Finite Automata CSCI 338



Consider a car.

States:

??

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States:

- Moving
- Stopped

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Actions:

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Consider a car.

- •Gas
- Brake

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State Diagram



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Computational Question

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Deterministic Finite Automaton (DFA): An abstract model (machine) that determines (yes or no) if a string has a specific pattern.











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