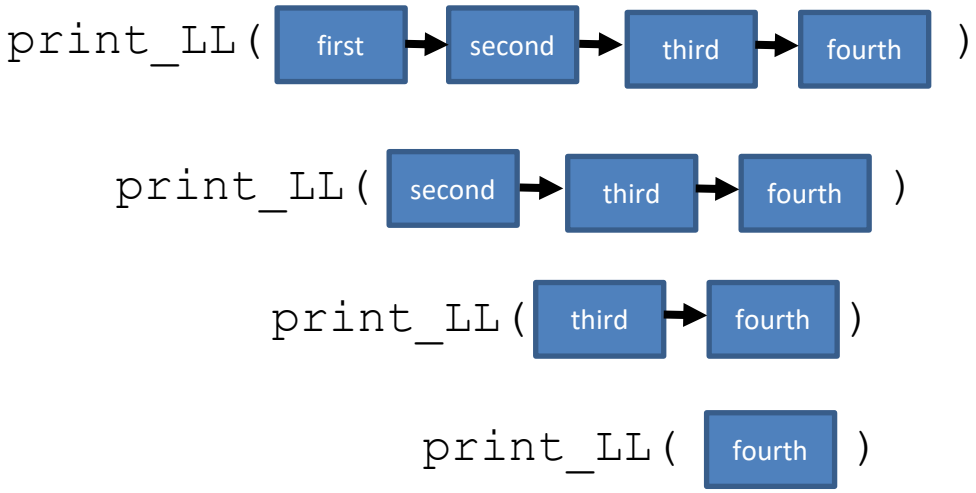
```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
Second
Third
fourth
```



Base case!!

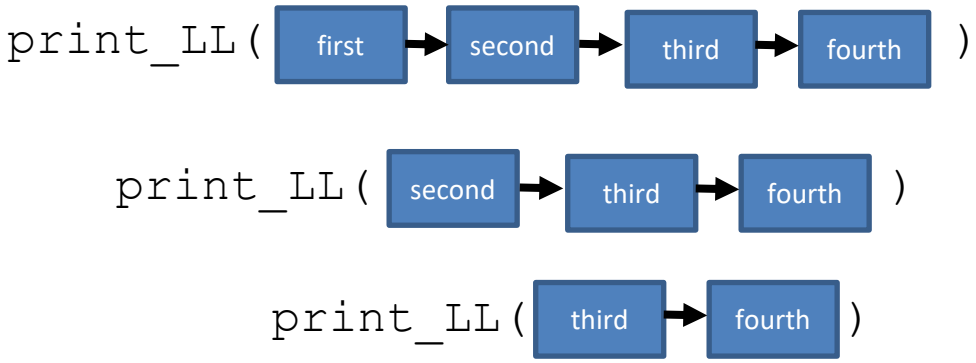
```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
Second
Third
fourth
```



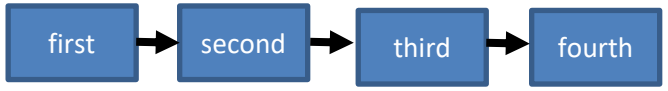
```java
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

Output

```
first
Second
Third
fourth
```

print_LL(

)

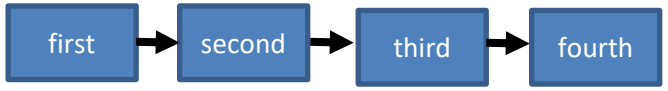
print_LL(

)

```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

Base Case

Recursive Case

print_LL(

)

Output

```
first
Second
Third
fourth
```

```
public static void print_LL(LinkedList<String> ll) {

  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
  }
  else {
    System.out.println(ll.removeFirst());
    print_LL(ll);
  }

}
```

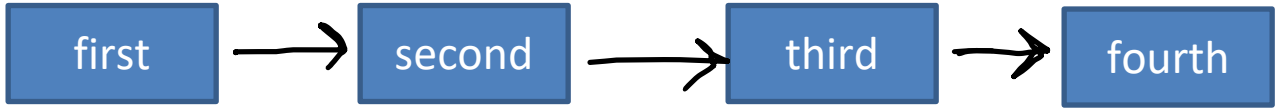
Base Case

Recursive Case

Output

```
first
Second
Third
fourth
```

Example #3: Printing a Linked List in **Reverse**



Goal: Print contents of linked list in reverse order using recursion

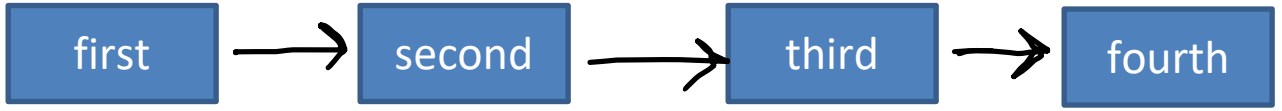
Base Case?

Recursive Case?

Expected Output

```
fourth
third
second
first
```

Example #3: Printing a Linked List in **Reverse**



Goal: Print contents of linked list in reverse order using recursion

Expected Output

```
fourth
third
second
first
```

Base Case?

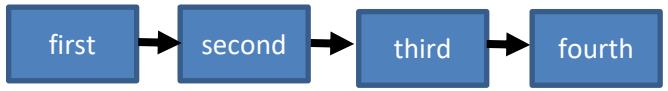
If the size of the LL is 1, print out the only node

Recursive Case?

Remove a node (but don't print it yet), call the recursive method and pass it the new LL. When method returns, print out the node we saved

```java
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

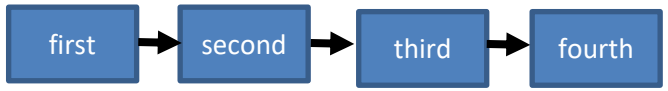
```java
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



value saved: “first”

```
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



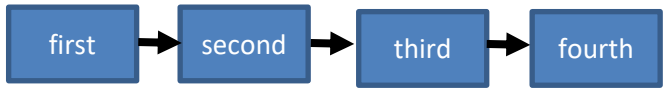
value saved: “first”

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

value saved: “second”

```
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

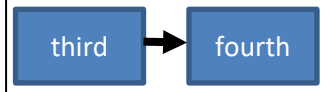


value saved: “first”

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

value saved: “second”

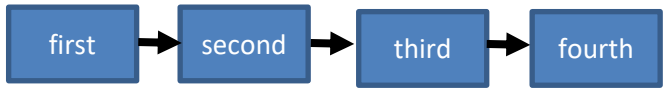
```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



value saved: “third”

```
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

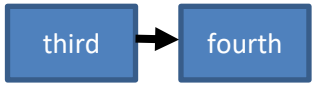


value saved: “first”

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

value saved: “second”

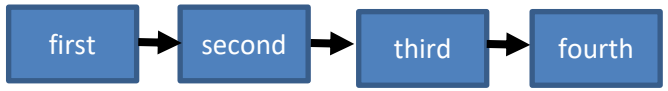
```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



value saved: “third”

```java
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

```java
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

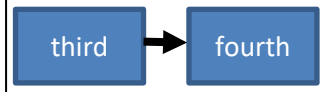


value saved: “first”

```java
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

value saved: “second”

```java
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



value saved: “third”

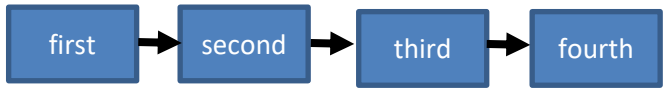
```java
System.out.println(ll.getFirst());
return;
```

```
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

Output

```
fourth
```

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

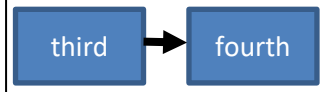


value saved: “first”

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```

value saved: “second”

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



value saved: “third”

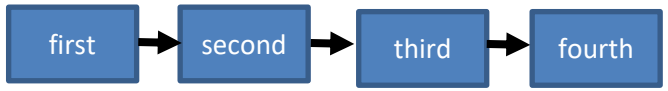
```
System.out.println(ll.getFirst());
return;
```

```
public static void print_LL_reverse(LinkedList<String> ll) {
  if(ll.size() == 1) {
    System.out.println(ll.getFirst());
    return;
  }
  else {
    String removed = ll.removeFirst();
    print_LL_reverse(ll);
    System.out.println(removed);
    return;
}
```

Output

```
fourth
```

```
String removed = ll.removeFirst();
print_LL_reverse(ll);
System.out.println(removed);
return;
```



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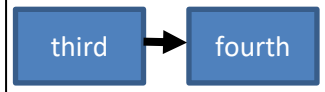

value saved: “third”

```
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return;
```

```java
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Output

```
fourth
```

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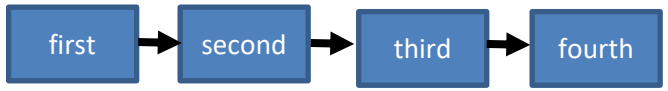

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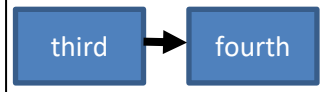

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Output

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fourth
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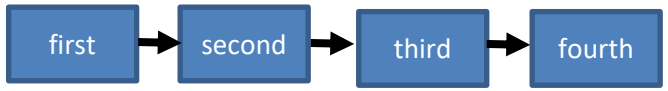

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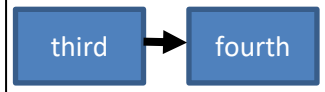

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Output

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fourth
third
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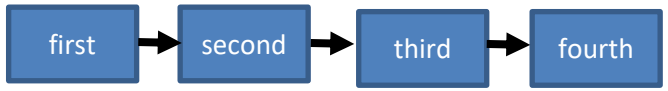

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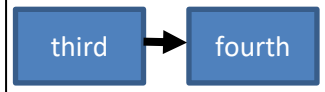

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Output

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fourth
third
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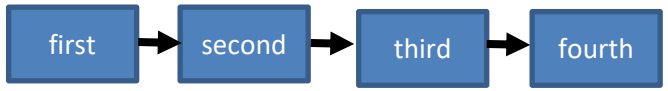

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    return;
}
```

Output

```
fourth
third
second
```

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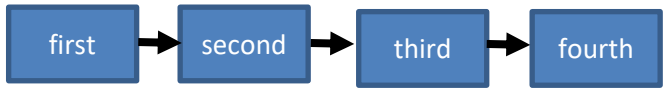

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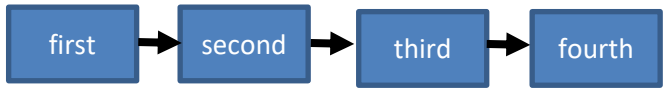

value saved: “first”

Output

```
fourth
third
second
```

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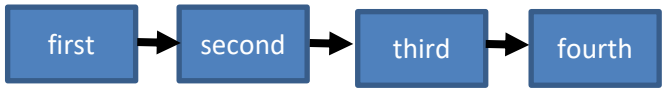

value saved: “first”

Output

```
fourth
third
second
first
```

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    print_LL_reverse(ll);
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    return;
}
```

Output

```
fourth
third
second
first
```

RACECAR

Checking for Palindromes

RACECAR

Checking for Palindromes

RACECAR

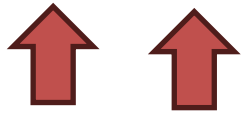
ACECA

Checking for Palindromes

RACECAR

ACECA

CEC

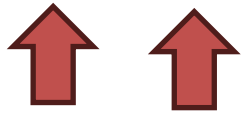


Checking for Palindromes

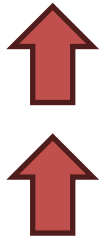
RACECAR

ACECA

CEC



E ✓



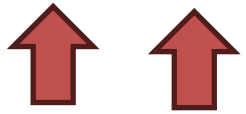
Checking for Palindromes

AABBAA

RACECAR

ACECA

CEC



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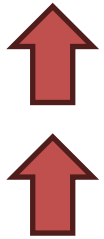

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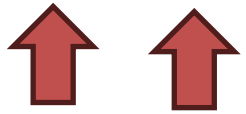

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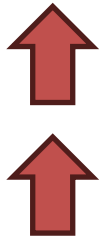

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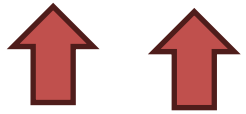

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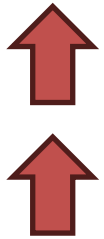

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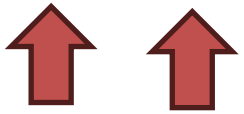

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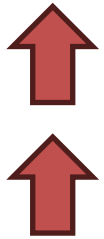

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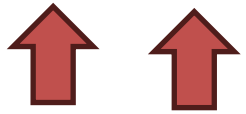

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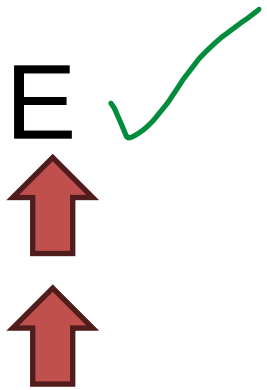

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