

CSCI 232:

Data Structures and Algorithms

Dynamic Programming (Part 3)

Reese Pearsall
Spring 2025

Announcements

Program 4 posted, due Sunday 5/4

→ Watch 4/17 lecture when you are ready to start it

Lab 10 due **tomorrow** at 11:59 PM



(job market is not totally cooked i promise)

Rod Cutting

Given a rod of length n inches, and an array of prices that includes prices of all pieces of size smaller than n , determine the maximum value obtainable by cutting up the rod and selling the pieces.

Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



$n = 8$
(no cuts)

Total profit
\$20



$n = 2$

$n = 2$

$n = 2$

$n = 2$

Total profit
\$20



$n = 3$

Total profit
\$18

$n = 5$



$n = 2$

Total profit
\$22

Optimal profit!

$n = 6$

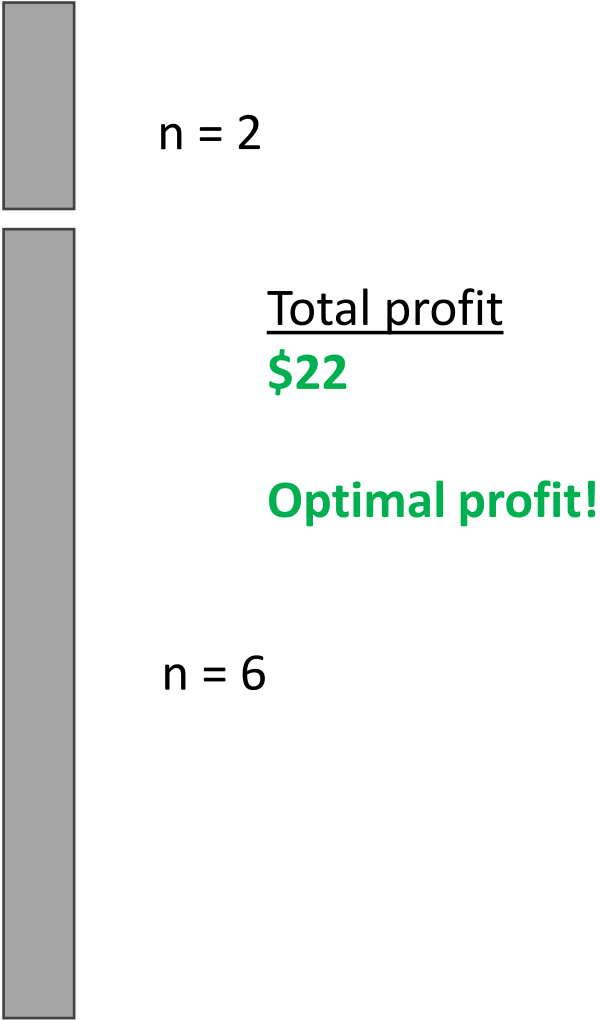
Rod Cutting

Given a rod of length n inches, and an array of prices that includes prices of all pieces of size smaller than n , determine the maximum value obtainable by cutting up the rod and selling the pieces.

Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

Optimal Substructure

Our solution for a rod length of $n=8$, has the optimal solution for rod length of $n = 6$, and $n = 2$



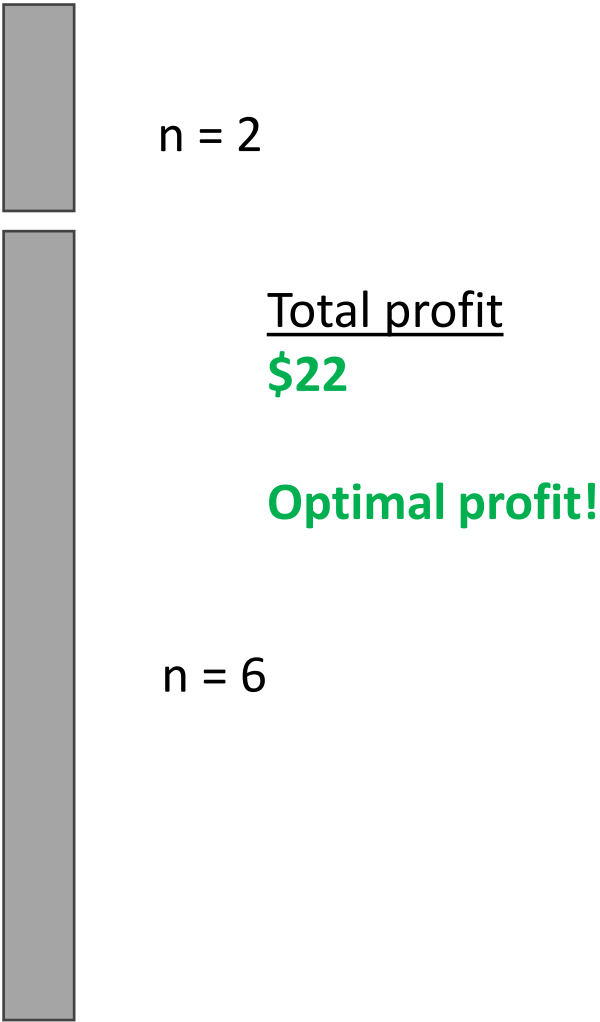
Rod Cutting

Given a rod of length n inches, and an array of prices that includes prices of all pieces of size smaller than n , determine the maximum value obtainable by cutting up the rod and selling the pieces.

Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

General Approach:

Compute all possible ways to cut the rod using dynamic programming, and return which one had the highest profit



Rod Cutting

Given a rod of length n inches, and an array of prices that includes prices of all pieces of size smaller than n , determine the maximum value obtainable by cutting up the rod and selling the pieces.

Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



$n = 2$



$n = 2$

Total profit
\$20



$n = 2$



$n = 2$

Overlapping subproblems

We will compute the optimal way to cut a rod of length $n=2$ many times. We will use memoization to make sure we don't compute problems that we have already solved.

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Technically, our algorithm will consider making a cut of length 8 first, but we will skip over this part to avoid confusion

Rod Cutting

Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



index

Rod Cutting

Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

0 1 2 3 4 5 6 7



index

n = 8



Two options

n = 8



Don't Cut

n = 7



n = 1



Make cut of length index

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



Don't Cut

n = 7



n = 1



Make cut of length index

We want to select the option that yield the highest profit

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



Two options

n = 8



Don't Cut

Now we recurse, and check a new cut value



index



n = 7



n = 1



Make cut of length **index**

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



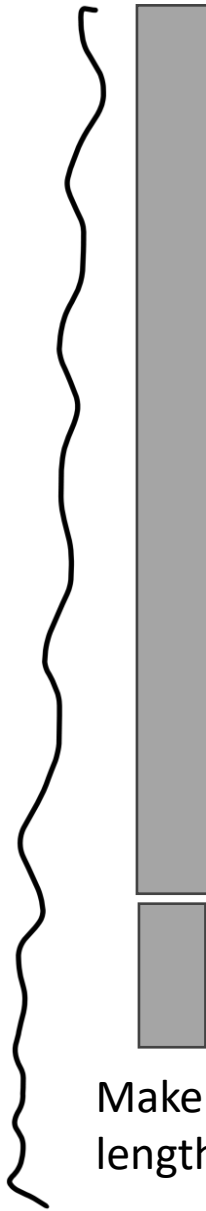
Don't Cut

Now we recurse, and check a new cut value

(index - 1)

n = 7

n = 1



Make cut of length **index**

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



Two options

n = 8



Don't Cut

n = 2



n = 6

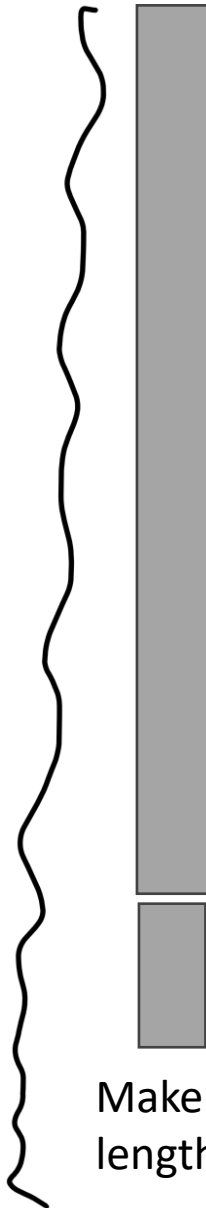


Make cut of
length **index**



index

n = 7



n = 1



Make cut of
length **index**

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



Don't Cut

n = 2



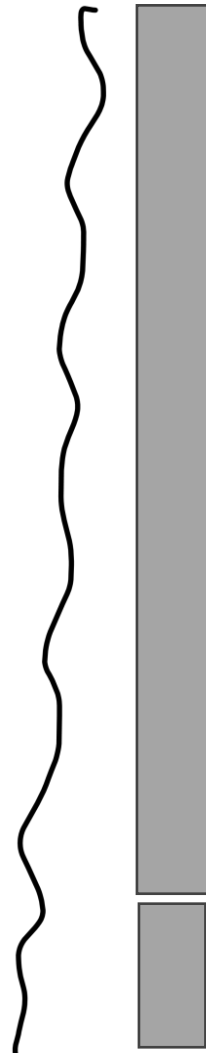
n = 6



Make cut of length index

We want to select the option that yield the highest profit

n = 7



n = 1



Make cut of length index

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



Two options

n = 8



Don't Cut



index



Make cut of
length **index**

n = 2



n = 6



n = 7



n = 1



Make cut of
length **index**

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



Two options

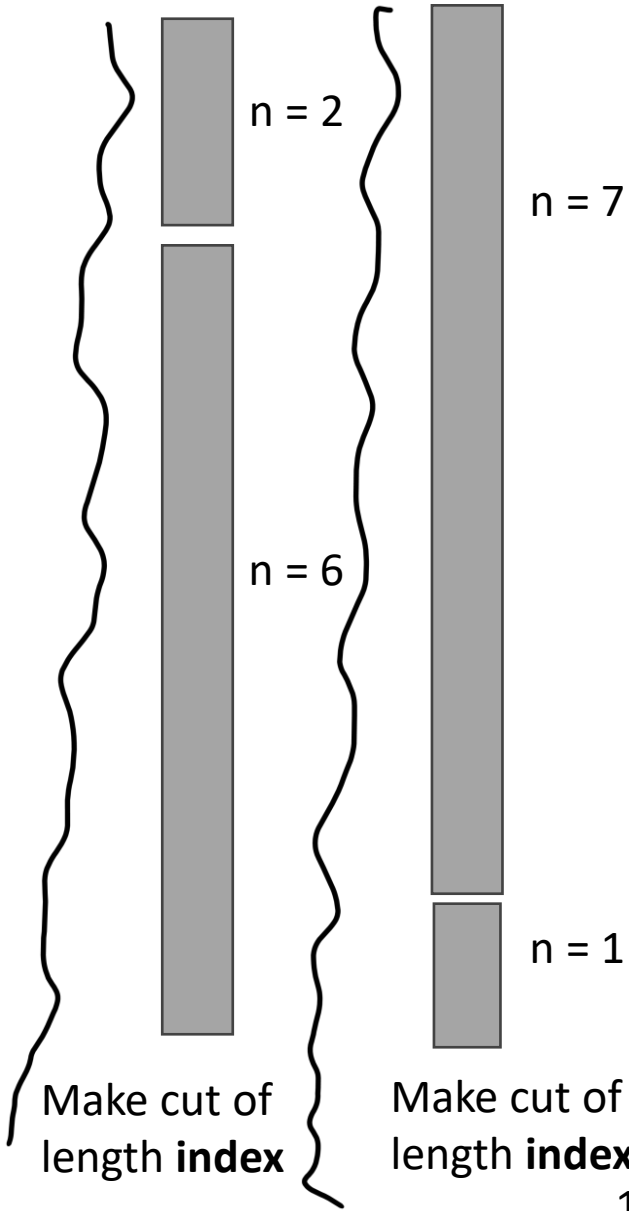
n = 8



Don't Cut



index



Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



Two options

n = 8



Don't Cut

N = 5



N = 3



Make cut of
length **index**



index

n = 2



n = 6



Make cut of
length **index**

n = 7



n = 1



Make cut of
length **index**

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

n = 8



Two options

n = 8



Don't Cut

Whenever we don't make the cut,
we don't adjust the size of the rod,
but we check the next cut length



index



Make cut of
length **index**

N = 5

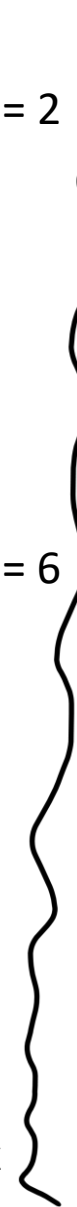
N = 3



Make cut of
length **index**

n = 6

n = 2



Make cut of
length **index**

n = 1

n = 7

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



Don't Cut

n = 7



n = 1



Make cut of
length **index**

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



Don't Cut

n = 7



n = 1

Make cut of
length **index**

We made a cut of length index,
so lets figure out how much that
piece is worth!

`prices[index]`

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



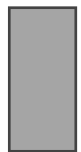
Don't Cut

n = 7



Make cut of length **index**

n = 1



We made a cut of length index, so let's figure out how much that piece is worth!

`prices[index]`

We have 1 inch of rod left, so we need to now figure out the optimal way to cut this

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



n = 8



Two options

n = 8



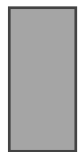
Don't Cut

n = 7



Make cut of
length **index**

n = 1



We made a cut of length index,
so lets figure out how much that
piece is worth!

`prices[index]`

Length of cut made = (index + 1)

We have 1 inch of rod left, so we
need to now figure out the
optimal way to cut this
--Recurse!

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



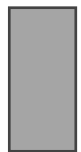
Don't Cut

n = 7



Make cut of
length **index**

n = 1



We made a cut of length index,
so lets figure out how much that
piece is worth!

`prices[index]`

Length of cut made = $(\text{index} + 1)$

New subproblem = $n - \text{length_of_cut}$

We have 1 inch of rod left, so we
need to now figure out the
optimal way to cut this
--Recurse!

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



Don't Cut

n = 7



Make cut of
length **index**

n = 1



We made a cut of length index,
so lets figure out how much that
piece is worth!

`prices[index]`

Length of cut made = $(\text{index} + 1)$

New subproblem = $n - \text{length_of_cut}$

We have 1 inch of rod left, so we
need to now figure out the
optimal way to cut this
--Recurse!

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 8



Don't Cut

n = 7



n = 1

Make cut of
length **index**

Whenever we make the cut, we
adjust the size of the rod, but keep
the same index

Rod Cutting

	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 4



Don't Cut

n = 2



n = 2



Make cut of
length **index**

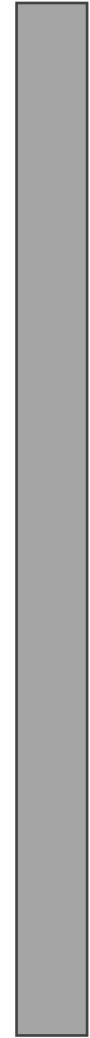
Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



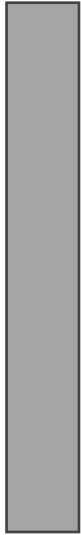
index

n = 8



Two options

n = 4



Don't Cut

Profit: 9

n = 2



n = 2



Make cut of
length index

Profit: 10

Given a rod of length 4 and a potential cut value of length 2, the optimal solution is to **make the cut**

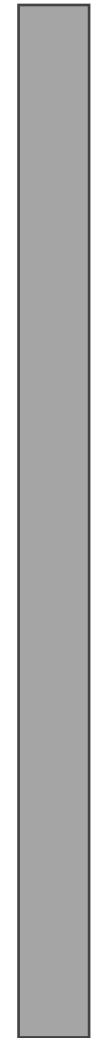
Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20



index

n = 8



Two options

n = 4



Don't Cut

Profit: 9

n = 2



n = 2



Make cut of length index

Profit: 10

Given a rod of length 4 and a potential cut value of length 2, the optimal solution is to **make the cut**

If we ever encounter this same subproblem again, we want to make sure we don't recompute it

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20

↑
index

n = 8



Two options

n = 4



Don't Cut

Profit: 9

n = 2



n = 2



Make cut of
length index

Profit: 10

We need to put this solution (10)
into our memorization table

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20


index



$n = 2$



$n = 2$

Make cut of
length **index**

Profit: 10

Cut Length

Rod Length

	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6								
7								
8								

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20


index



$n = 2$



$n = 2$

Make cut of
length **index**

Profit: 10

Cut Length

Rod Length

	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6								
7								
8								

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20


index

$dp[index][n] = 10$

Rod Length

	1	2	3	4	5	6	7	8
1								
2				10				
3								
4								
5								
6								
7								
8								

Cut Length

$n=4$



$n = 2$



$n = 2$

Make cut of length **index**

Profit: 10

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20


index

$dp[index][n] = 10$

Rod Length

	0	1	2	3	4	5	6	7	8
0									
1					10				
2									
3									
4									
5									
6									
7									

Cut Length

$n=4$



$n = 2$



$n = 2$

Make cut of length **index**

Profit: 10

Rod Cutting

	0	1	2	3	4	5	6	7
Length	1	2	3	4	5	6	7	8
Price	1	5	8	9	10	17	17	20


index

$dp[index][n] = 10$

Rod Length

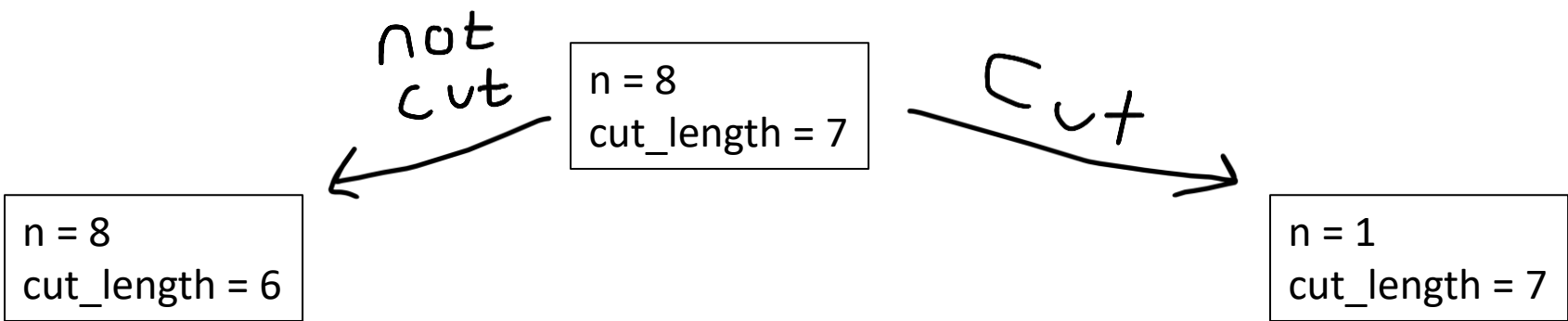
Cut Length

	1	2	3	4	5	6	7	8
1								
2				10				
3								
4								
5								
6								
7								
8								

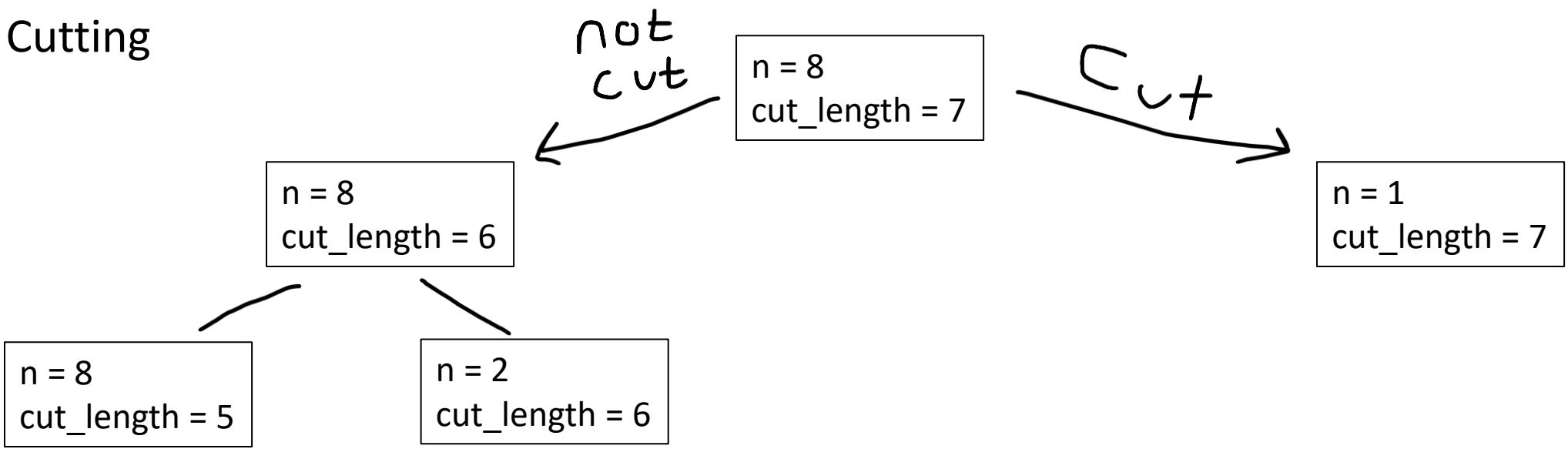
Profit: 10

Whenever we solve a subproblem, remember to place it inside of our memoization table

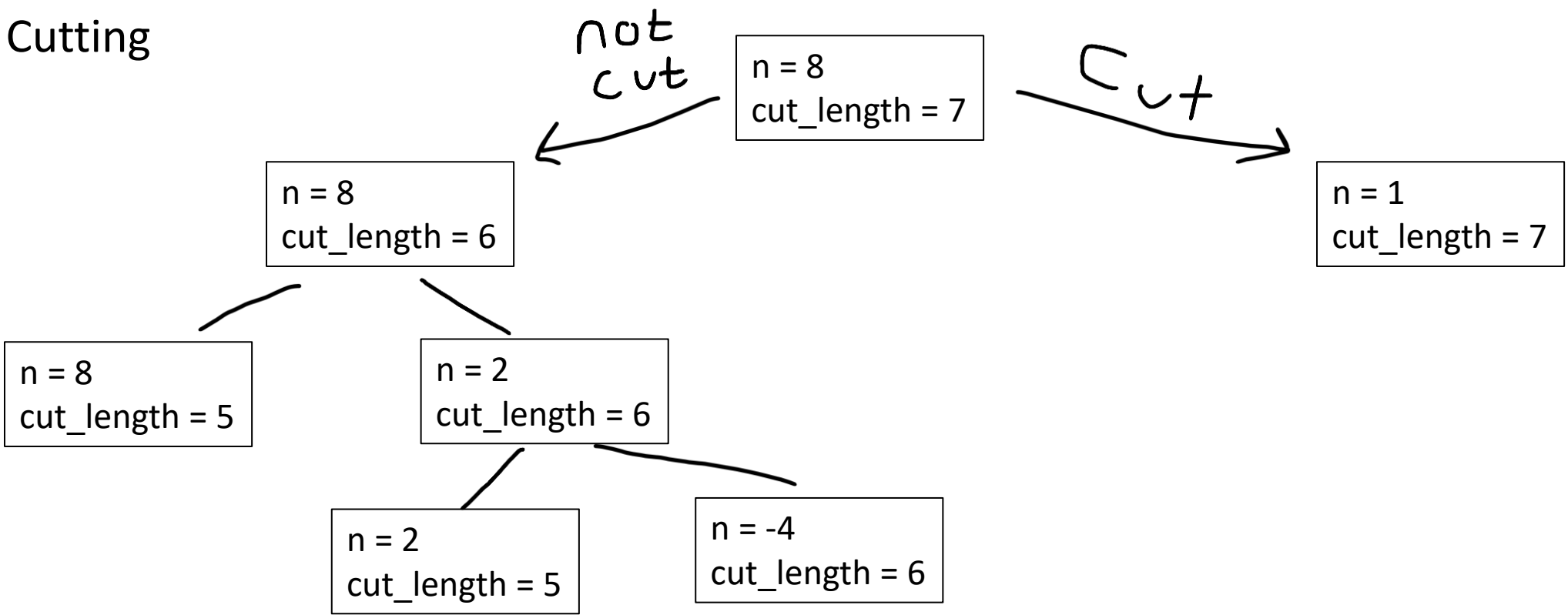
Rod Cutting



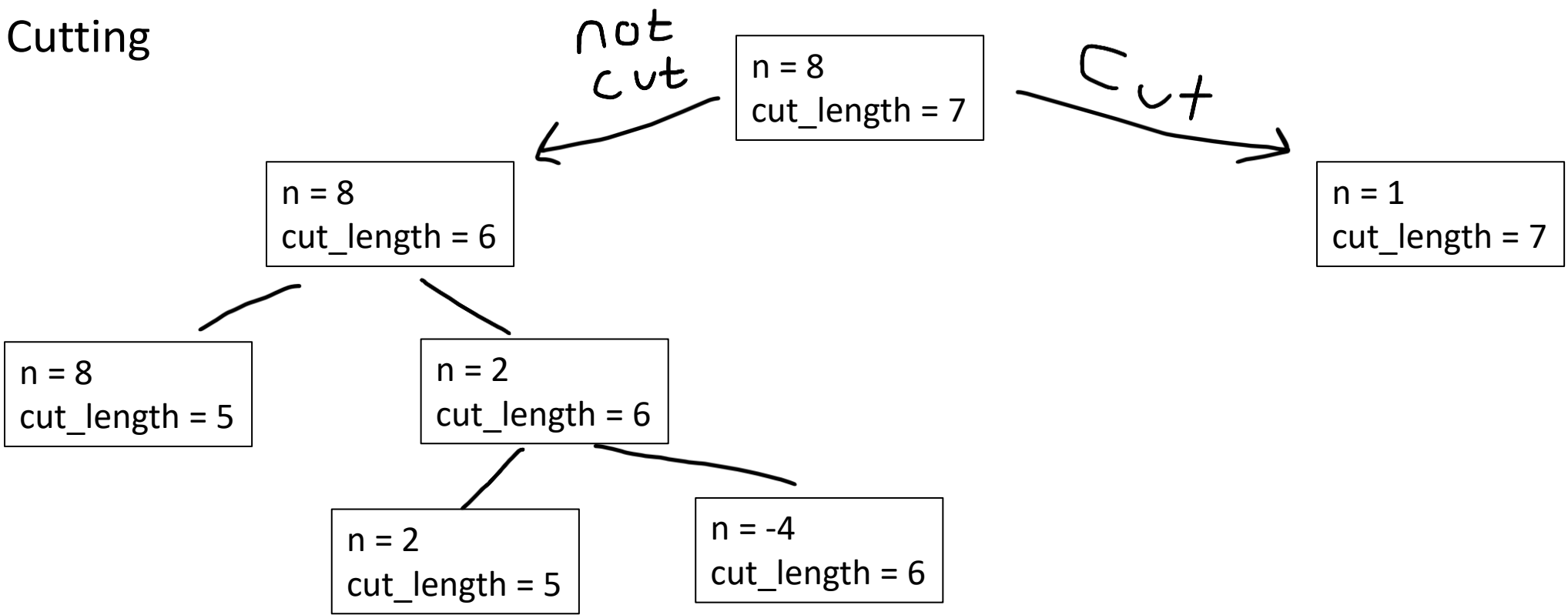
Rod Cutting



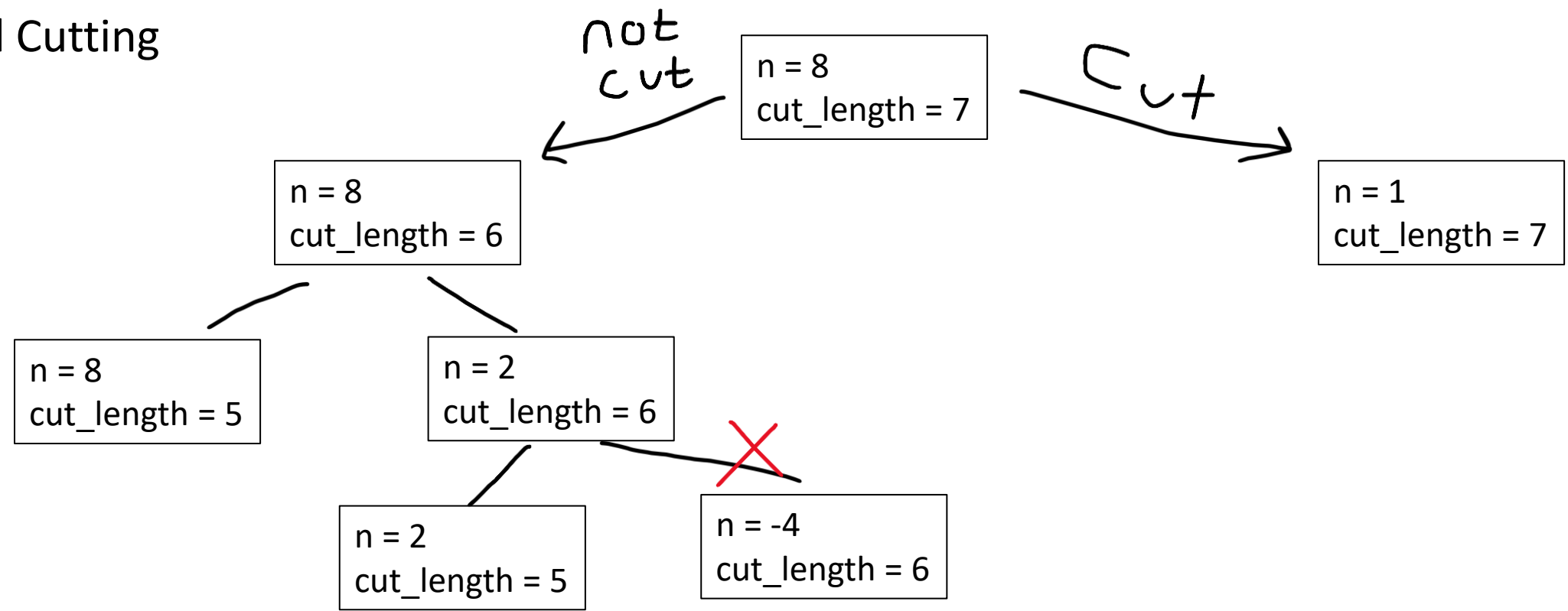
Rod Cutting



Rod Cutting

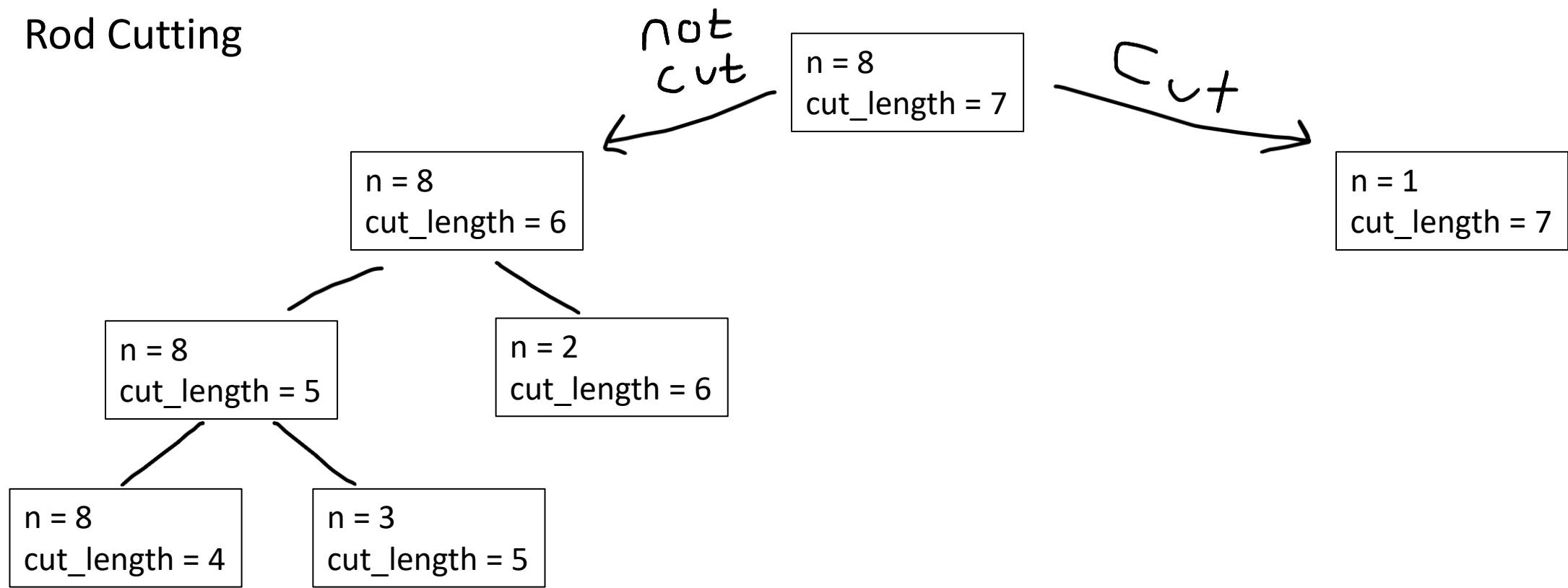


Rod Cutting

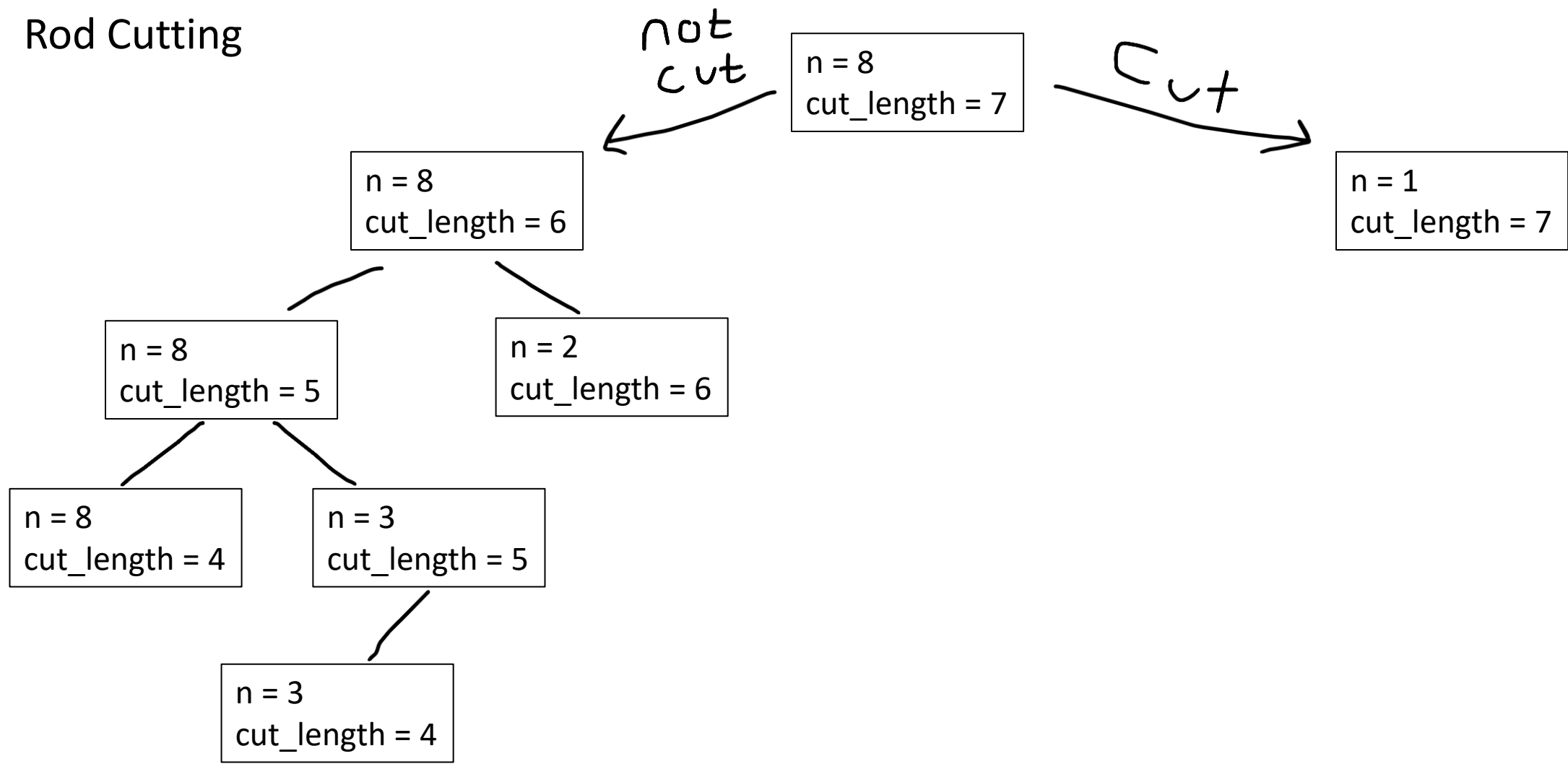


Only make the cut if its possible

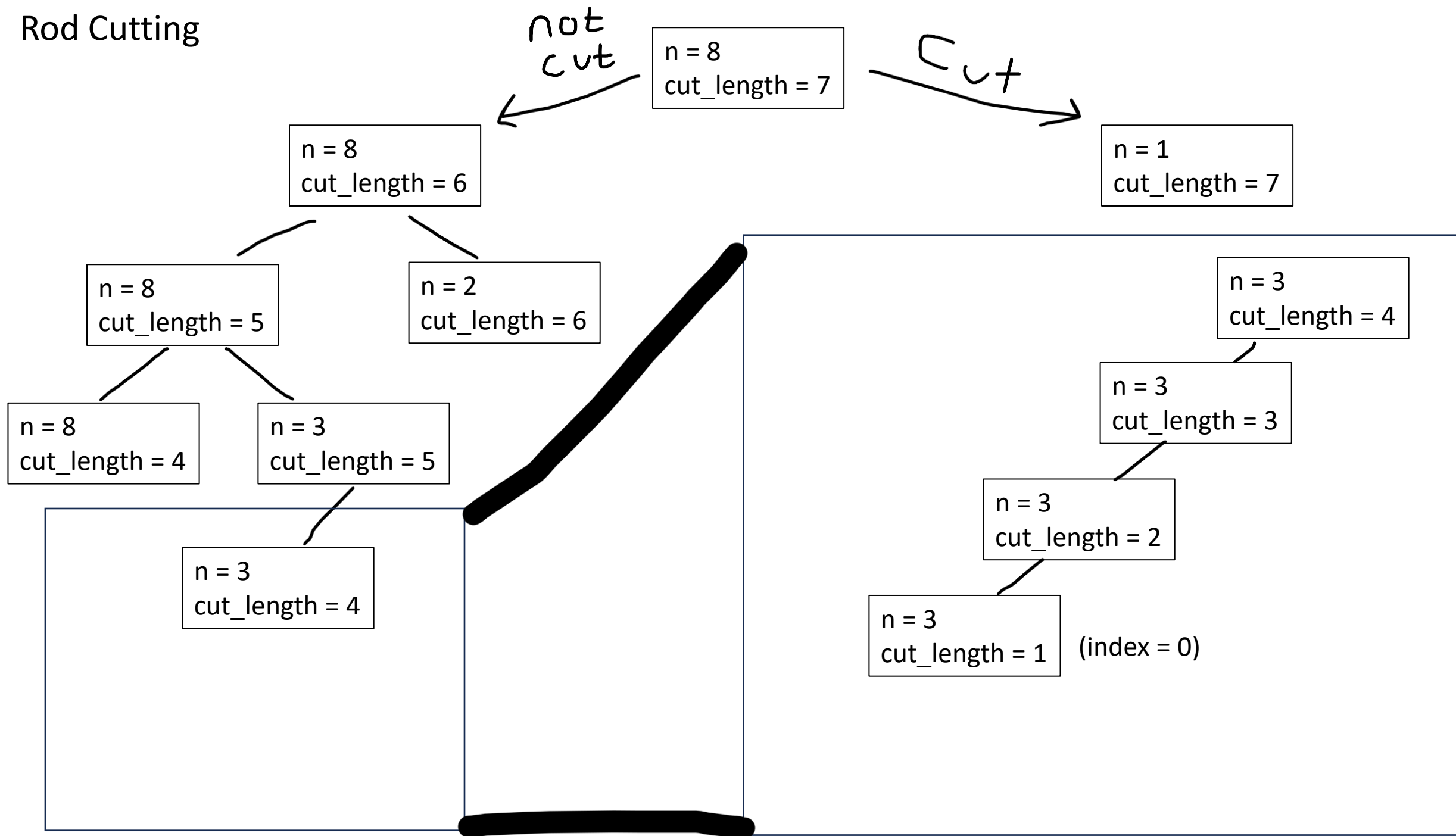
Rod Cutting



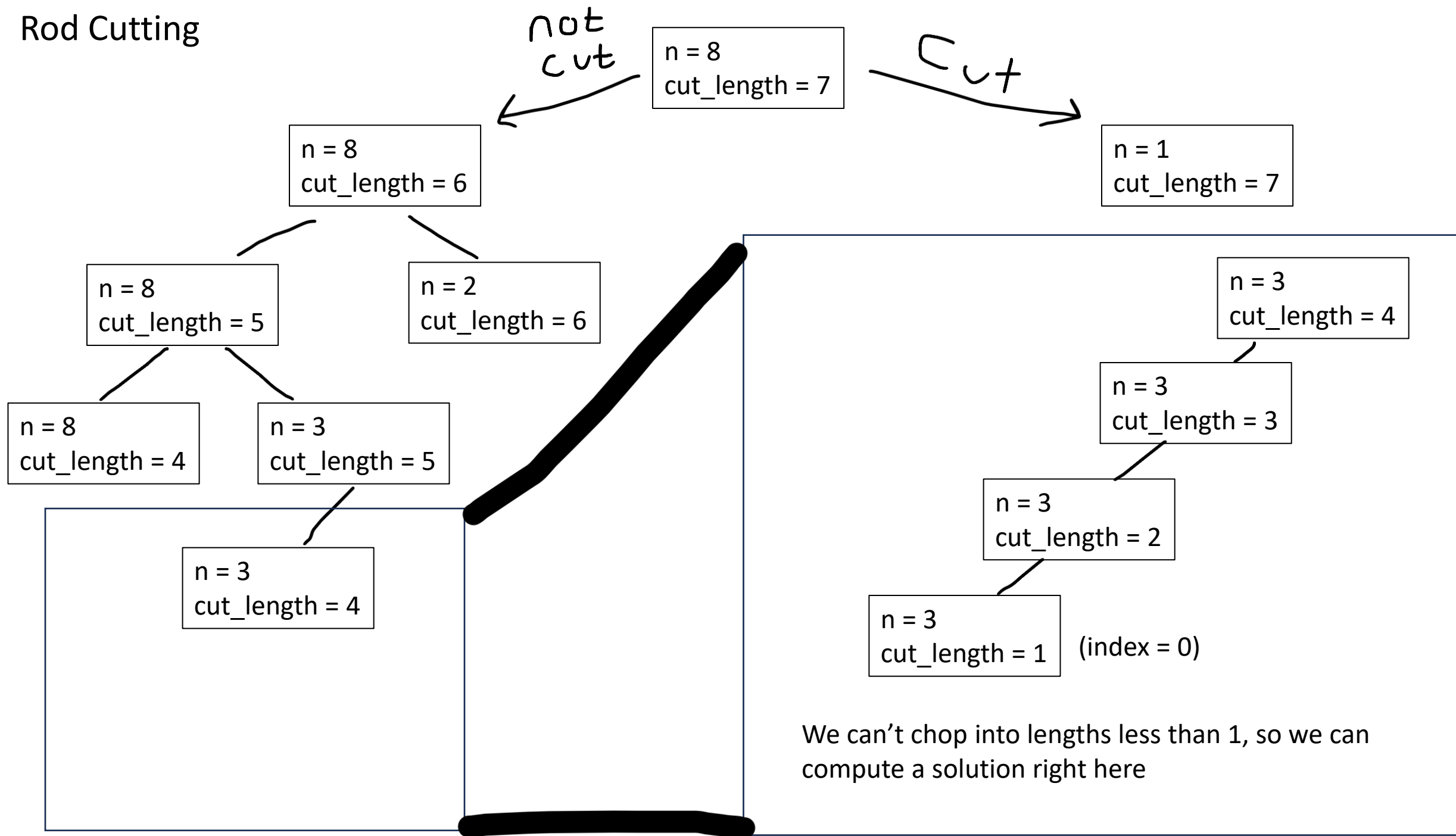
Rod Cutting



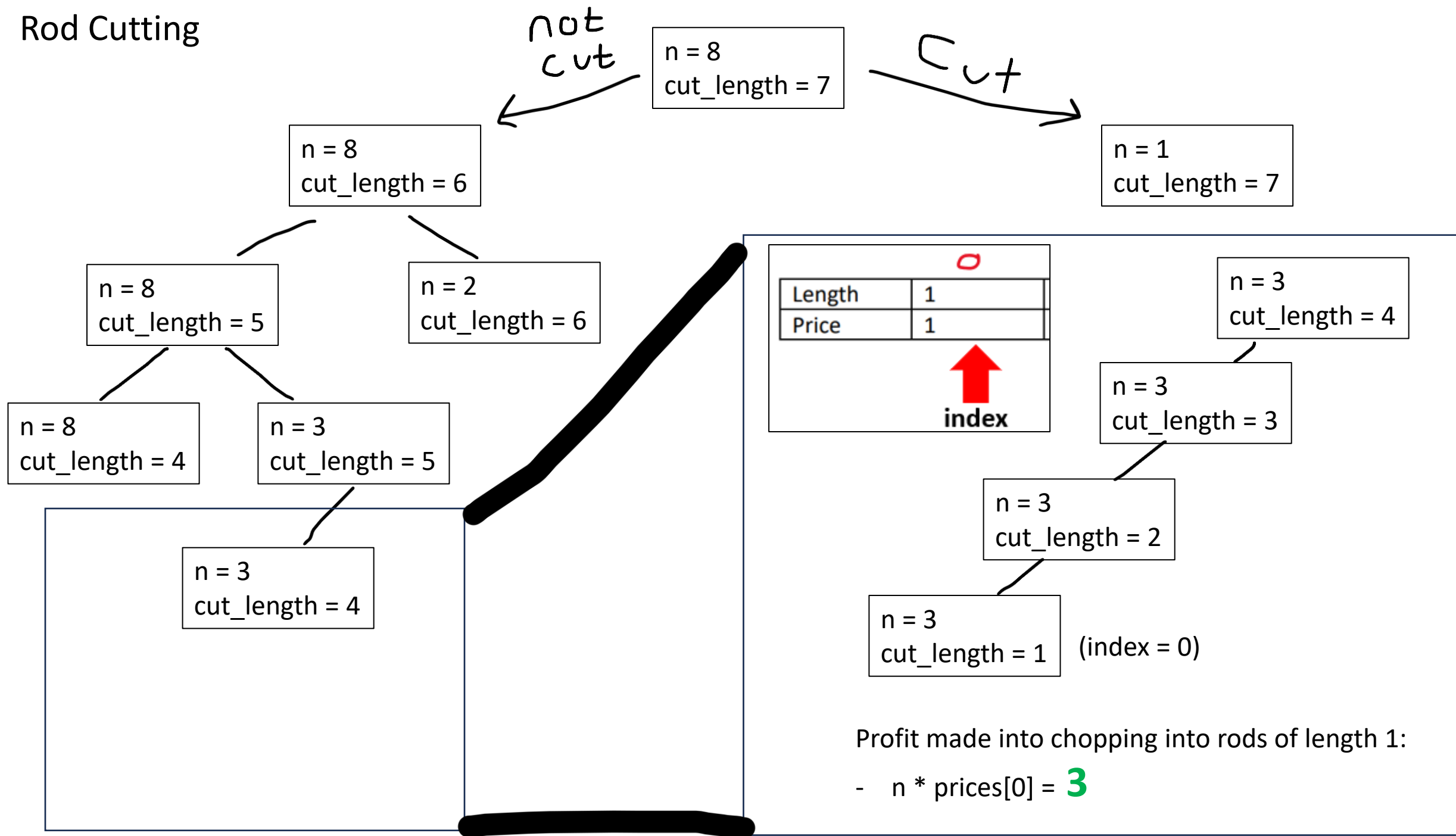
Rod Cutting



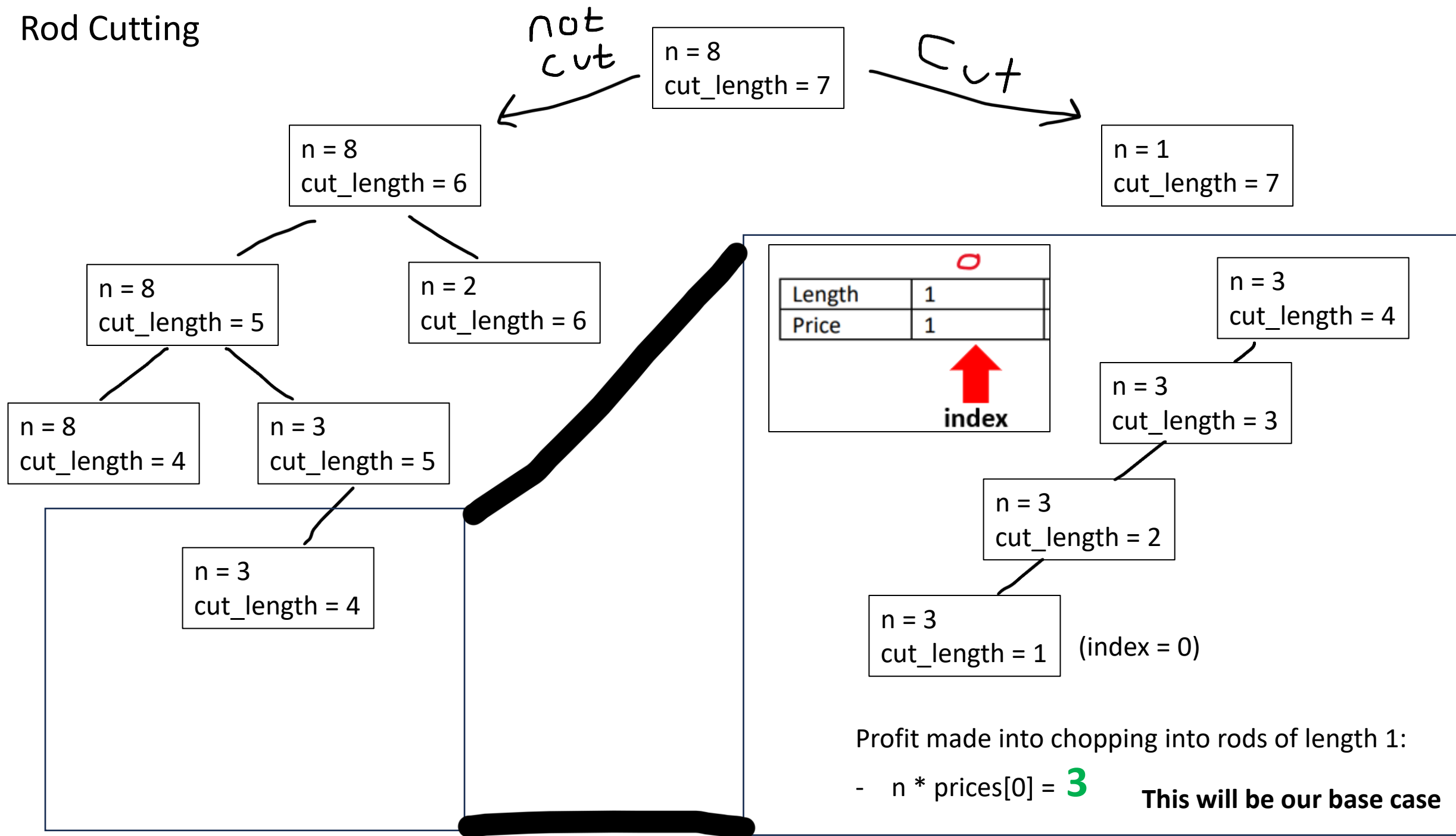
Rod Cutting



Rod Cutting



Rod Cutting



LETS TRY TO CODE THIS

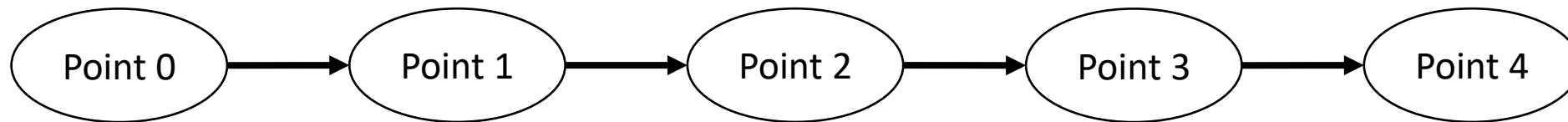
If you are confused are the recursion is set up, don't stress out about it. Its not a big deal.

n = 8
cut_l

The goal here is to show how we are using dynamic programming to solve this problem

Taxi Profit

Given a street that goes from point 1 to point N, we are able to pick up customers on the street and take them to the other end of the street. Our taxi is only able to go one direction

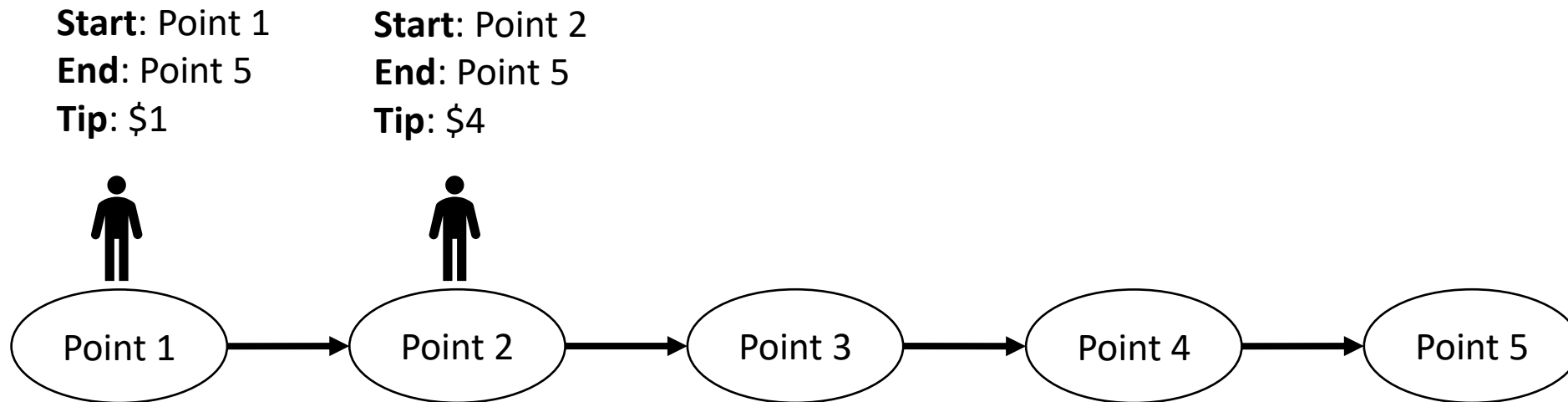


Taxi Profit

Given a street that goes from point 1 to point N, we are able to pick up customers on the street and take them to the other end of the street. Our taxi is only able to go one direction

Each customer has their starting point (pick-up spot), their ending point (destination), and the tip you will receive if you pick them up

The profit for selecting a customer is $(\text{END} - \text{START}) + \text{TIP}$



Taxi Profit

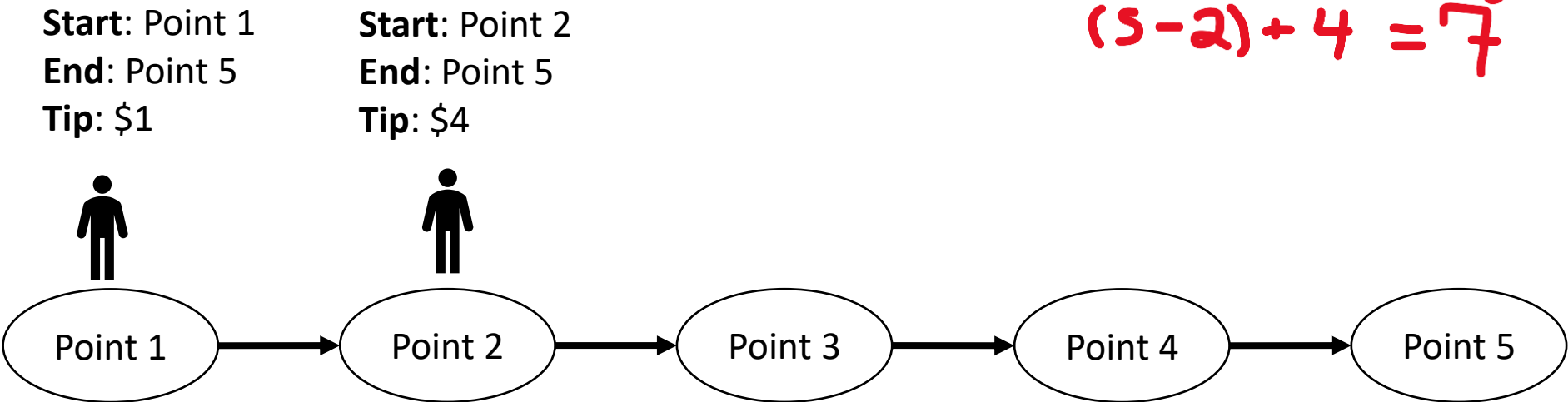
Given a street that goes from point 1 to point N, we are able to pick up customers on the street and take them to the other end of the street. Our taxi is only able to go one direction

Each customer has their starting point (pick-up spot), their ending point (destination), and the tip you will receive if you pick them up

The profit for selecting a customer is $(\text{END} - \text{START}) + \text{TIP}$

$(5 - 1) + 1 = 5$

$(5 - 2) + 4 = 7$



Taxi Profit

Given a street that goes from point 1 to point N, we are able to pick up customers on the street and take them to the other end of the street. Our taxi is only able to go one direction

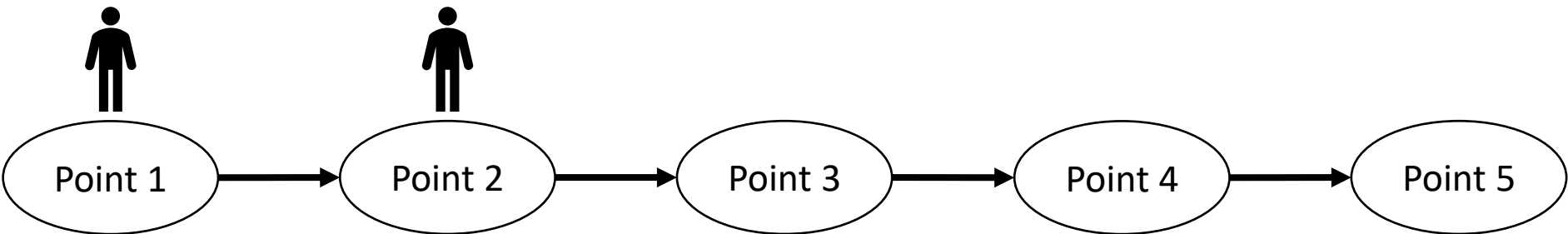
Each customer has their starting point (pick-up spot), their ending point (destination), and the tip you will receive if you pick them up

The profit for selecting a customer is $(\text{END} - \text{START}) + \text{TIP}$

```
rides = [[1, 5, 1]      [2, 5, 4]      ]
```

Start: Point 1
End: Point 5
Tip: \$1

Start: Point 2
End: Point 5
Tip: \$4



What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Taxi Profit

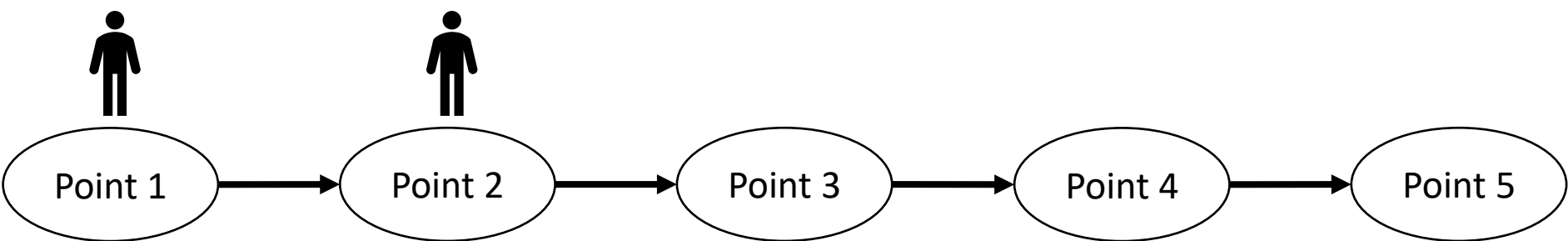
Given a street that goes from point 1 to point N, we are able to pick up customers on the street and take them to the other end of the street. Our taxi is only able to go one direction

Each customer has their starting point (pick-up spot), their ending point (destination), and the tip you will receive if you pick them up

The profit for selecting a customer is $(END - START) + TIP$

```
rides = [[1, 5, 1]      [2, 5, 4]      ]
         Start: Point 1  Start: Point 2
         End: Point 5    End: Point 5
         Tip: $1         Tip: $4
```

Is there another way we could represent this problem?

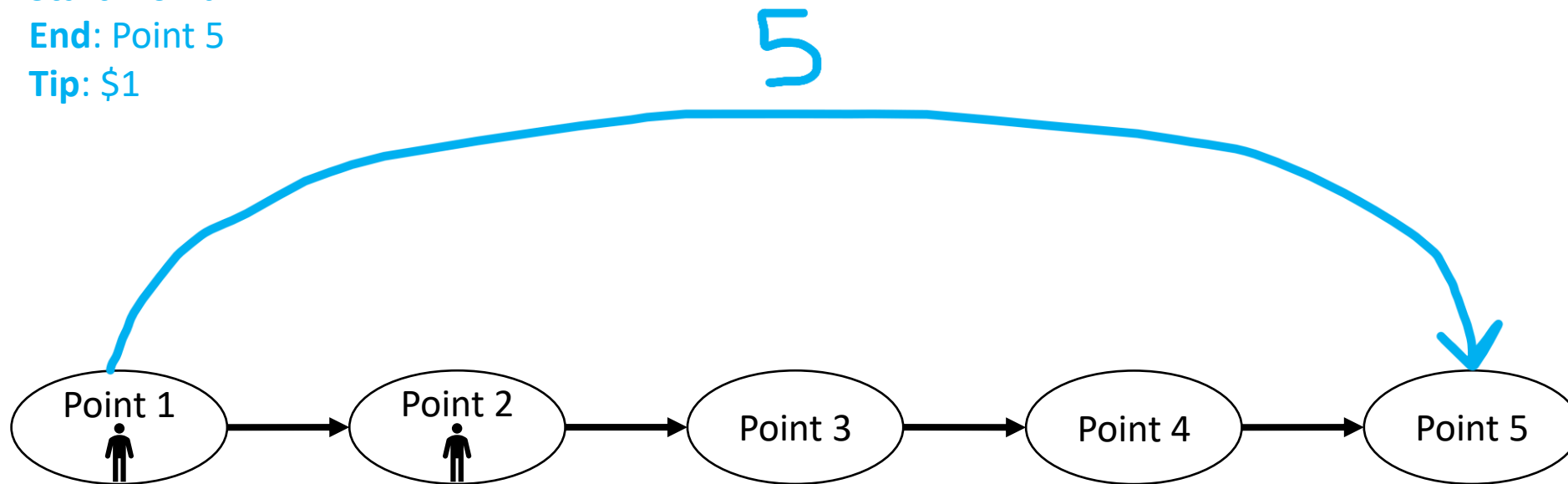


What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Taxi Profit (Graph Representation)

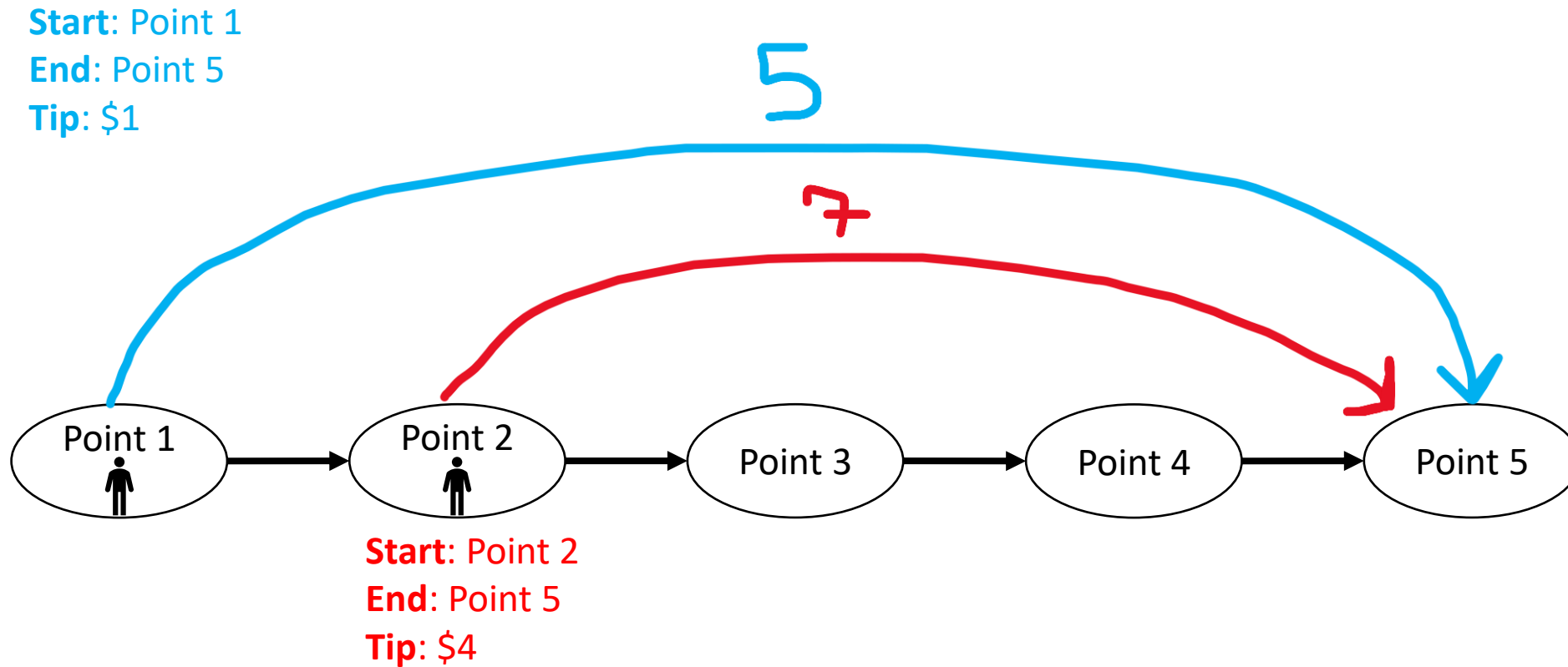
What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Start: Point 1
End: Point 5
Tip: \$1



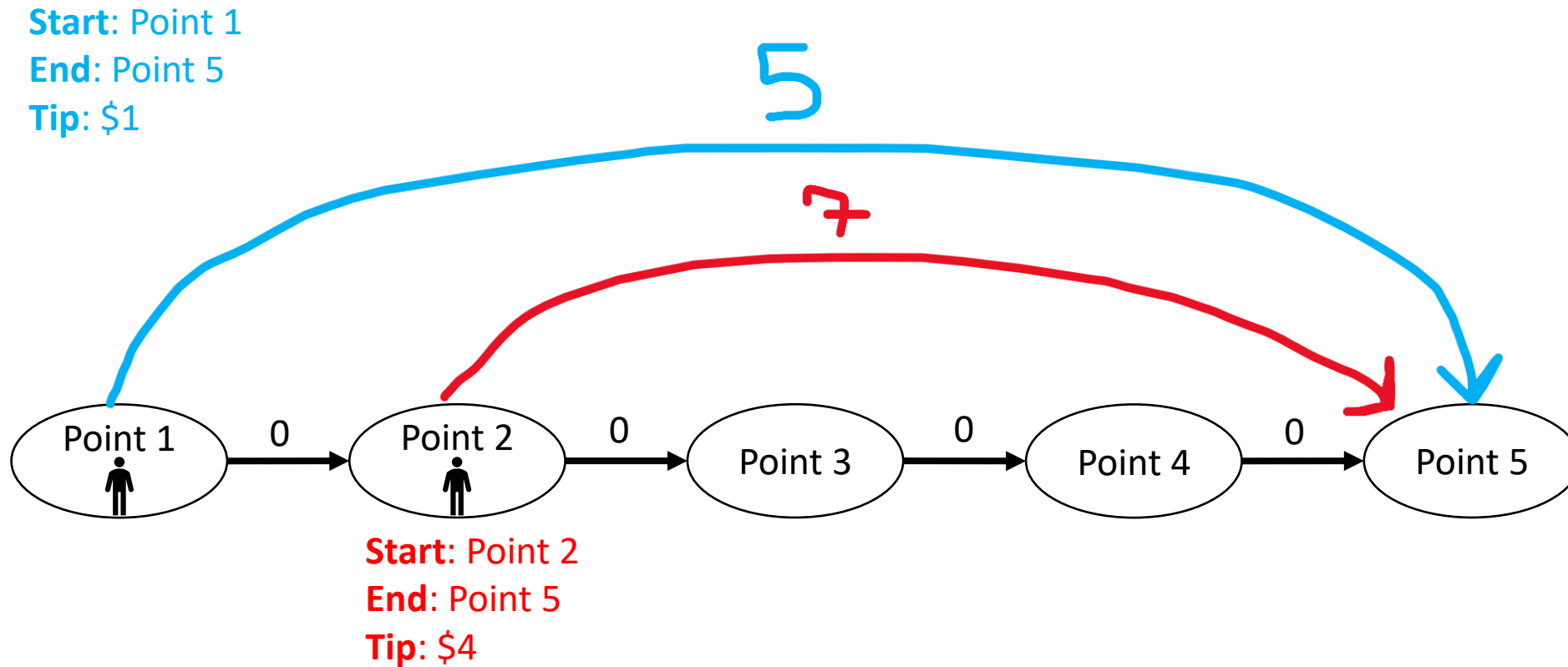
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?



Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?



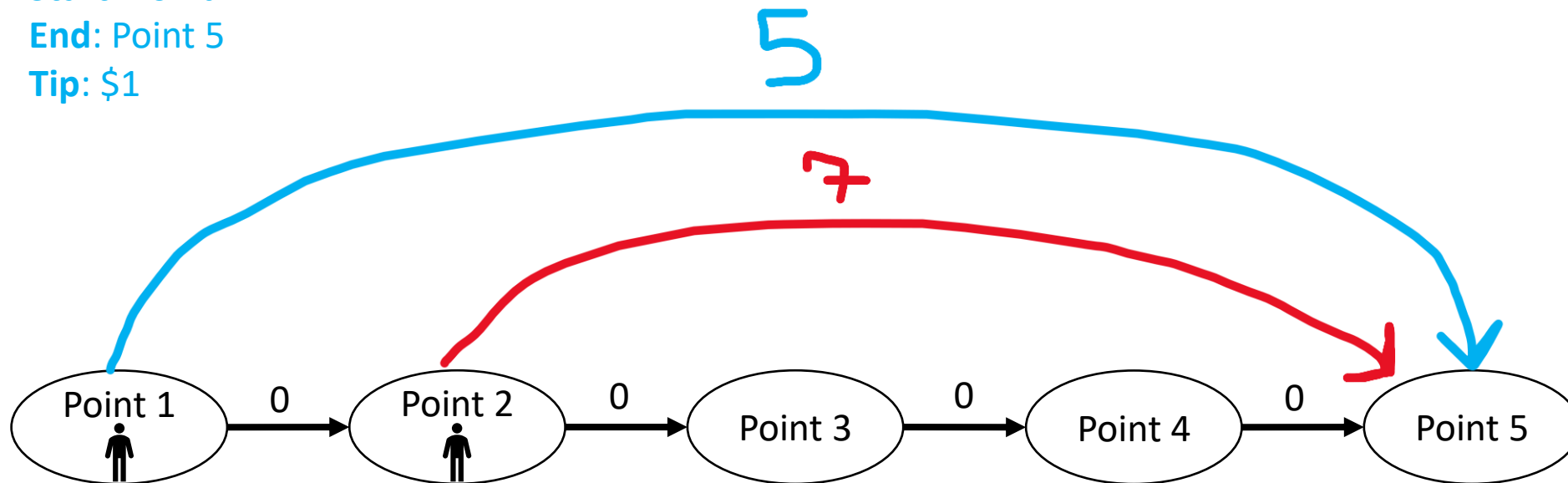
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

What is the *longest* path from point 1 to point 5?

Directed Acyclic Graph (DAG)- a directed graph that contains no cycles

Start: Point 1
End: Point 5
Tip: \$1

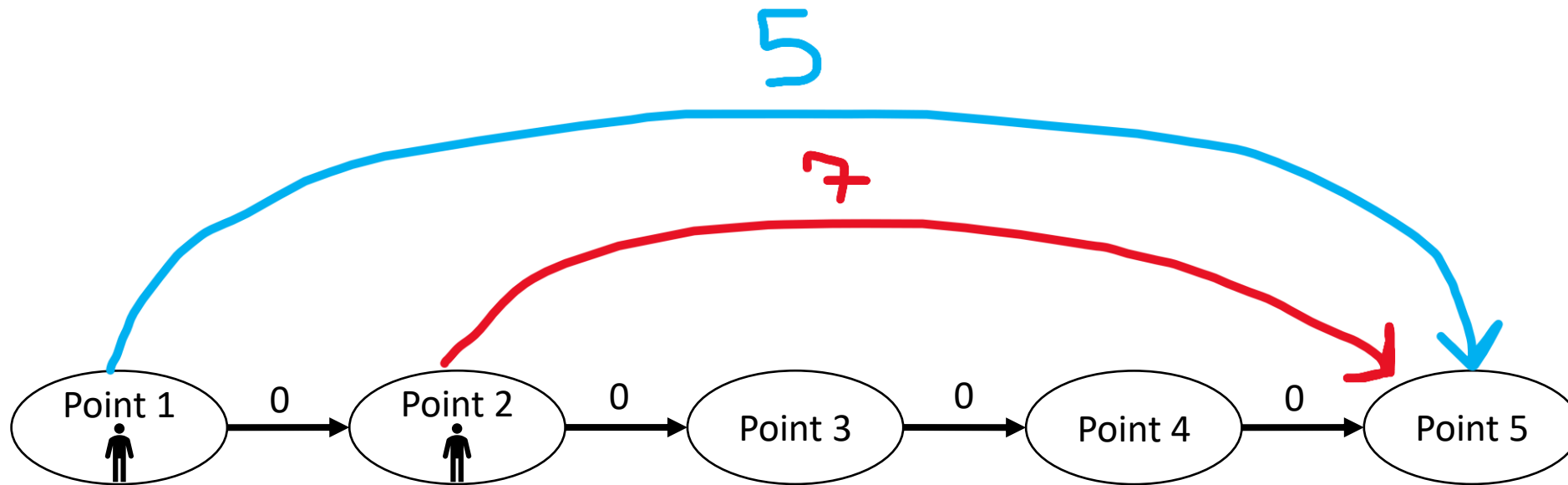


Start: Point 2
End: Point 5
Tip: \$4



Taxi Profit (Graph Representation)

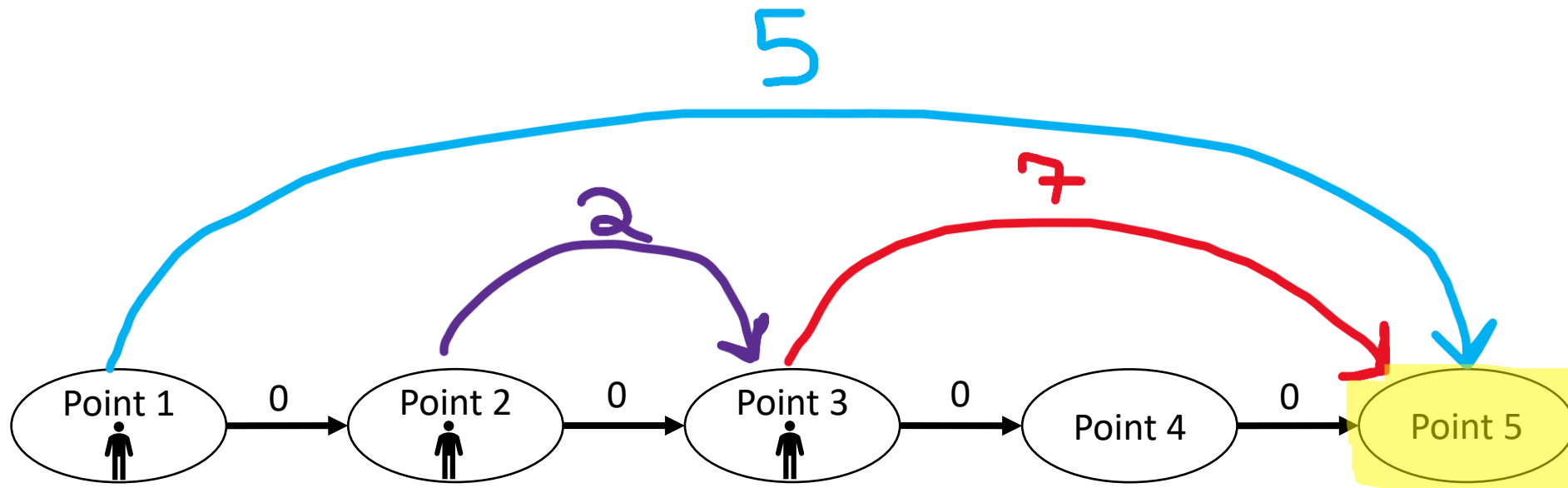
What is the **maximum profit** that the taxi can make when going from point 1 to point N?



Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

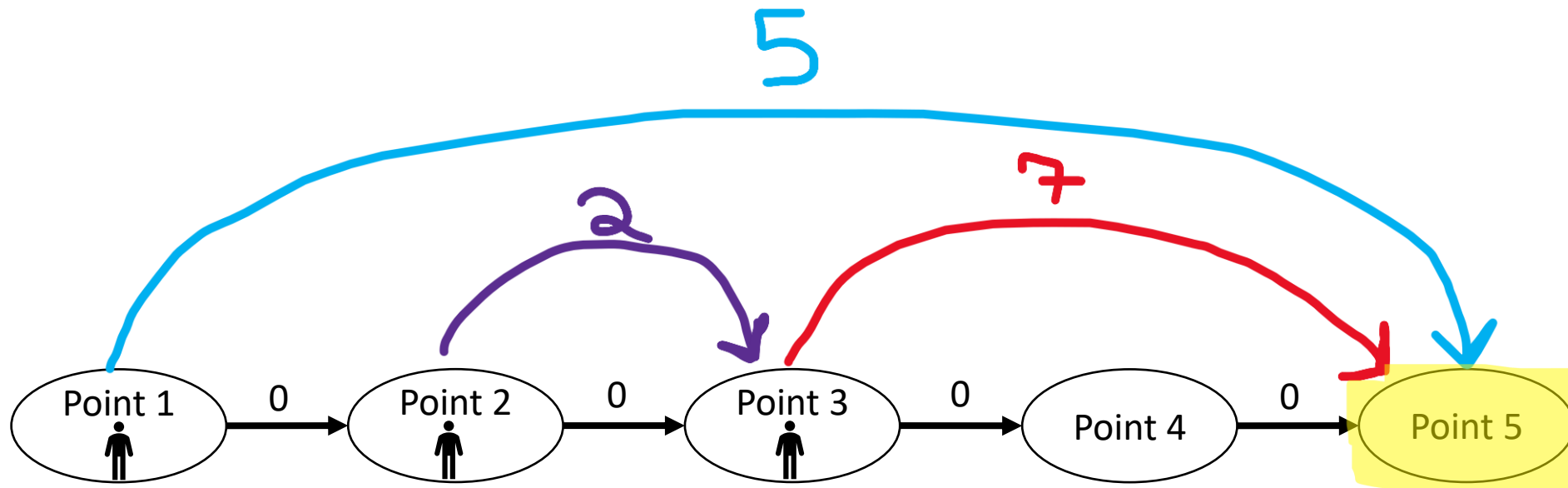


Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x



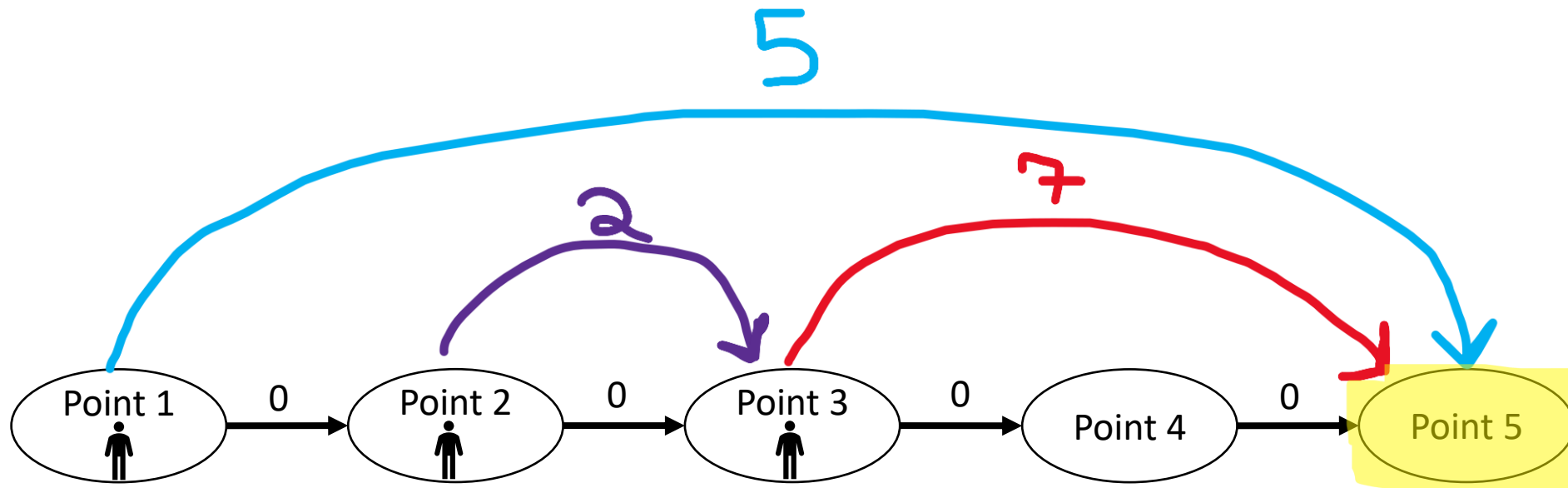
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(5) = ?$$



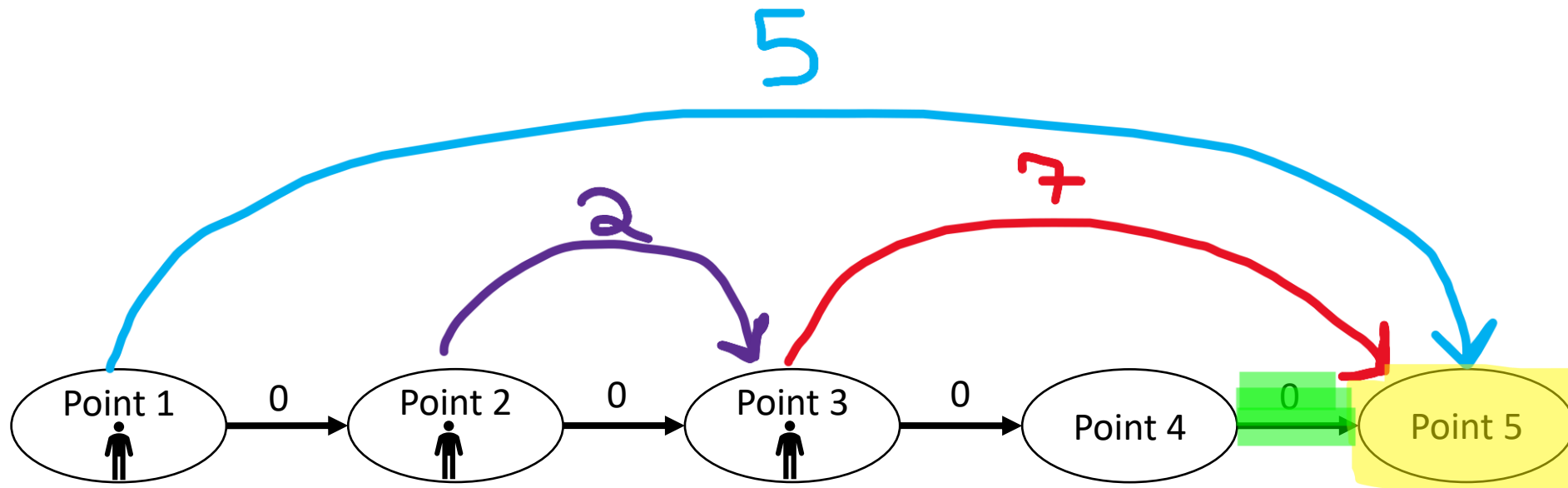
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(5) = B(4) + 0$$



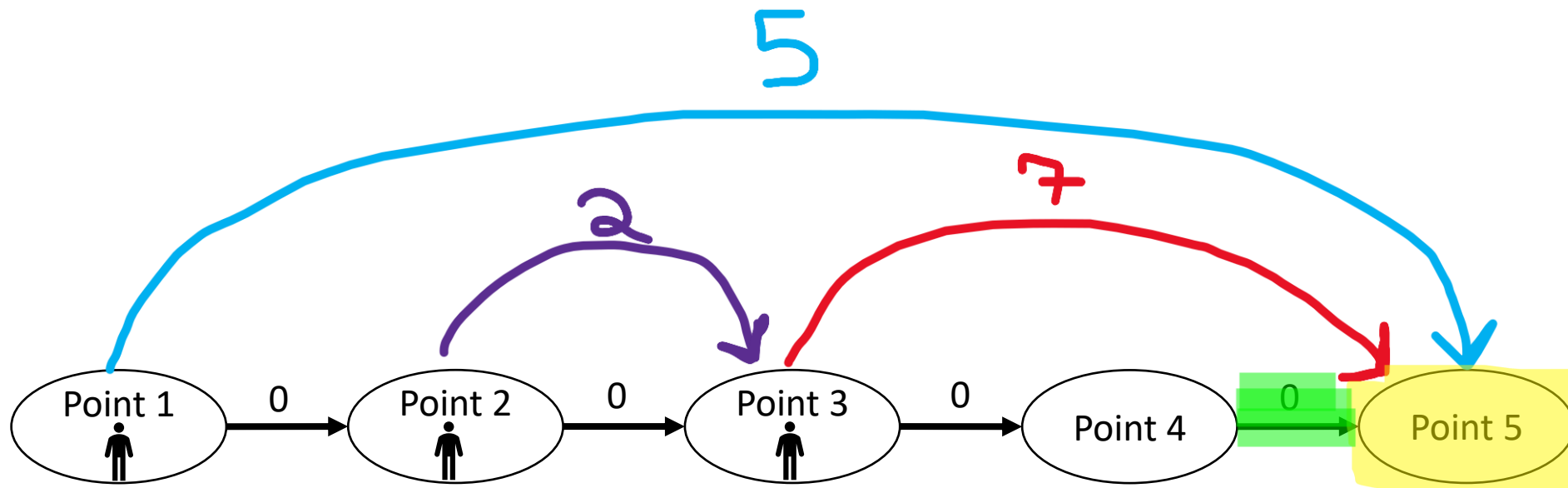
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(5) = B(4) + 0 \text{ or } B(3) + 7 \text{ or } B(1) + 5$$



Taxi Profit (Graph Representation)

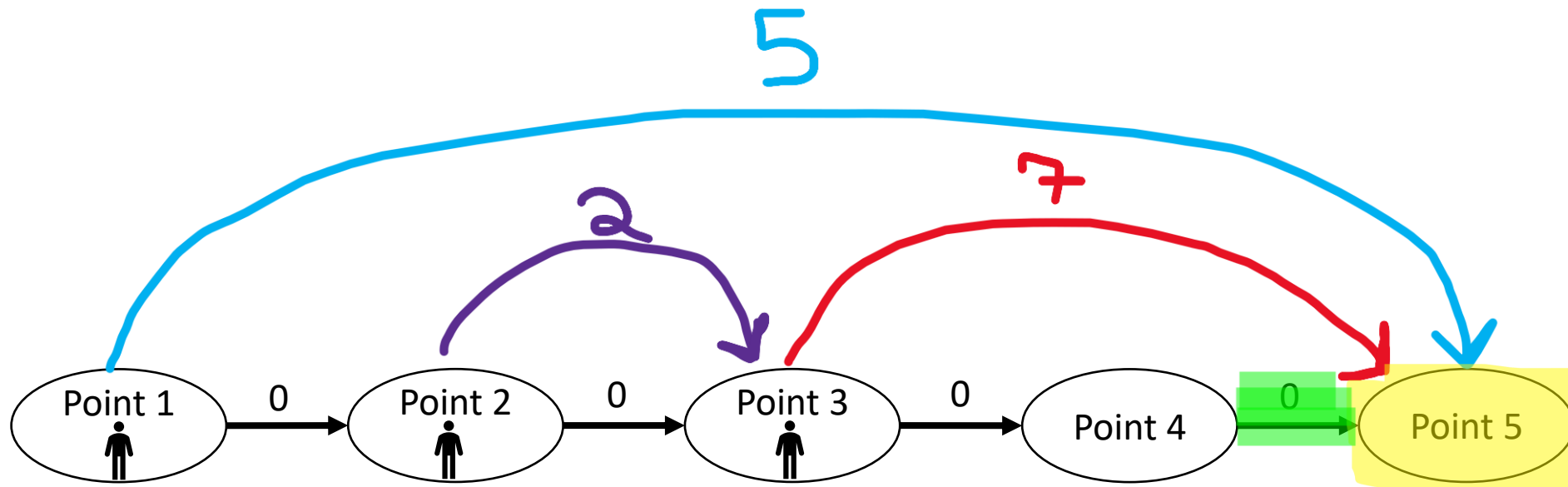
What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(5) = B(4) + 0 \text{ or } B(3) + 7 \text{ or } B(1) + 5$$

Optimal
Substructure



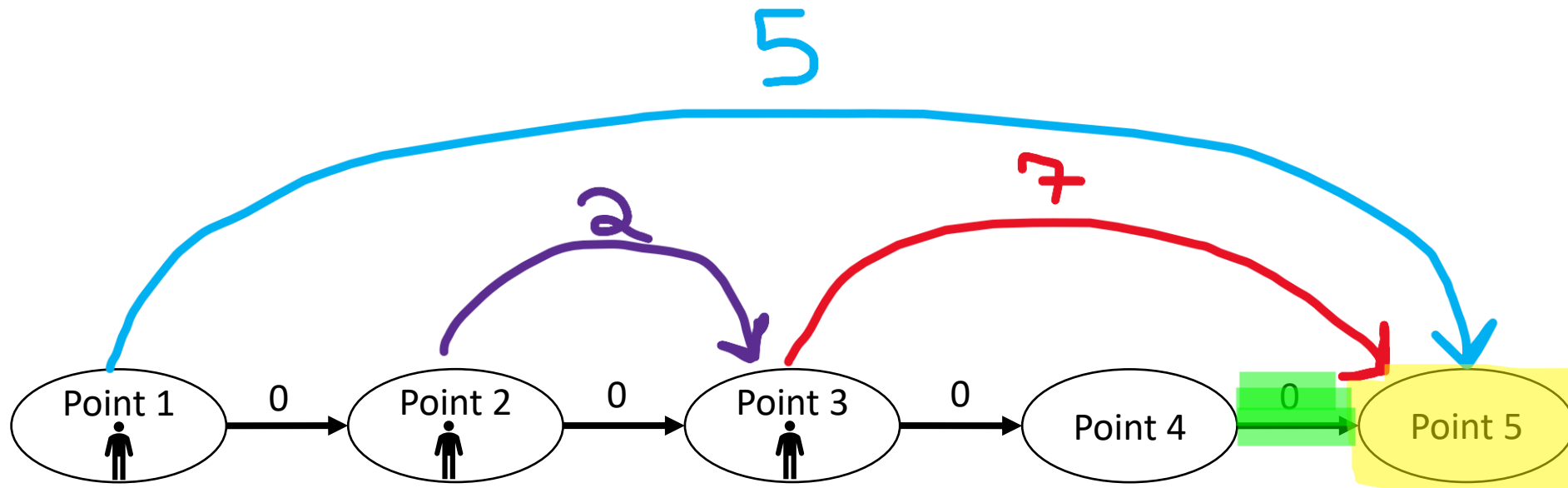
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(5) = B(4) + 0 \text{ or } B(3) + 7 \text{ or } B(1) + 5$$



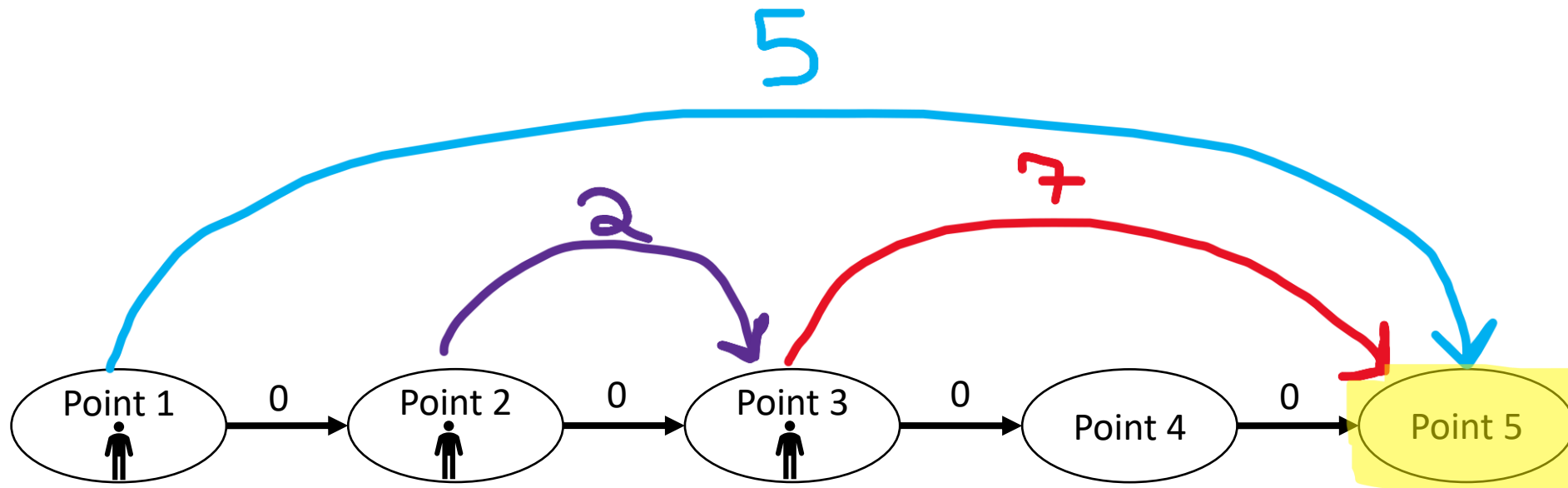
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(x) = \max \begin{cases} B(x-1) + 0 \\ B(x-i) + P(i,x) \\ \text{(for each edge that leads to point } x) \end{cases}$$



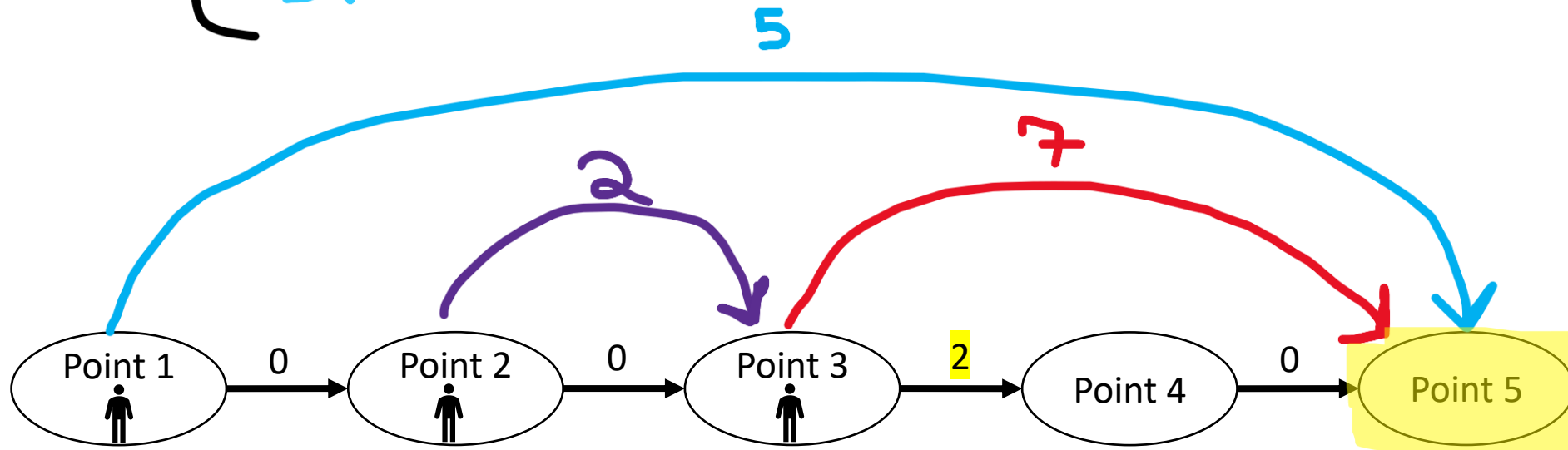
Taxi Profit (Graph Representation)

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(x) = \max \begin{cases} B(4) + 0 = 2 \\ B(3) + 7 = 2 + 7 = 9 \\ B(1) + 5 = 5 \end{cases}$$



Taxi Profit (Graph Representation)

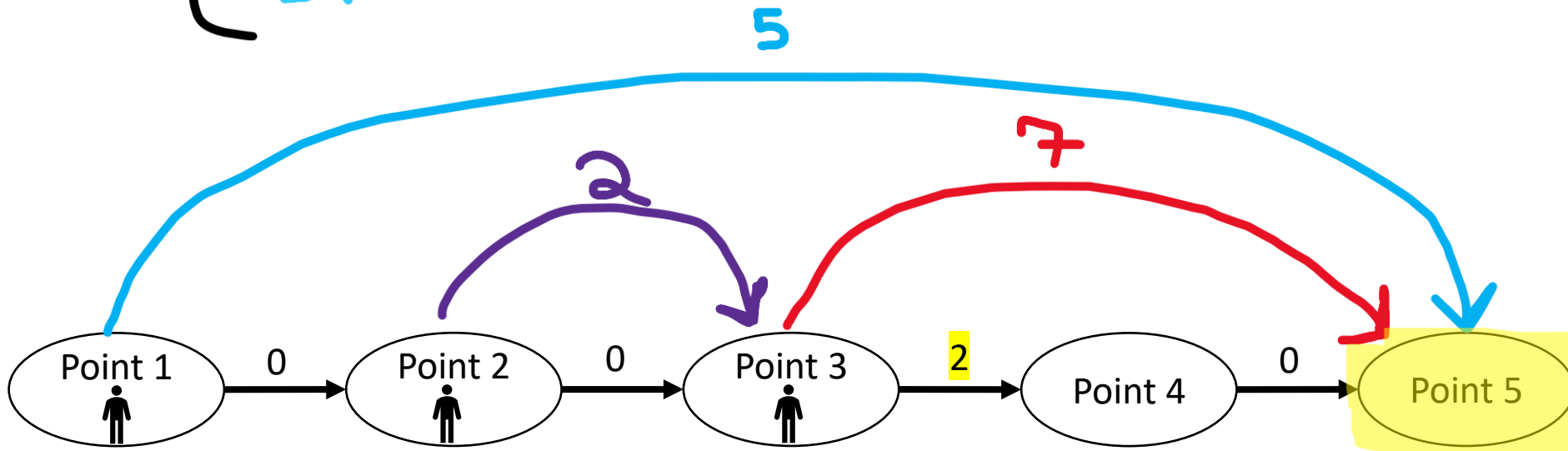
What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Let $P(i, x)$ be the profit made for a ride that goes from point 1 to point x

$$B(x) = \max \begin{cases} B(4) + 0 = 2 \\ B(3) + 7 = 2 + 7 = 9 \\ B(1) + 5 = 5 \end{cases}$$

Maximum profit = \$9



Taxi Profit (Graph Representation)

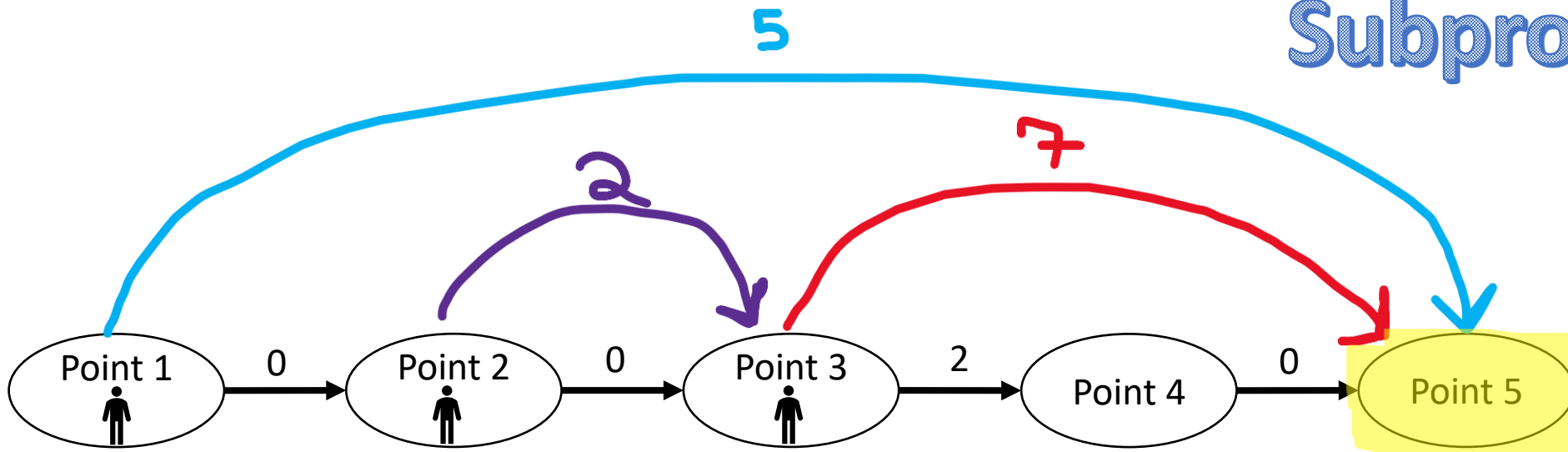
What is the **maximum profit** that the taxi can make when going from point 1 to point N?

To solve maximum profit from 1 to 5, we will solve :

- 1 to 4
- 1 to 3 (This may include *several paths* by picking up customers along the way ie 2 to 3)
- 1 to 2

2 to 3 may be a subproblem we solve several times

Overlapping Subproblems



To

-
-
-

DP

Optimal Substructure

olve

overlapping
problems

DP

Optimal Substructure

Overlapping subproblems

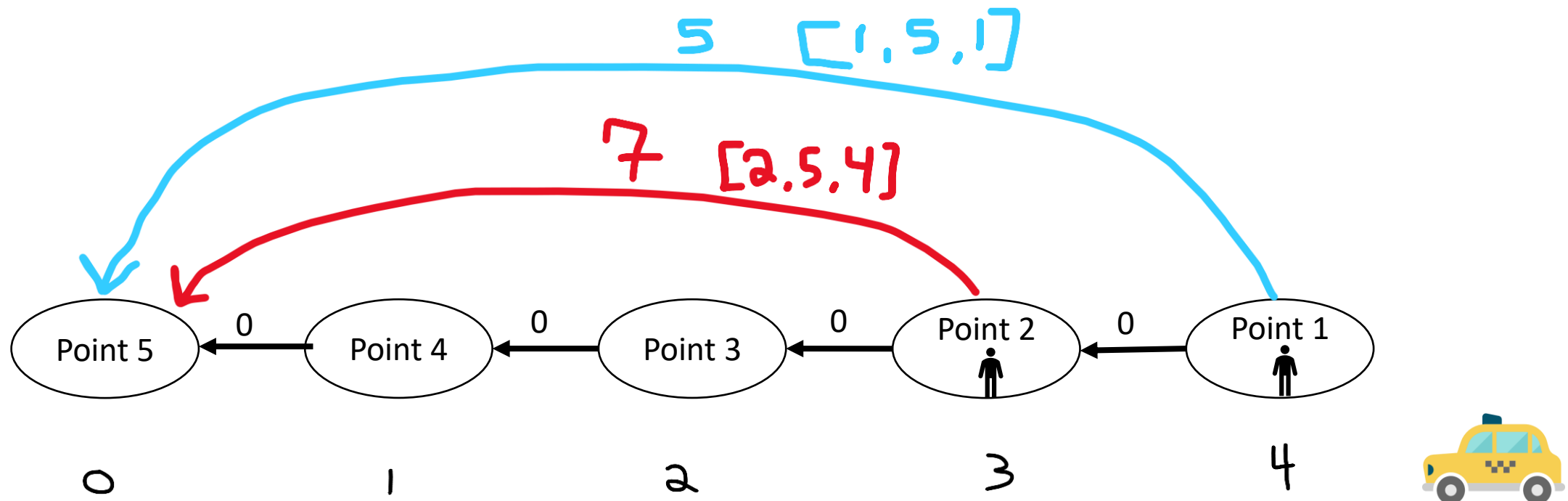
Point 5

Poi

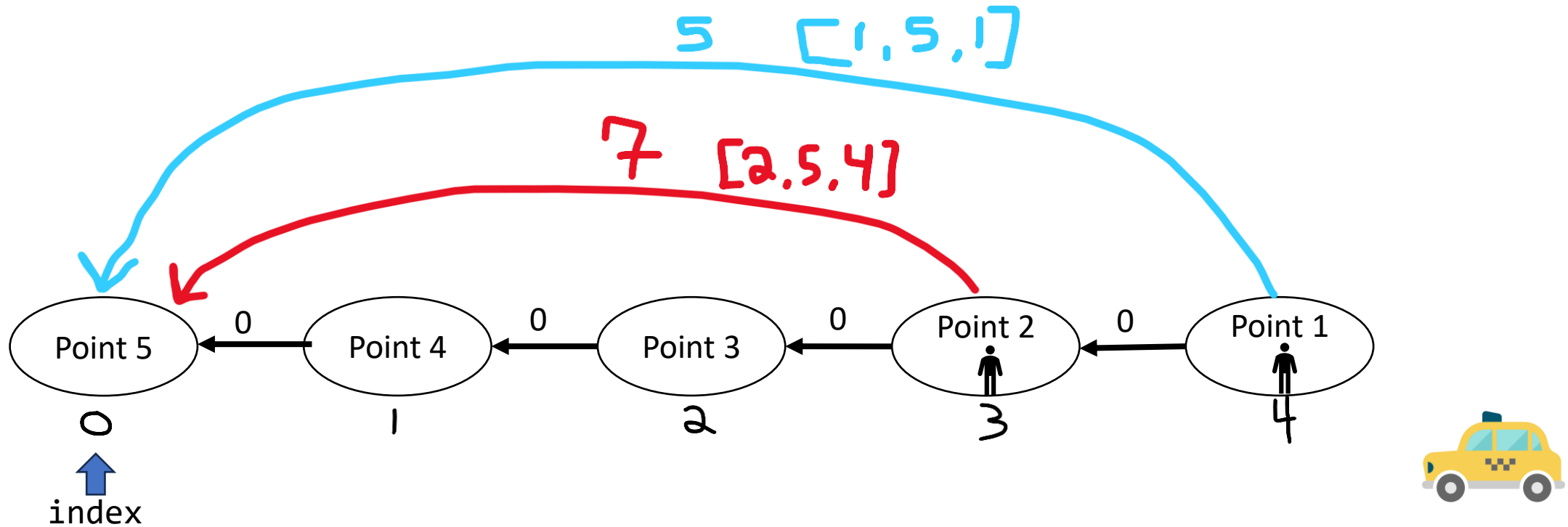


Taxi Profit

What is the **maximum profit** that the taxi can make when going from point 1 to point N?



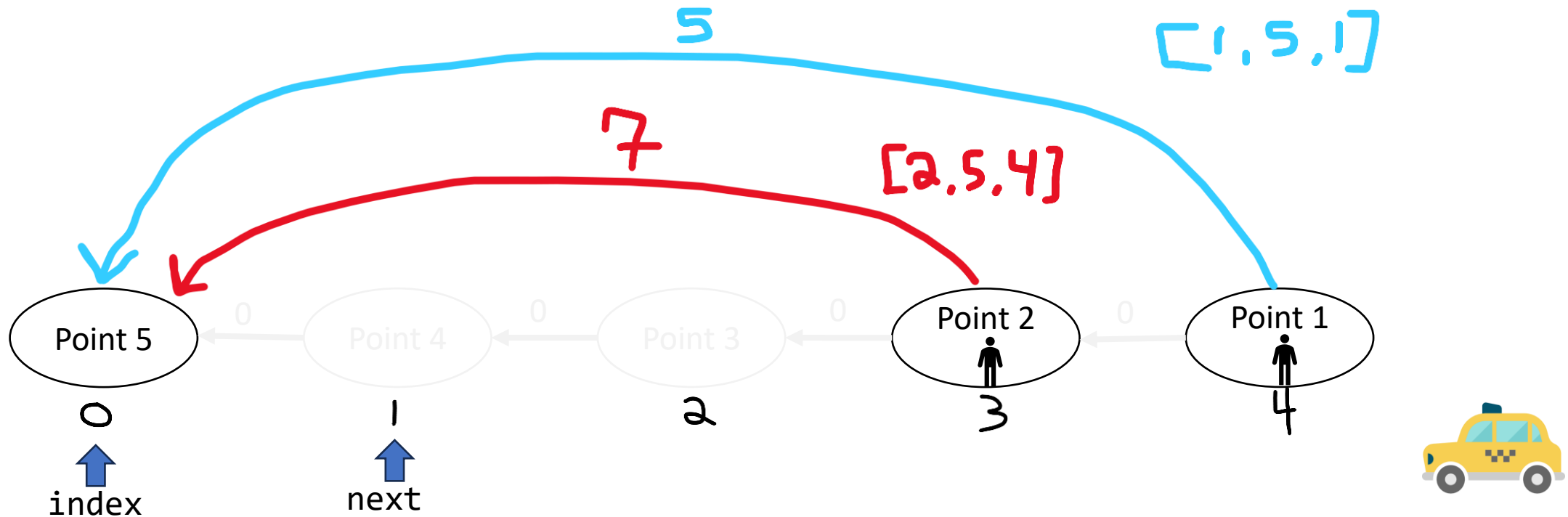
We are going to do this **Top-Down**



We are going to do this **Top-Down**

To solve B(5) we must solve B(4). There isn't an entry that starts at point 4, so must find the next closest customer

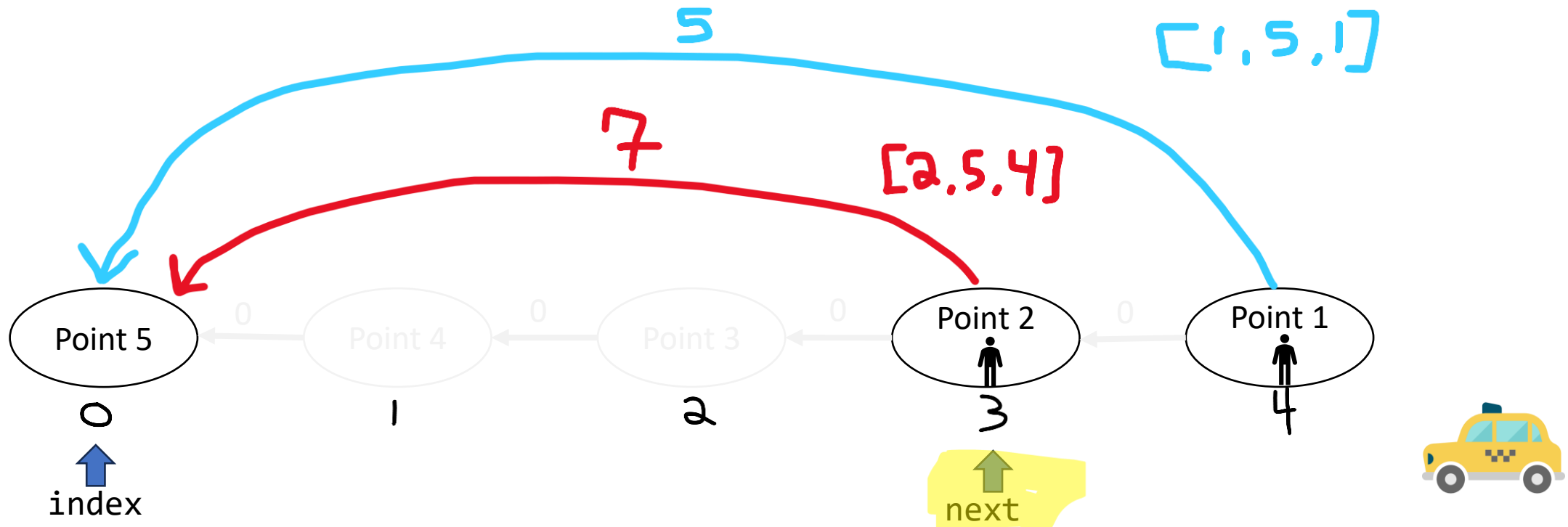
```
int[][] rides = [[2, 5, 4] , [1, 5, 1]]
```



We are going to do this **Top-Down**

To solve B(5) we must solve B(4). There isn't an entry that starts at point 4, so must **find the next closest customer**

```
int[][] rides = [[2, 5, 4] , [1, 5, 1]]
```



Taxi Profit

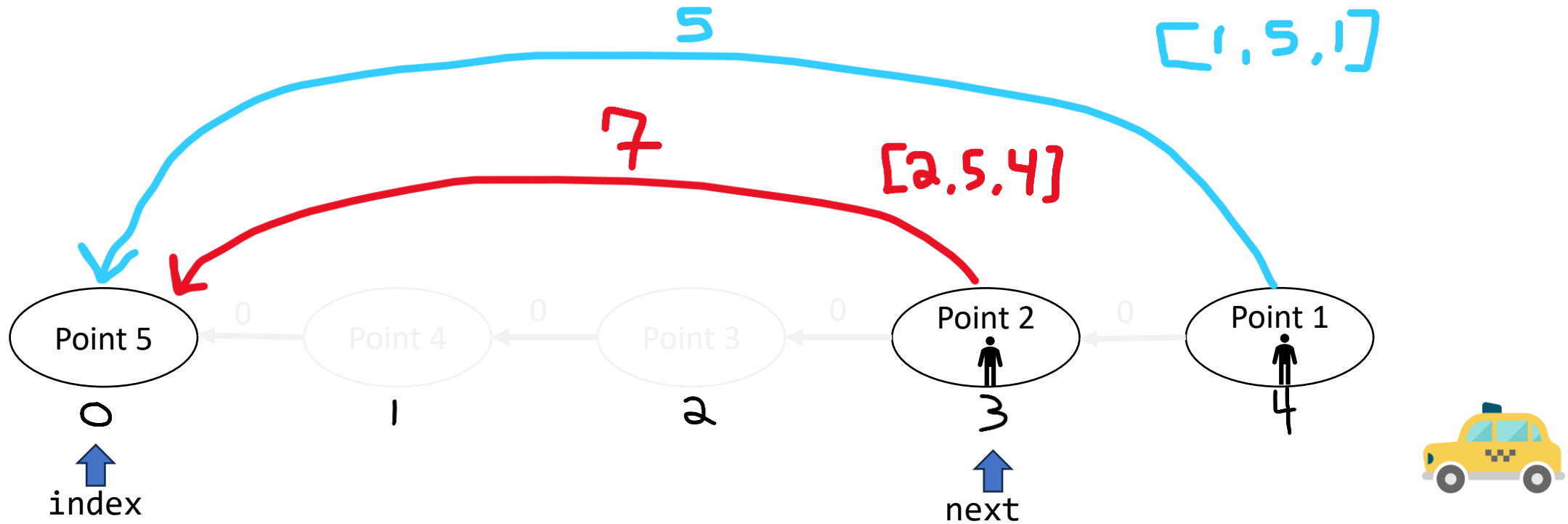
What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

We are going to do this **Top-Down**

To solve $B(5)$ we must solve $B(4)$. There isn't an entry that starts at point 4, so must find the next closest customer

```
int[][] rides = [[2, 5, 4] , [1, 5, 1]]
```



Taxi Profit

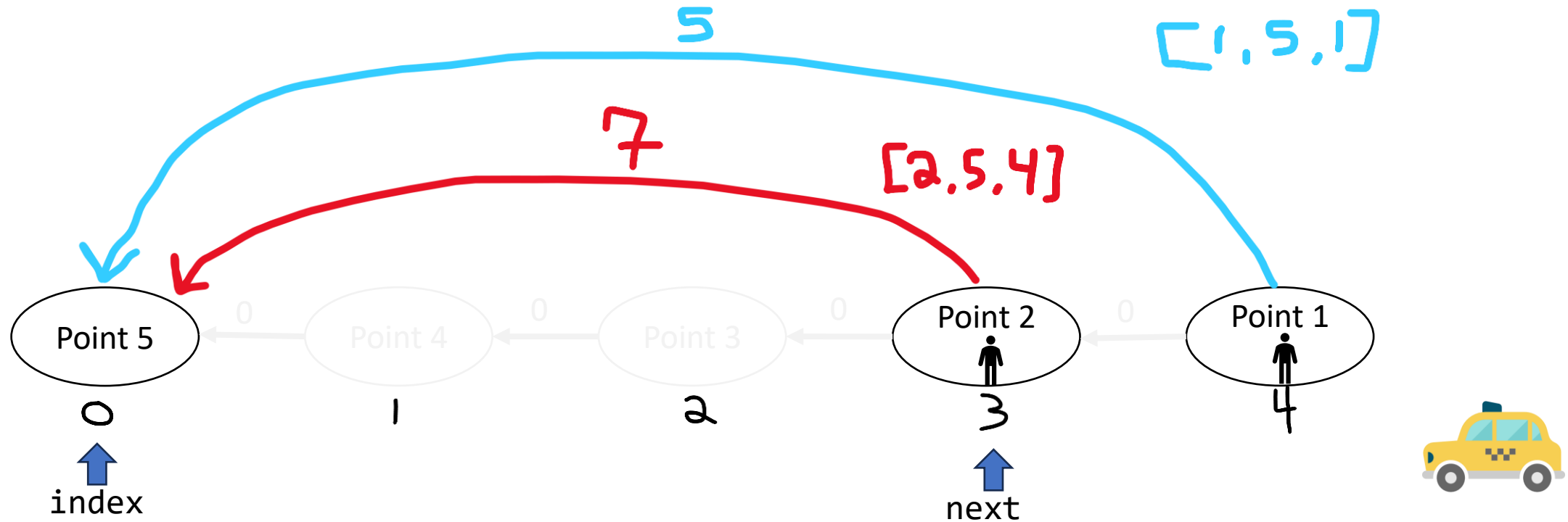
What is the **maximum profit** that the taxi can make when going from point 1 to point N?

Let $B(x)$ be the maximum cost to go from point 1 to point x

Either we **take** this customer, or we **skip**

take: $(\text{ride.end} - \text{ride.start} + \text{ride.tip}) + B(2)$ ↖ Recursive call!

“We pick up the customer, and add their payment to our profit so far”



Taxi Profit

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

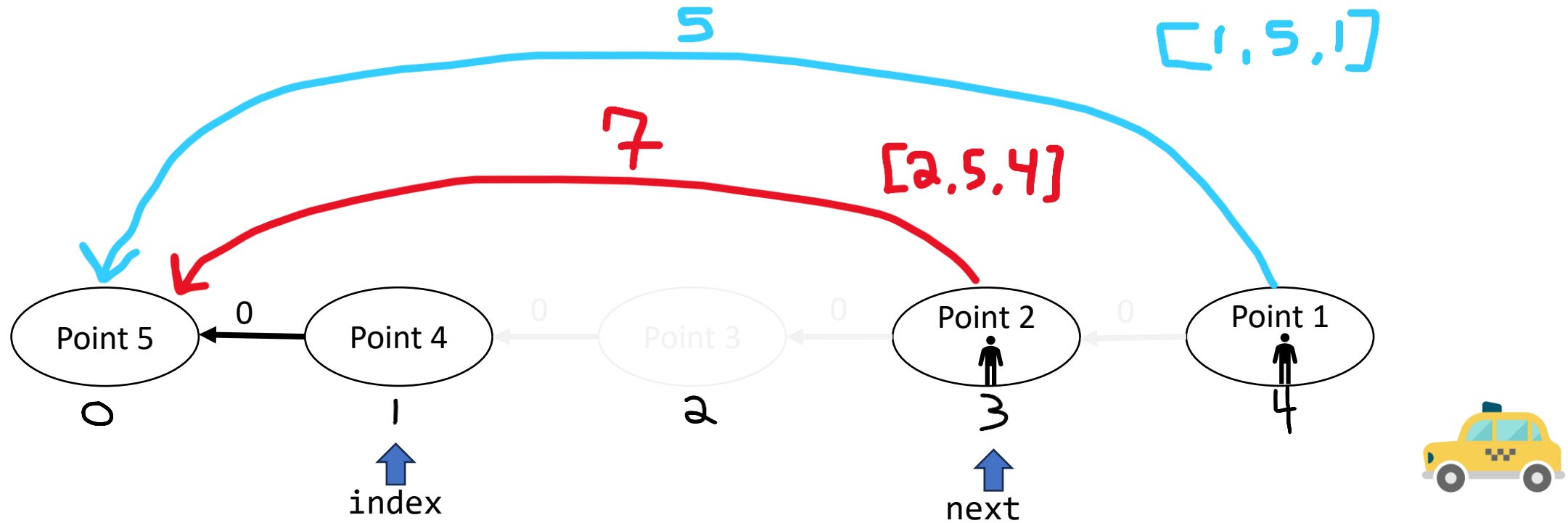
Let $B(x)$ be the maximum cost to go from point 1 to point x

Either we **take** this customer, or we **skip**

take: $(\text{ride.end} - \text{ride.start} + \text{ride.tip}) + B(2)$

Skip: $B(4)$

index + 1



Taxi Profit

What is the **maximum profit** that the taxi can make when going from point 1 to point N?

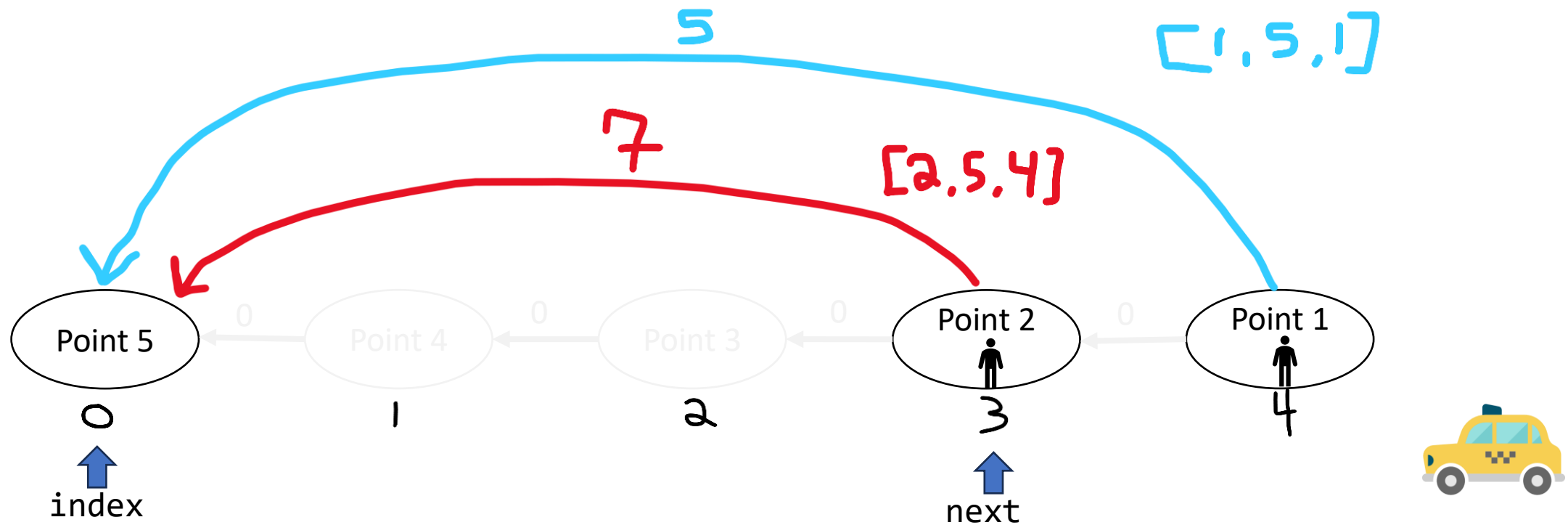
Let $B(x)$ be the maximum cost to go from point 1 to point x

Either we **take** this customer, or we **skip**

take: $(\text{ride.end} - \text{ride.start} + \text{ride.tip}) + B(2)$

Skip: $B(4)$

Take the Max choice, and
store answer in
memorization table

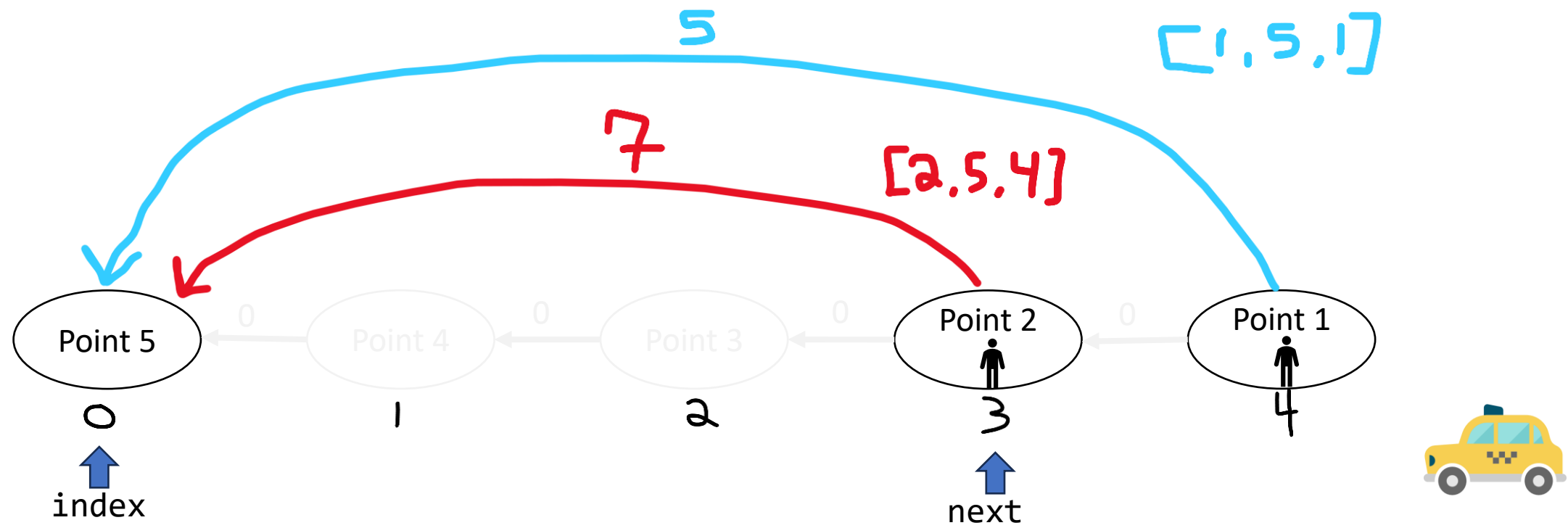


Taxi Profit

What is the **maximum profit** that the taxi can make when going from point 1 to point N?
Let $B(x)$ be the maximum cost to go from point 1 to point x

int[] dp

0	1	2	3	4

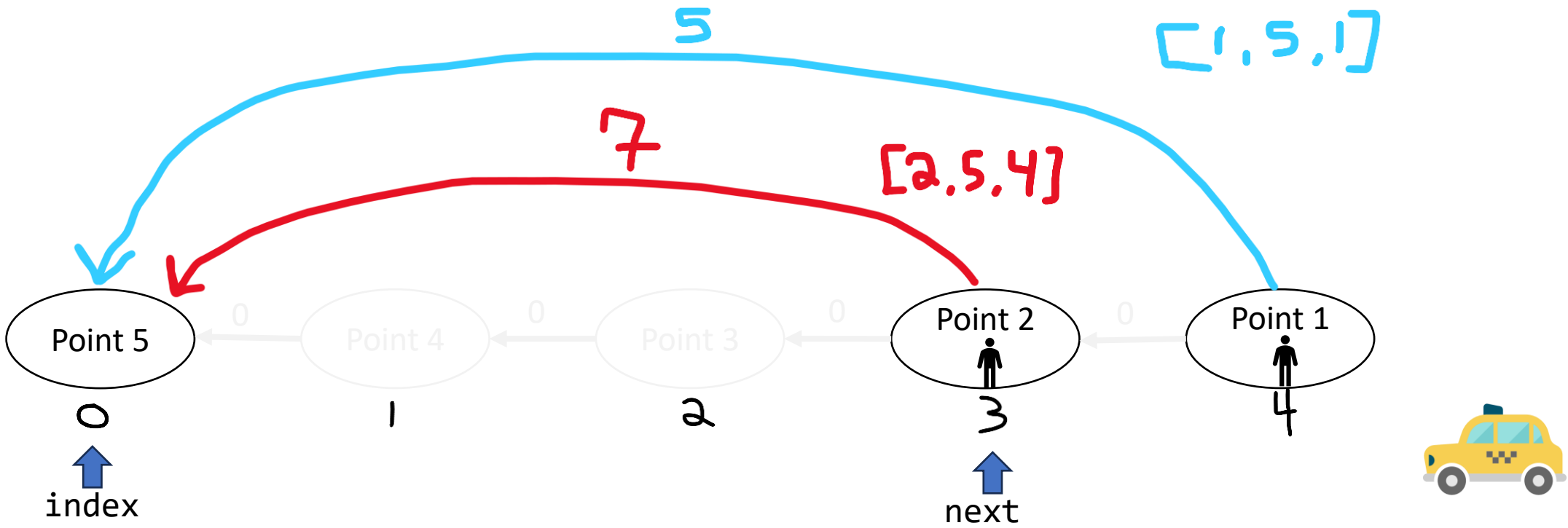


Taxi Profit

What is the **maximum profit** that the taxi can make when going from point 1 to point N?
Let $B(x)$ be the maximum cost to go from point 1 to point x

	0	1	2	3	4
int[] dp	7	0	0	0	0

↑ “The maximum profit to go from point 1 to point 5 (index 0) is \$7”



Taxi Profit

What is the **maximum profit** that the taxi can make when going from point 1 to point N?
Let $B(x)$ be the maximum cost to go from point 1 to point x

	0	1	2	3	4
int[] dp	7	0	0	0	0

“The maximum profit to go from point 1 to point 5 (index 0) is \$7”

